

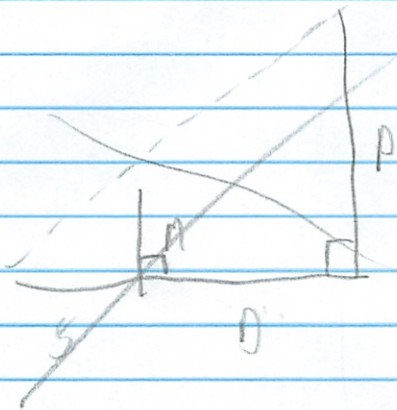
Shadows



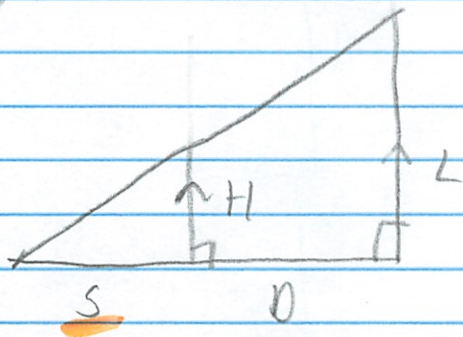
I am
sorry!!

- Carol

Shadows

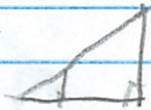


$$S = f(H, D, P)$$

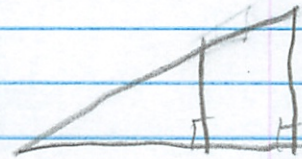


If 2 angles of 1 triangle are congruent to 2 angles of another triangle, the 3rd angle is \cong in both triangles

Other shadows



Short D ,
Long S



H is just shorter than L , long S

IF $H > L$ - no S - never meets



L is much greater than H , short S

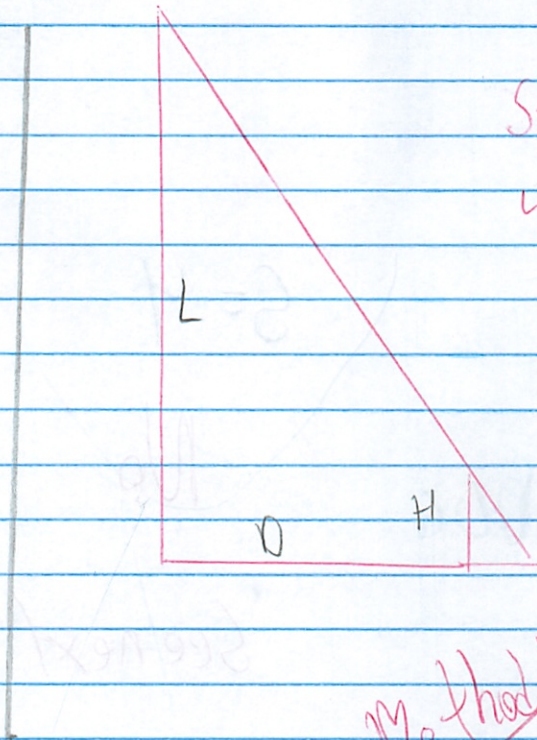
Longer D , smaller S



Longer D , smaller H & S
Taller H , longer S
Taller L , shorter S
IF $H > L$ - undefined
IF $D = 0, S = 0$

Watch Letters

#2



$$S = f(h, d, L)$$

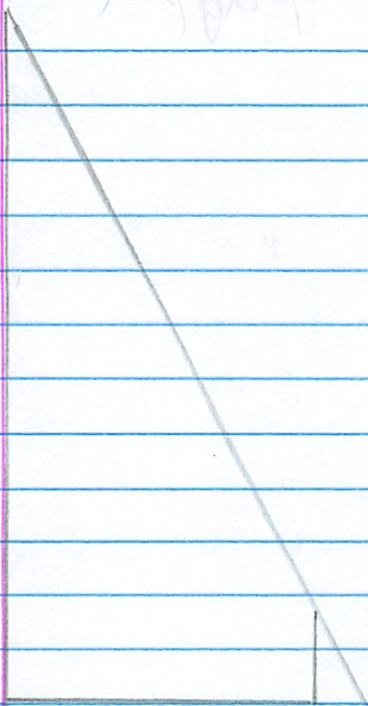
$$4 = f(6, 20, \frac{4}{6})$$

$$S = 4$$

Method

Draw + Measure

#1



If L is increased by 10, S is increased by 10. Otherwise insufficient data.

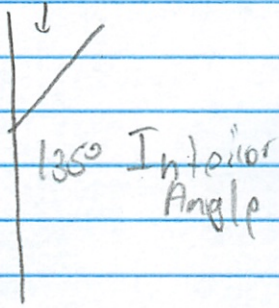
$$6/2 = 3$$

$$3 = f(6, 20, \frac{4}{6})$$

$$S = f(h, d, L)$$

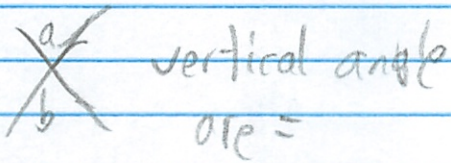
Angle

Exterior
 45°

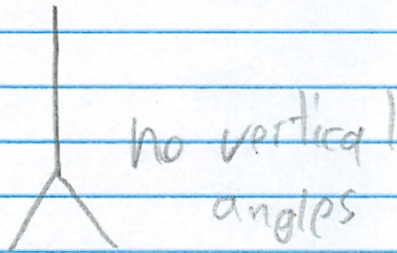
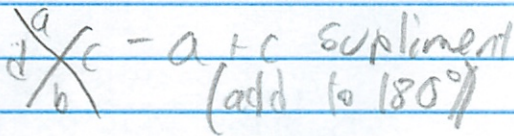


complementary add to 90°

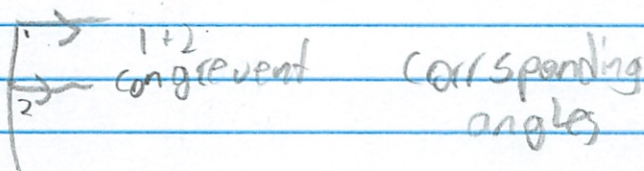
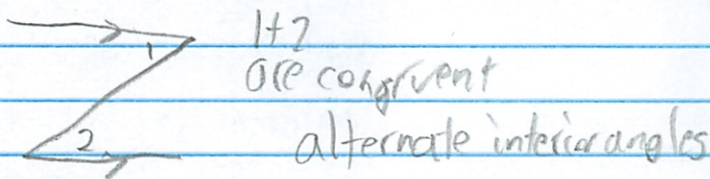
→ parallel symbol

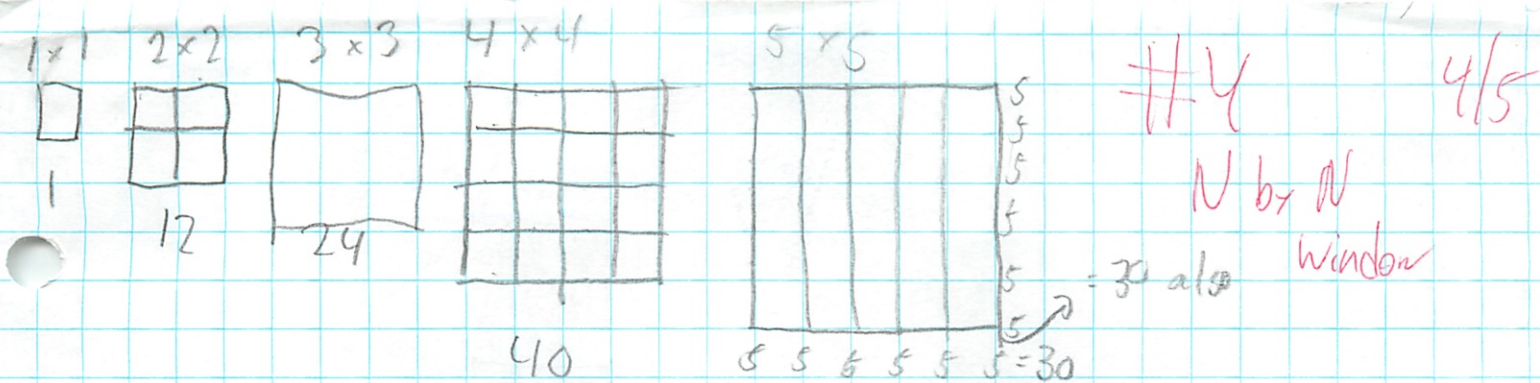


same ↓



If corresponding
angles are in proportion
triangle is similar.





6	84
7	112
8	144
9	180
10	220

$(n \times (n+1))$
 $30 + 30 = 60$
 60

$2(x^2 + x)$
 $2x^2 + 2x$

$2(n \times (n+1))$

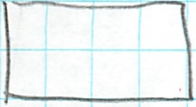
In a $n \times n$ square, there is 1 more row than what n is. The row is the length of n , ~~the column~~
 There are the same numbers of columns as rows

More Windows #15

4/5

$$(n^2 + n) + (m^2 + m)$$

$$(2^2 + 2) + (4^2 + 4)$$

$$m(4+2) + (6+4)$$


$$6 + 20$$

$$26$$

$$n^2 + n + m^2$$

$$4 + 2 + 16$$

$$8 + 16$$

$$22$$

$$3^2 + 3 + 2^2$$

$$9 + 3 + 4$$

$$16$$



$$n \times (m+1) + m \times (n+1)$$

$$2 \times (4+1) + 4 \times (2+1)$$

$$2 \times 5 + 4 \times 3$$

$$10 + 12$$

$$22$$

$$3 \times (2+1) + 2 \times (3+1)$$

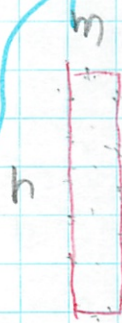
$$3 \times 3 + 2 \times 4$$

$$9 + 8$$

$$17$$

~~$$(n^2 + n) + (m^2 + m)$$~~

$$\underline{n^2 + n + m^2}$$



$$5^2 + 5 + 1^2$$

$$25 + 5 + 1$$

$$31$$

~~NO~~

$$5(1+1) + 1(5+1)$$

$$5(2) + 1(6)$$

$$10 + 6$$

1st My

2nd Aley

3rd My

Answer

$$(m+1)n + (n+1)m$$

#4, 5

Explanation

4/5

On a ~~1x1~~ window pane there are both horizontal



and vertical lines. On this size 1x1

square there are 2 horizontal lines + 2 vertical lines.



On a 2x2 square there are 3 horizontal + 3 vertical lines.
You notice that the number of horizontal + vertical lines are the same on a square



With a 2x1 square, there are 3 horizontal line and 2 vertical.

You may notice that the # of horizontal lines is whatever the number of rows of the square is plus one.

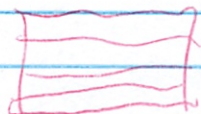
This is the same for vertical lines and the number of columns

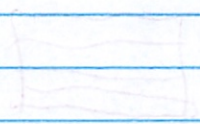
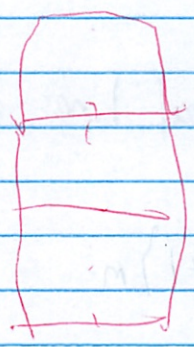
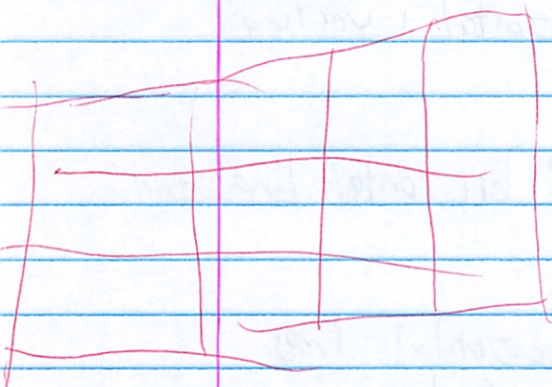
Therefore: $n(n+1) + (n+1)n$

or a square $2(n \times (n+1))$ or $2n^2 + 2n$

Whats with $n \times n + 1$ the $n+1$ because window is not 1/1p

I forget





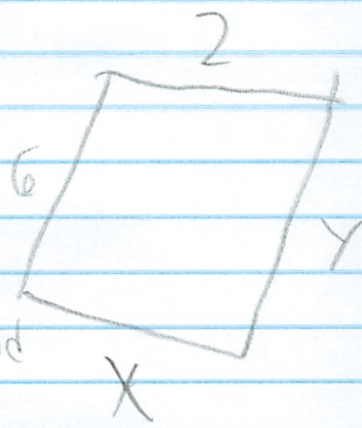
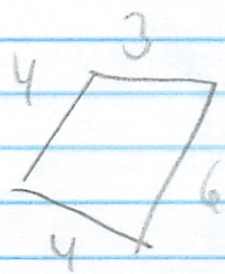
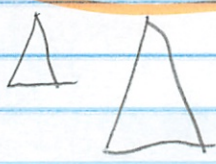
Same Shape (#6)

4/7

1. Not same, similar

2. all angles must be same measure, side must change.

*** polygon - same angles and corresponding sides must be in proportion**



angles correspond

$$x = 6$$

$$y = 9$$

$$z = 4.5$$

$$\frac{2}{3} = \frac{4}{6} = \frac{4}{x} = \frac{6}{y} = \frac{3}{2}$$

must hold same ratio or proportion

ratios

$$\frac{3}{2} = \frac{4}{4} = \frac{12}{8}$$

still

3. a. not same shape

b. different

c. - similar - bases are same must do

d. - different - flipped + different (use ratios)

Check Rule

State of Liberty (#7)

4/7

1. David's nose = 2" Statue = 4'6"
Dave's arms = 33" Statue arms = ?

Don't
relate ~~$\frac{2}{33}$~~

$$\frac{2}{54} = \frac{33}{?}$$

David
statue not Nose
Arm

$$\frac{2}{54} = \frac{33}{?} = 891/12$$

741 3" = Statue Arm

parts of 1
parts of 2

Counter Examples

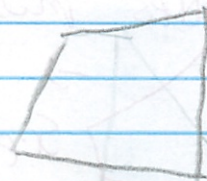
#1

True, 1 side is relate



will change - if change other angles

#2 False



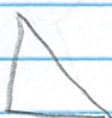
#3 True, also has 3 angles the same

#9

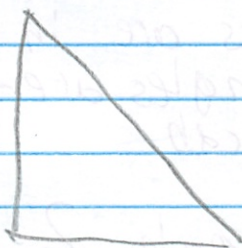
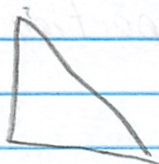
#1 True



#2 False



#3 True



but what about

The And M.C.T
underlined 3
times in statement

Check no cap in next pgs.

but can only be similar if

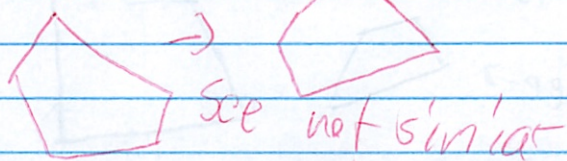
- angles are = and

- all sides in proportion

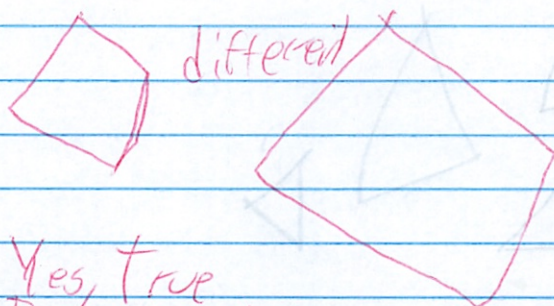
Back for re-do

Resto

p422- #11 - F sides must also be in proportion



#12 F - same as above - must have both



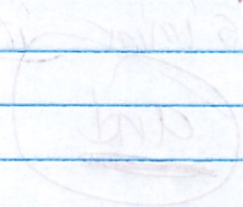
#13 Yes, True

If 2 sides are in proportion then it's similar,
so 2 angles are =

#14 #11 True - see vocab

#12 True - see vocab 2 - If 2 sides
are =, triangle are =

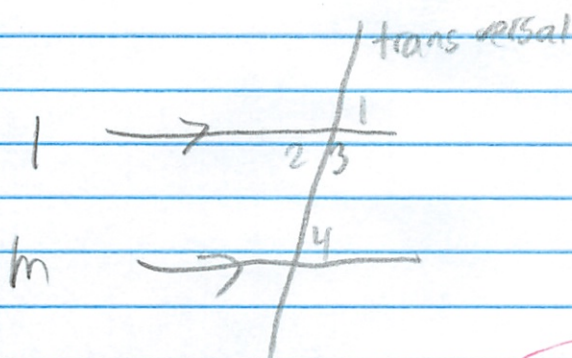
#13 True - see vocab



all angles in proportion

ab - 91 - not ab

Geo Vocab



\cong = Congruent
 \sphericalangle = angle
 $m\angle$ = measure of angle

Vertical angles ($\sphericalangle 1 \cong \sphericalangle 2$) are congruent

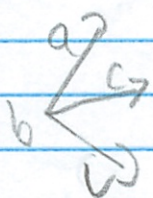
2 angles sum to 90° = Complementary

" " + " " 180° = Supplementary

$\sphericalangle 1 + \sphericalangle 3$ are adjacent

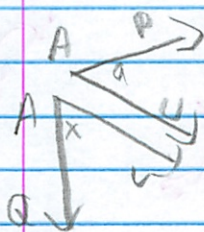
$\sphericalangle 2 + \sphericalangle 3$ are adjacent

$m\angle 1$ and $m\angle 4$ are equal
 Parallel lines cut by transversal
 Corresponding angles are \cong
 $m\angle 2$ and $m\angle 4$ are equal
 parallel lines cut by a transversal
 Alternate interior angles are \cong



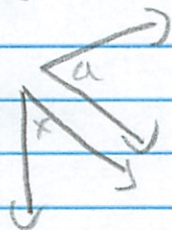
angle $\sphericalangle abc$
 $\sphericalangle abc$

are adjacent



not adjacent because share common ray

removed labels

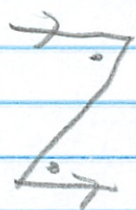


not adjacent

because you don't know that they share

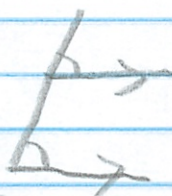
Geo Vocab Cont

4/8



\bullet = alternate interior angle

$m\angle 1$ = measure of angle 1



\curvearrowright = corresponding angles

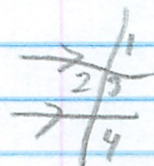
Mini Proof

Statement

Reason

$$\angle 1 \cong \angle 4$$

Given: parallel lines cut by a transversal corresponding \angle 's are \cong



$m\angle 1 = m\angle 4$

Prove

$m\angle 2 = m\angle 4$

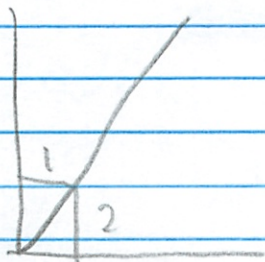
$$\angle 1 \cong \angle 2$$

vertical angles are \cong

$$\angle 2 \cong \angle 4$$

transitive property

\downarrow
If $a \cong b$ and $a \cong c$ then $b \cong c$



complementary

$$m\angle 1 + m\angle 2 = 90^\circ$$

Geometry Vocab

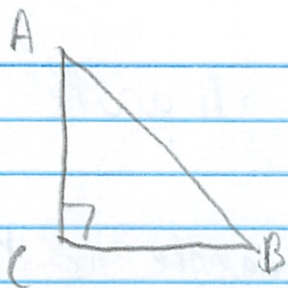
4/11

- 2 polygons (with the same # of sides) are similar if
 - their corresponding angles are equal and
 - their corresponding sides are proportional in length
- The line through 2 points A and B will be written as \overleftrightarrow{AB}
- The line segment connecting A and B will be written as \overline{AB} and the length of this segment will be written as AB .
- The ray from A through B will be written as \overrightarrow{AB}
- If the sides of a triangle have the same lengths as the corresponding sides of another triangle, then the triangles must be congruent.
- If the sides of 1 polygon have the same lengths as the corresponding sides of another polygon, then the polygons do not have to be congruent.
 - like a square w/ all sides = 4 is not like a rhombus w/ all sides 4 length
- If 2 triangles have their corresponding sides proportional, then the triangles must be similar.
- If 2 triangles have their corresponding angles equal, then the triangles must be similar.

(ent \rightarrow)

Geo cont

4/4



A right triangle is a triangle w/ a right angle

The 2 sides that form the right angle \overline{AC} and \overline{BC} are called the leg,

The side opposite the right angle, \overline{AB} is called the hypotenuse.

Each of the acute angles of a right triangle is formed by the hypotenuse and one of the legs. Angle A is formed by the hypotenuse \overline{AB} and by the leg, \overline{AC}

The leg that helps form an acute angle is said to be adjacent to that angle. \overline{AC} is the leg that is adjacent to angle A

\overline{AC} is said to be opposite to angle B.

If the legs of 2 right triangles are proportional, then the triangles must be similar.

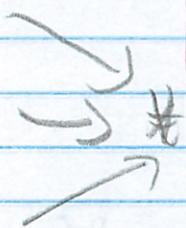
2 lines that meet at right angles are called perpendicular

A triangle with an obtuse angle is called an obtuse triangle

Over

A triangle whose angles are all acute angles is called an acute triangle

The sum of the angles of a triangle is 180°

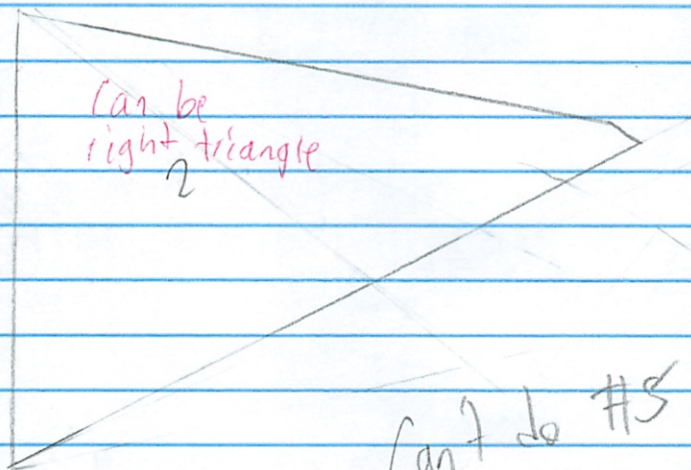
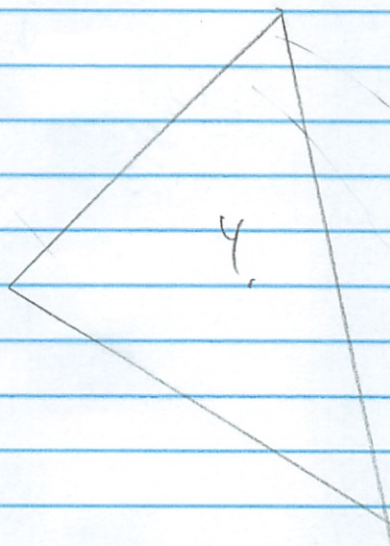
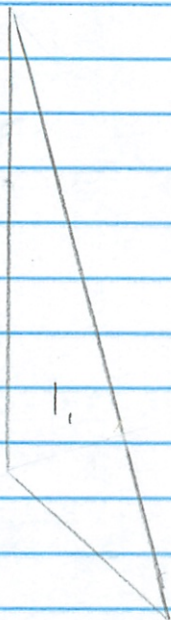


* The sum of lengths of any 2 sides of a triangle must be more than the length of a third (this is called triangle inequality)

* If 2 angles of 1 triangle are = to 2 angles of another triangle, then the triangles must be similar.

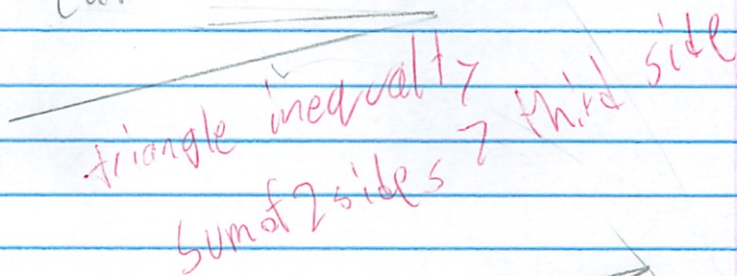
Warm up
Draw triangles

4/12

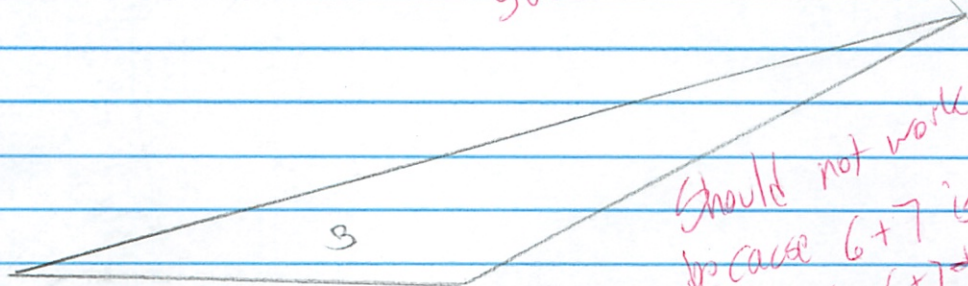


Can be
right triangle
2

Can't do #5



triangle inequality
sum of 2 sides > third side

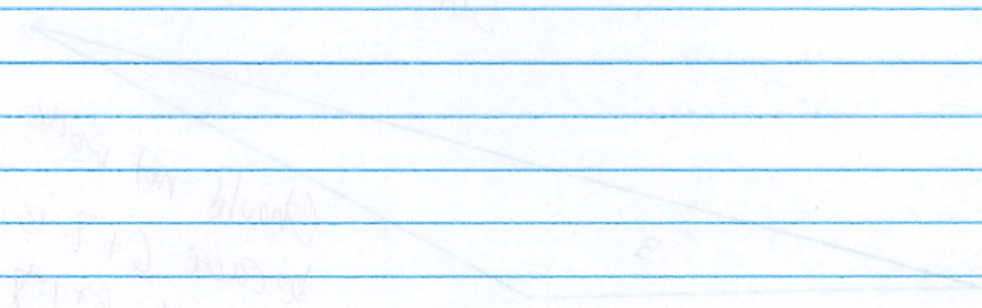
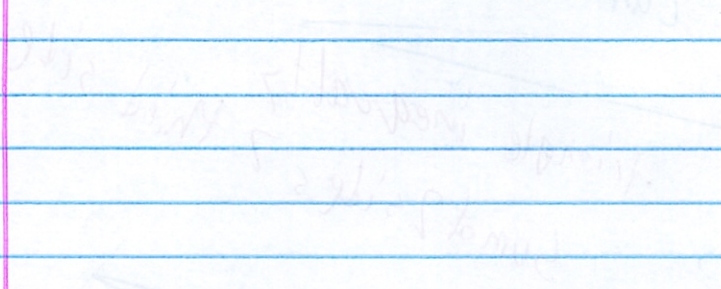
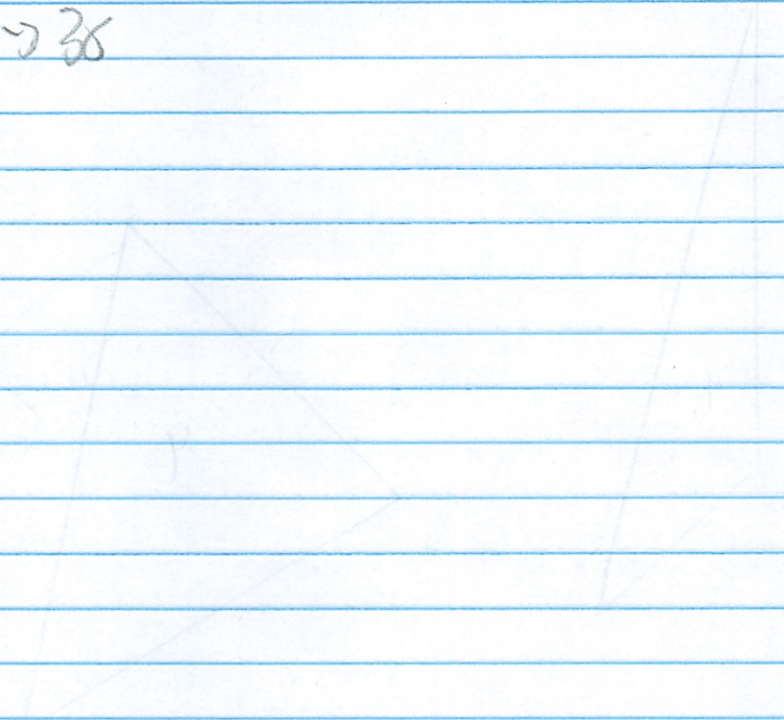


Should not work
because $6 + 7$ is not > 13
or $6 + 7 < 13$

Warm up
Area triangles

1. $72^\circ, 78^\circ, ? \rightarrow 30$

$$\begin{array}{r} 180 \\ - 72 \\ \hline 108 \\ - 78 \\ \hline 30 \end{array}$$



Very Special Triangles (#12)

4/13

1. The 2 other angles must both be acute because 1 angle is 90° , and 3 angles must sum to 180° . That leaves 2 angles w/ 90° to split between them. An angle can't be 0° in a triangle so it must be 89° and 1° and they would still be acute.

2. ? only 2 angles to account for
 $90^\circ \times 4$ makes a complete turn
we build and make squares w/ right angles
a square is 2 right triangles
measure hypotenuse *trigonometry*

3. Hypotenuse is longer than legs
Hypotenuse length is figured using lengths of legs

4. See back #1 and #2

a it is double

b they are the same

c they are in proportion + are similar

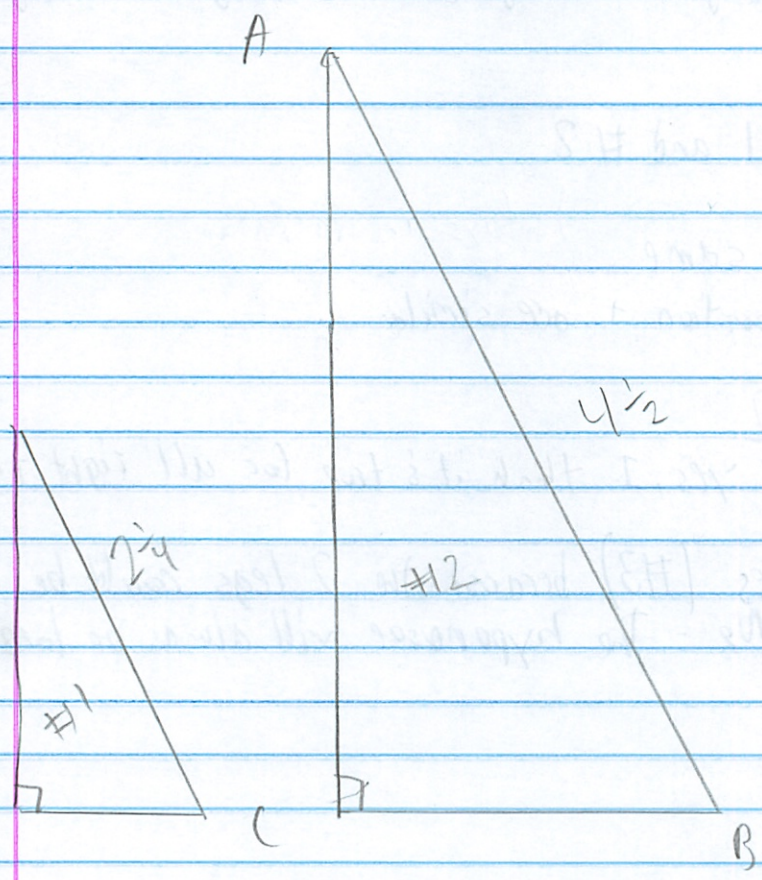
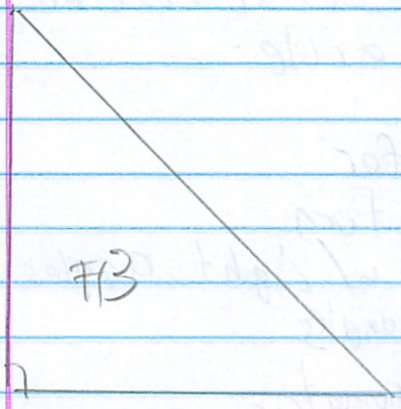
5. See back #2

opposite - yes, I think it's true for all right triangles

6. Isosceles - Yes (#3) because the 2 legs could be =
Equilateral - No - The hypotenuse will always be longer

(11) Vertical Triangle #12

8/14



What's Possible

p432

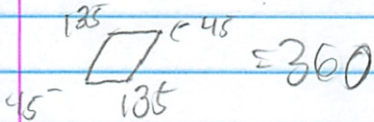
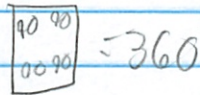
4/12

Part 1 ~~Angles~~ Angles must add to 180°

Part 2 Sides must be more than third.

Triangle Inequality

Part 3 Angles

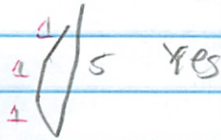


(*) A Quadrilateral will sum to 360°

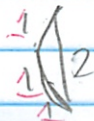
Quad

Sides

? All sides must be more than fourth



$$S_1 + S_2 + S_3 > S_4$$



$$5 < 1$$

$$\sum 7 < 4$$

(*) Yes 3 sides must be shorter than 4th

Part 4 Angles

Sides	Total
3	180
4	360
5	540
...	...

(*) n $(n-2) \cdot 180$ - or -
 $180(n-2)$ or
 Source: Prior knowledge
 $180n - 360$

Poly

Sides

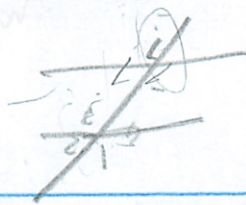
Quad Rule

Penta Rule \rightarrow 4 sides must be shorter than 5th

(*) Poly Rule \rightarrow $(n-1)$ sides must be shorter than n th

So if you add all the sides except 1, the last side measure should be less than the sum of all previous sides

$$S_1 + S_2 + S_3 + S_4 + \dots > S_{n-1}$$



180

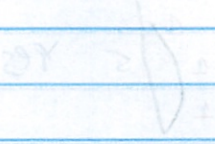
180

180

Triangle Inequality

8-9-2

All sides must be more than 0

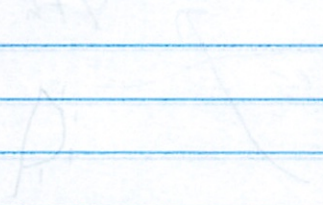


$a + b > c$

$a + c > b$

$b + c > a$

All sides must be more than 0



$a + b > c$

$a + c > b$

All sides must be more than 0

$a + b > c$

Sum of angles in a triangle is 180

Sum of angles in a quadrilateral is 360

Sum of angles in a pentagon is 540

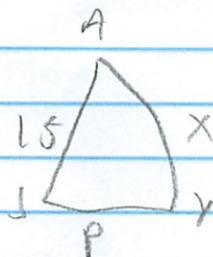
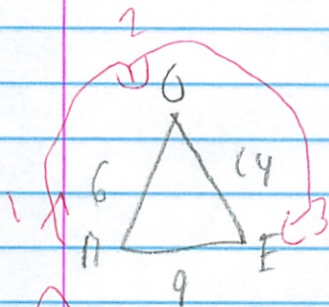
Sum of angles in a hexagon is 720

Inventing Rules #13

$$\frac{6}{15} = \frac{14}{x} = \frac{9}{p}$$

$$\frac{MO}{JA} = \frac{OE}{AY} = \frac{EM}{YS}$$

$$\frac{6}{15} = \frac{14}{x} \quad \text{cross up products}$$



$$\frac{220}{6} = \frac{6x}{6} \quad \text{Equation}$$

$$35 = x \quad \text{solup}$$

$\triangle MOE \sim \triangle JAY$

Keep in order of name

$$\frac{6}{15} = \frac{9}{p} \quad 45 = \frac{2p}{2}$$

$$\frac{2}{5} = \frac{9}{p} \quad 22\frac{1}{2} = p$$

#1 $\frac{x}{5} = 7$

Do $7 \times 5 = 35$

$$\frac{35}{5} = 7$$

#2 $\frac{x}{6} = \frac{72}{24}$

$$\frac{x}{6} = \frac{3}{1}$$

$$\frac{18}{6} = \frac{72}{24}$$

#3 $\frac{x}{8} = \frac{11}{4}$

$$\frac{88}{4} = \frac{4x}{4}$$

$$\frac{22}{8} = \frac{11}{4}$$

#4 $\frac{x}{7} = \frac{5}{3}$

$$\frac{35}{3} = \frac{3x}{3}$$

$$\frac{11\frac{2}{3}}{7} = \frac{5}{3}$$

#5 $\frac{x+1}{3} = \frac{4}{6} = \frac{2}{3}$

similar

$$\frac{1+1}{3} = \frac{4}{6}$$

or $6(x+1) = 3 \times 4$

$$6x + 6 = 12$$

$$\frac{6x}{6} = \frac{6}{6}$$

$$x = 1$$

#6 $\frac{5}{13} = \frac{19}{x}$

$$\frac{247}{5} = \frac{5x}{5}$$

$$49.4 = x$$

$$\frac{5}{13} = \frac{19}{49.4}$$

#7 $\frac{2}{x} = 6$

$$6 \times 2 = 12$$

$$\frac{2}{12} = 6$$

still cross

$$x \times x = 4 \times 16$$

$$x^2 = 144$$

$$\sqrt{x} = \sqrt{12} \quad \text{or} \quad x = -12$$

#8 $\frac{9}{x} = \frac{x}{16}$

can have multiple ans

$$\frac{9}{18} = \frac{8}{16}$$

x must be same

$$\frac{9}{12} = \frac{12}{16}$$

Michael Placencia

All correct 100%

1. A pole that is 10 feet high casts a 6 foot shadow.

a. How long a shadow will a 40 foot high pole cast?

$\frac{\text{pole}}{\text{shadow}} = \frac{10}{6} = \frac{40}{x}$ $x = 24$

b. If a pole has a 15 foot shadow, how high is the pole?

$\frac{10}{6} = \frac{x}{15}$ $x = 9$
 ~~$\frac{10}{6} = \frac{x}{15}$ $x = 25$~~

2. A 10 foot tall tree casts a 6 foot shadow.

a. Another tree casts a 15 foot shadow. How tall is it?

$\frac{10}{6} = \frac{x}{15}$ $6x = 150$ $x = 25$

c. How long a shadow will a 32 foot tall tree cast?

$\frac{10}{6} = \frac{32}{x}$ $10x = 192$ $x = 19.2$

3. A map is scaled so that 1 inch on the map is equal to 2 miles.

a. How many inches on the map is a 12 mile distance?

$\frac{1 \text{ in}}{2 \text{ mi}} = \frac{x}{12}$ $x = 6$

b. What distance is represented by 17 inches on the map?

$\frac{1}{2} = \frac{17}{x}$ $x = 34$

4. A map is scaled so that 2 inches on the map is equal to 3 miles.

a. How many inches on the map is a 12 mile distance?

$\frac{2}{3} = \frac{x}{12}$ $24 = 3x$ $x = 8$

b. What distance is represented by 30 inches on the map?

45 miles

c. What distance is represented by 17 inches on the map?

25.5 miles

5. A map is scaled so that 5 inches on the map is equal to 8 miles.

a. How many inches on the map is a 12 mile distance?

$\frac{5}{8} = \frac{x}{12}$ $60 = 8x$ $x = 7.5$

b. How many inches on the map is a 30 mile distance?

18.75 inches

c. What distance is represented by 8 inches on the map?

12.8 miles

d. What distance is represented by 17 inches on the map?

27.2 miles

6. A 13 foot tall tree casts a 5 foot shadow.

a. Another tree casts a 12 foot shadow. How tall is it?

$\frac{5}{8} = \frac{x}{12}$ $64 = 8x$ $x = 8$

b. How long a shadow will a 32 foot tall tree cast?

31.2 feet

$\frac{5}{8} = \frac{32}{x}$ $5x = 136$ $x = 27.2$

tree shadow $\frac{13}{5} = \frac{x}{12}$ $5x = 156$ $x = 31.2$
 $\frac{13}{5} = \frac{32}{x}$ $13x = 160$ $x = 12\frac{4}{13}$
 Shadows 1

$\frac{x}{x-1} = \frac{3}{4}$ $4x = 3(x-1)$ $\frac{2x}{x+1} = \frac{3}{2}$ $3(x+1) = 2x(2)$
 $4x = 3x - 3$ $4x = 3x - 3$ $2x = 3$ $3x + 3 = 4x$
 $-3x \quad -3x$ $-3x \quad -3x$ $3x = x$ $3x + 3 = 4x - 3x$
 $x = -3$ $3 = x$

Find the value of x.

1. $\frac{9}{x} = \frac{3}{4}$ $\frac{3x}{3} = \frac{36}{3}$
 $x = 12$

9. $\frac{8}{3} = \frac{5x}{6}$ $3(5x) = 48$
 $15x = 48$ $15x$
 $\frac{3x}{3} = \frac{32}{3}$
 $x = 11 \frac{1}{3}$

2. $\frac{x}{2} = \frac{3}{5}$ $\frac{5x}{5} = \frac{6}{5}$
 $x = 1.2$ $1 \frac{1}{5}$ use fractions!

10. $\frac{5}{3} = \frac{x-1}{-2}$ $3(x-1) = -10$
 $3x - 3 = -10$
 $+3 \quad +3$
 $3x = -7$
 $\frac{3x}{3} = \frac{-7}{3}$
 $x = -2 \frac{1}{3}$

3. $\frac{3}{2} = \frac{x}{6}$ $\frac{2x}{2} = \frac{18}{2}$
 $x = 9$

11. $\frac{3x+1}{6} = \frac{2}{3}$ $3(3x+1) = 12$
 $9x + 3 = 12$
 $-3 \quad -3$
 $9x = 9$
 $\frac{9x}{9} = \frac{9}{9}$
 $x = 1$

4. $\frac{3}{2} = \frac{x+1}{8}$ $2(x+1) = 24$
 $2x + 2 = 24$
 $-2 \quad -2$
 $2x = 22$
 $\frac{2x}{2} = \frac{22}{2}$
 $x = 11$

12. $\frac{3x}{2} = \frac{5}{6}$ $6(3x) = 16$
 $18x = 16$
 $\frac{18x}{18} = \frac{16}{18}$
 $x = \frac{8}{9}$

5. $\frac{x}{-2} = \frac{3}{4}$ $\frac{4x}{4} = \frac{-6}{4}$
 $x = -1.5$ $-1 \frac{1}{2}$

13. $\frac{18}{4x-3} = \frac{1}{2}$ $4x - 3 = 36$
 $4x = 39$
 $\frac{4x}{4} = \frac{39}{4}$
 $x = 9.75$ $9 \frac{3}{4}$

6. $\frac{6}{-5} = \frac{x}{6}$ $\frac{-5x}{-5} = \frac{-36}{-5}$
 $-x = -7.2$ $x = 7.2$ x is negative

14. $\frac{x}{2} = \frac{4}{3}$ $\frac{3x}{3} = \frac{8}{3}$
 $x = 2 \frac{2}{3}$

7. $\frac{x+3}{6} = \frac{2}{3}$ $3(x+3) = 12$
 $3x + 9 = 12$
 $-9 \quad -9$
 $3x = 3$
 $\frac{3x}{3} = \frac{3}{3}$
 $x = 1$

15. $\frac{3}{5} = \frac{2}{4x+1}$ $3(4x+1) = 10$
 $12x + 3 = 10$
 $-3 \quad -3$
 $12x = 7$
 $\frac{12x}{12} = \frac{7}{12}$
 $x = \frac{7}{12}$ see it's there

8. $\frac{4}{5} = \frac{7}{2x+1}$ $4(2x+1) = 35$
 $8x + 4 = 35$
 $-4 \quad -4$
 $8x = 31$
 $\frac{8x}{8} = \frac{31}{8}$
 $x = 3 \frac{7}{8}$

16. $\frac{-3}{4} = \frac{x}{-8}$ $4x = 24$
 $\frac{4x}{4} = \frac{24}{4}$
 $x = 6$

Michael Plasmeier

Properties of Proportions - Worksheet

Find the value of the given variable:

1. $\frac{x}{8} = \frac{12}{18}$
 $\frac{18x}{18} = \frac{96}{18}$
 $18 : 5\frac{1}{3}$
 $x = 5\frac{1}{3}$

6. $\frac{1}{2} = \frac{z}{25}$
 $\frac{22}{2} = \frac{25}{2}$
 $2 = 12.5$ $12\frac{1}{2}$

2. $\frac{x}{12} = \frac{60}{45}$
 $\frac{45x}{45} = \frac{720}{45}$
 $x = 16$

7. $\frac{3x}{21} = \frac{5}{3}$
 $3 \times (3) = 105$ *would be 9x*
 $9x = 105$ ~~distributed~~
 $x = 11\frac{2}{3}$ *proportion*

3. $\frac{c}{6} = \frac{12}{15}$
 $\frac{15c}{15} = \frac{72}{15}$
 $c = 4.8$

8. $\frac{x}{9} = \frac{16}{x}$
 $x(x) = 144$
 $x^2 = 144$
 $x = 12$ or -12 *can also be*

4. $\frac{q}{56} = \frac{15}{14}$
 $\frac{14q}{14} = \frac{840}{14}$
 $q = 60$

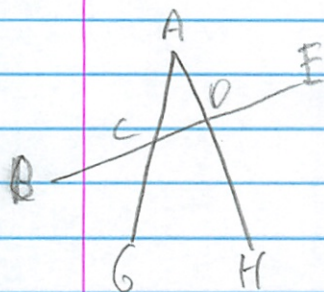
9. $\frac{9}{12} = \frac{x-1}{4}$
 $12(x-1) = 36$
 $12x - 12 = 36$
 $12x = 48$
 $x = 4$
Correct distributive

5. $\frac{8}{d} = \frac{40}{30}$
 $\frac{40d}{40} = \frac{240}{40}$
 $d = 6$

10. $\frac{x}{6} = \frac{1}{2}$
 $\frac{6}{2} = \frac{2x}{2}$
 $3 = x$

$12(x-1) = 12x - 12$
do but not
 $3 \times (3) = 9x$

What's the angle? (#14)



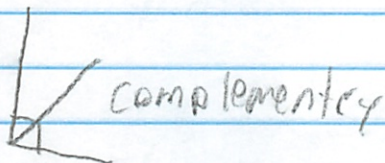
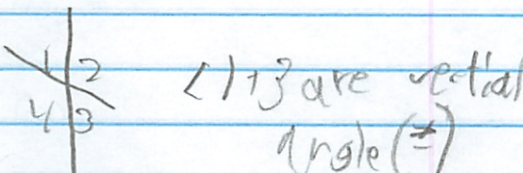
1. What's =
What's sum relations
2. Other diagrams for that
3. Generalize

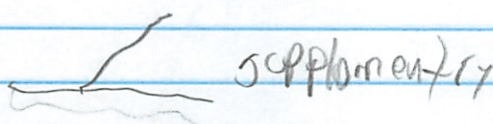
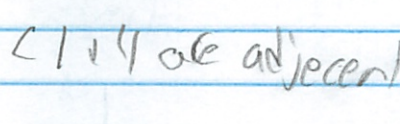
1. Angles BCG and BCA are supplementary (add to 180°)
Angles BCG, BCA, ACD, and GCD ~~add to~~ 360°
Angles ACD and GCD are also supplementary (add to 180°)

Angle GCH and ACB are adjacent

Angles ACD make a triangle

Angles ACB and GCD are vertical and = m

2.  

3. Vertical angles are = (opposite)

Other: An angle that is divided by angles adds to 180° (supplementary)
A right angle (90°) cut by a line, still adds to 90° (complementary)

If you know 1 angle the supplement can be measured as $(180 - m)$
If you know 1 angle here, you can easily figure the rest of the measuring

Notes 4/12

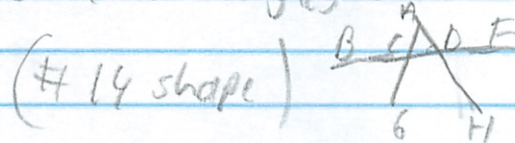
about #14

2 angles are called supplementary angles if the sum of the measures of the angles is 180°

2 angles are called complementary angles if the sum of the measures of the angles is 90°

A straight angle is an angle w/ the measure of 180°

Vertical angles are formed w/ the intersection of 2 angles



$\angle ACD + \angle BCG$ are vertical angles

Vertical angles are always =

Angles that are supplements of the same angle must be =

Formal Proof

Given: $\angle 1$ and $\angle 8$ are supplementary
 $\angle 1$ and $\angle 3$ " " " "

problem

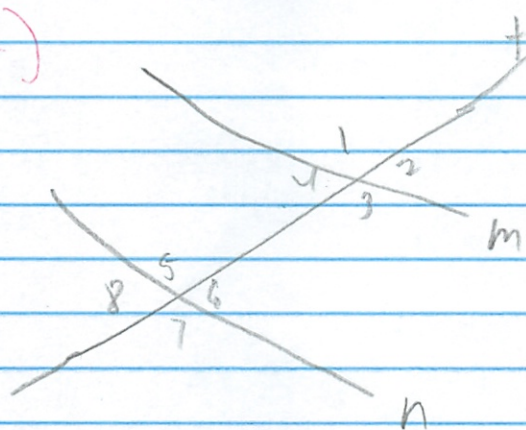
~~1/3~~
~~8~~

Prove: $\angle 3 \cong \angle 8$

Statement	Reason	Statement cont.	Reason cont.
$\angle 1$ and $\angle 3$ are supplementary	Given	$m\angle 1 + m\angle 3 = 180^\circ$	Definition of supplementary
$\angle 1$ and $\angle 8$ are supplementary	Given	$m\angle 8 = 180^\circ - m\angle 1$	Subtracted $m\angle 1$ from both sides
$m\angle 1$ and $m\angle 8 = 180^\circ$	Definition of supplementary	$m\angle 3 = 180^\circ - m\angle 1$	Subtracted $m\angle 1$ from both sides
		$m\angle 3 = m\angle 8$	transitive property (if $a=b$, and $b=c$ then $a=c$)

Notes, 4/11

Transversal
 corresponding angles
 alternate interior angles



When a transversal cuts across parallel lines, the corresponding angles are \cong (2 and 6)

When a transversal cuts across parallel lines, the alternate interior angles are \cong . (4 and 6)

alternate exterior angles (1 and 7) 2 and 7 are same side exterior

Proof
 See above

Statement	Reason
$G: m \parallel n$ $P: \angle 2 \cong \angle 8$	Given
$m \parallel n$	vertical angles are \cong
$\angle 2 \cong \angle 4$	Corresponding angles are \cong
$\angle 4 \cong \angle 8$	transitive property
$\angle 2 \cong \angle 8$	

p 446

4/10

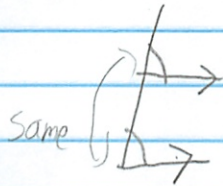
Angles BCA & HCD are vertical \cong

Angles HFG & HCD correspond \cong

Angles ACD and EFG are complementary (add to 180)

When angles are oppset, they are vertical and \cong

Corresponding lines cut by transversal are =
angles on



2 angles next to each other (adjacent) add to 180°
are called complementary

Angle BCF and CFG are Oppset Interior angles
and are also \cong

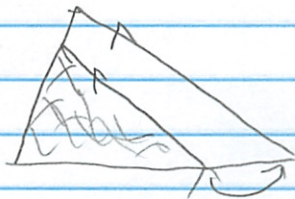
Inside Similarity #15

4/19

If you notice that the dotted line of the small triangle is parallel to the 3rd side of the triangle (that doesn't touch smaller triangle.)

The simple solution to fix this is to make the dotted line parallel to the 3rd line of the triangle.

This happens because the lines must be parallel for the ~~triangle~~ angles to be $=$ and therefore for the triangle to be similar



lines must be parallel

More Proofs

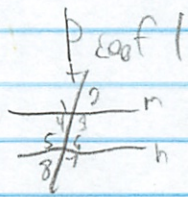
We can use 2 facts (Corresponding angles are \cong and alternate interior \angle 's are \cong) to use reasons to prove other things when we have parallel lines

Trans
if $a=b$ and $b=c$, then $a=c$

Substitution

$$m\angle 11 \cong m\angle 12 = 180^\circ \quad m\angle 11 \cong m\angle 81 = 180^\circ$$

$$m\angle 12 = m\angle 81 \quad \leftarrow$$



Given: $m \parallel n$
Prove: $\angle 3$ and $\angle 6$ are supplementary

Given: $m \parallel n$
Prove: $\angle 1 \cong \angle 7$

Statement	Reason	S	R
m and n are parallel	Given	$m \parallel n$	Given
$\angle 3$ and $\angle 7$ are \cong	Corresponding \angle 's are \cong	$\angle 1 \cong \angle 3$	vertical angles are \cong
$\angle 2$ and $\angle 6$ are \cong	Corresponding \angle 's are \cong	$\angle 3 \cong \angle 7$	Corresponding \angle 's are \cong
$\angle 2$ and $\angle 3$ are <u>supplementary</u> measures add to 180°	Supplementary angles	$\angle 1 \cong \angle 7$	transitive property
$\angle 6$ and $\angle 7$ are <u>supplementary</u> measures add to 180°	Supplementary angles		
If $180 - \angle 2 = \angle 3$ and $\angle 3$ and $\angle 7$ are \cong then $\angle 7 = 180 - \angle 2$	transitive property called this!	$\angle 2 + \angle 3 = 180$ $\angle 3 = 180 - \angle 2$	Defn of Supp Subtr property

2 adjacent w/ exterior sides (rays) forming a line

Simple way

Answers

$m \parallel n$ | Given
 $\angle 3$ and $\angle 4$ supplementary | 2 adjacent angles w/ exterior sides (rays) form a line
 $\angle 4 \cong \angle 6$ | Alternate interior angles are \cong
 $\angle 3$ and $\angle 6$ are supplementary | Substitution

Proportions #16

4/21

#1 $\frac{24}{20} = \frac{18}{15}$

$\frac{12}{24} = \frac{9}{18}$ (1)

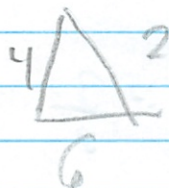
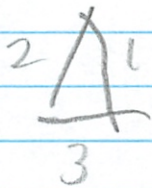
$\frac{12}{20} = \frac{9}{15}$

This is true that comparing 2 angles or 1 triangle to the same 2 sides of another

Given $\frac{20}{12} = \frac{18}{9}$

$\frac{20}{24} = \frac{15}{12}$

#2



$\frac{2}{3} = \frac{4}{6}$

$\frac{1}{2} = \frac{2}{4}$

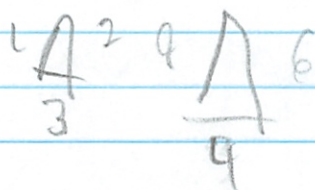
$\frac{2}{1} = \frac{4}{2}$

$\frac{1}{3} = \frac{2}{6}$

Yes again, it is true.

$\frac{3}{2} = \frac{6}{3}$

3.



That statement is no longer true

Actually, statement is true, it only works for similar triangles

$\frac{1}{3} \neq \frac{9}{6}$ Doesn't work

$\frac{2}{3} \neq \frac{6}{4}$

Over →

4a

$$2^x \Delta_{6=1}^{4=5}$$

old way

$$\frac{2}{1} = \frac{6}{3} = \frac{4}{2}$$

$$1 = x \Delta_{3=2}^{2=4}$$

b.

$$\frac{2}{6} = \frac{1}{3}$$

$$\frac{4}{6} = \frac{2}{3}$$

$$\frac{6}{2} = \frac{3}{1}$$

$$\frac{2}{4} = \frac{1}{2}$$

$$\frac{4}{2} = \frac{2}{1}$$

$$\frac{6}{4} = \frac{3}{2}$$

IMP 1 SHADOWS
QUIZ #1

NAME: Michael Masner's 8848

DATE: 4/20

SOLVE EACH OF THE FOLLOWING - SHOW ALL WORK SHOW YOUR CHECK!!
CIRCLE YOUR FINAL ANSWER

1. $\frac{X}{10} = \frac{3}{5}$
 $\frac{30}{5} = \frac{5x}{5}$
 $6 = x$

2. $\frac{2}{X} = \frac{4}{11}$

$\frac{4x}{4} = \frac{22}{4}$

$x = 5.5$

$\frac{19\frac{1}{2}}{20}$

3. $\frac{3}{8} = \frac{X}{100}$

$\frac{8x}{8} = \frac{300}{8}$

$x = 37.5$

4. $\frac{4X}{24} = \frac{5}{3}$

$3(4x) = 120$

$\frac{12x}{12} = \frac{120}{12}$

$x = 10$

5. $\frac{12}{X+1} = \frac{6}{8}$

$6(x+1) = 96$

$6x + 6 = 96$

$\frac{6x}{6} = \frac{90}{6}$

$x = 15$

6. $\frac{6}{X+1} = \frac{3}{4}$

$24 = 3(x+1)$

$24 = 3x + 3$

$\frac{21}{3} = \frac{3x}{3}$

$x = 7$

7. $\frac{X}{6} = \frac{30}{24}$

$\frac{180}{24} = \frac{24x}{24}$

$7\frac{1}{2} = x$

8. $\frac{1}{2} = \frac{X}{32}$

$\frac{32}{2} = \frac{2x}{2}$

$16 = x$

9. $\frac{X}{8} = \frac{2}{X}$

$x(x) = 16$

$\sqrt{x^2} = \sqrt{16}$

$x = \pm 4$

10. $\frac{5}{X} = \frac{4}{3}$

$\frac{4x}{4} = \frac{15}{4}$

$x = 3.75$

~~Don't!~~

66%

$\frac{4}{12}$ wrong

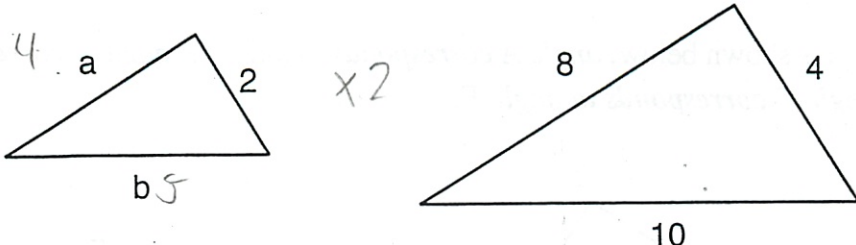
In each of the pairs of figures shown below, assume that the figures are similar. Then

a. Write the proportion relating the sides of the figures.

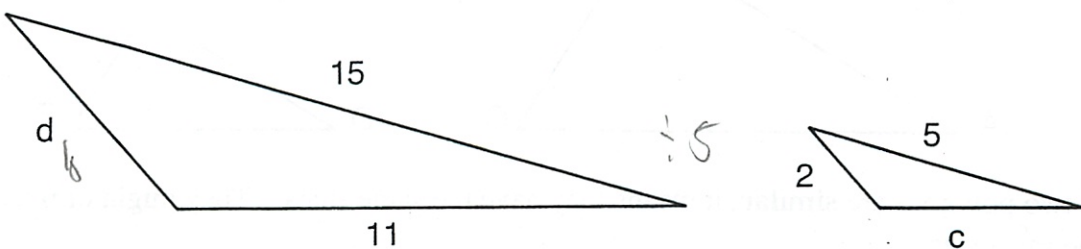
b. Solve the proportions to find the missing lengths.

say $\frac{4}{8} = \frac{5}{10}$ or $\frac{4}{5} = \frac{5}{10}$

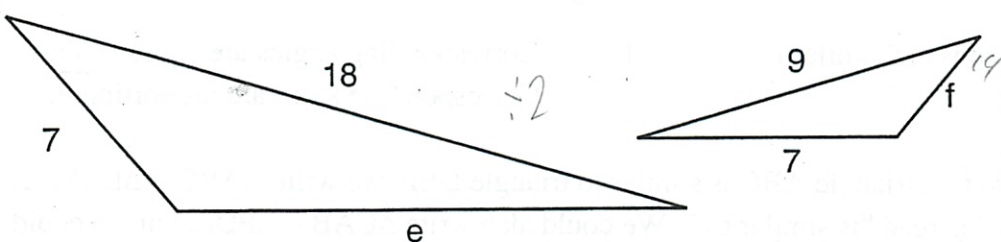
1.



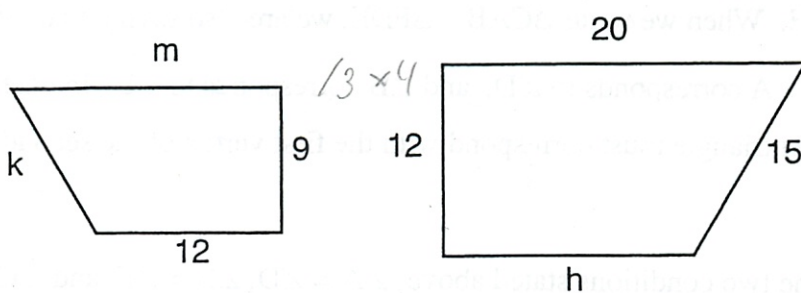
2.



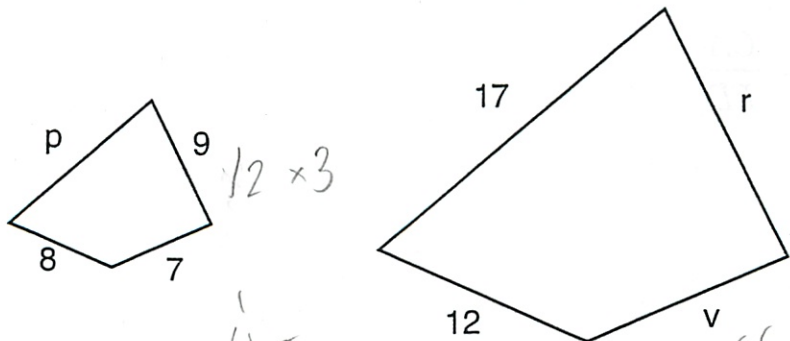
3.



4.



5.



Answers	
1. a	4
b	5
2. c	16 ^{3 2/3}
d	2.2 ⁶
3. e	14
f	14 ^{3.5}
4. h	16
k	4.25
m	15
5. p	5 ^{2/3} ^{11 1/3}
r	13.5
v	10.5

3.75
 $\sqrt{15}$
 3.75
 $\times 3$
 11.25

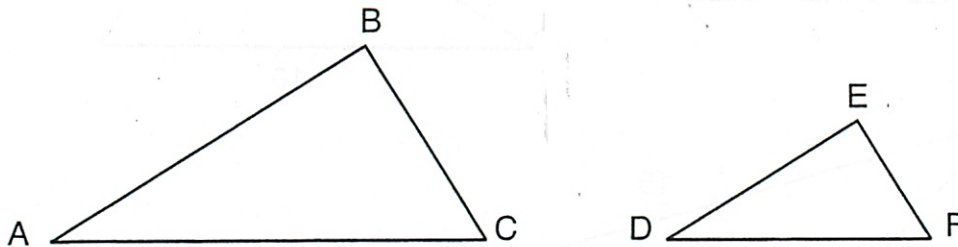
4.5
 $\times 3$
 13.5

5.666
 $\sqrt{17}$

Polygons and Similarity

A **polygon** is named by naming its **vertices** in order. For example, the polygon at the right can be called "triangle ABC" or "triangle CBA" or "triangle BCA" or "triangle ACB" or "triangle CAB" or "triangle BAC."

In the two triangles shown below, *angle A corresponds to angle D, angle B corresponds to angle E, and angle C corresponds to angle F.*



If two polygons are **similar**, it means they have the same shape. They might or might not be the same size.

Two polygons are similar if:

1. Corresponding angles are equal, and
2. Corresponding sides are proportional.

To indicate that triangle ABC is similar to triangle DEF, we write $\triangle ABC \sim \triangle DEF$. The symbol " \sim " is read "is similar to." We could also write $\triangle CAB \sim \triangle FDE$, but we could **not** write $\triangle ABC \sim \triangle FDE$. When we write $\triangle CAB \sim \triangle FDE$, we are also saying that $\angle C$

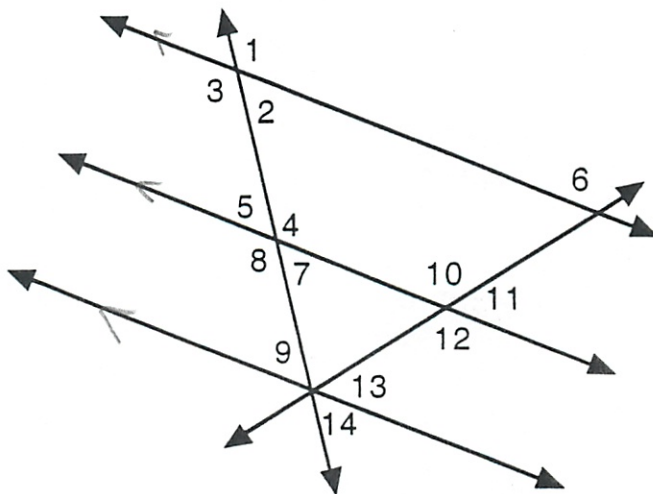
corresponds to $\angle F$, $\angle A$ corresponds to $\angle D$, and $\angle B$ corresponds to $\angle E$. In other words, the first vertex of the first triangle must correspond with the first vertex of the second triangle, and so on.

Also, according to the two conditions stated above, $\angle A = \angle D$, $\angle B = \angle E$, and $\angle C = \angle F$,

$$\text{and } \frac{AB}{DE} = \frac{BC}{EF} = \frac{CA}{FD}.$$

Michael Plasmeid

Classify each pair of angles.



- 1) Angle 1 and angle 4 Corresponding
- 2) Angle 3 and angle 4 Alternate interior Angles ???
- 3) Angle 3 and angle 8 Corresponding
- 4) Angle 5 and angle 7 vertical
- 5) Angle 2 and angle 5 alternate interior
- 6) Angle 6 and angle 10 Corresponding
- 7) Angle 12 and angle 6 alternate exterior
- 8) Angle 14 and angle 9 vertical
- 9) Angle 13 and angle 11 corresponding
- 10) Angle 9 and angle 7 alternate interior

Parallel proof

P442 + 443

4/20

G: $\overline{AB} \parallel \overline{CD}$

P: Triangles sum to 180° (angles $m\angle s$, $m\angle t$ and $m\angle r$ add to 180°)

Statement	Reason
$m\angle x$ and $m\angle s$ are \cong	Alternate interior angles are \cong
$m\angle x, m\angle r, m\angle y$ add to 180°	share a line, or are adj to one that does
$m\angle s, m\angle r, m\angle y$ add to 180°	Substitution
$m\angle y$ and $m\angle t$ are \cong	Alternate Interior angles are \cong
$m\angle s, m\angle r$ and $m\angle t$ add to 180°	substitution

say

$m\angle$
↑
measure of angle

say

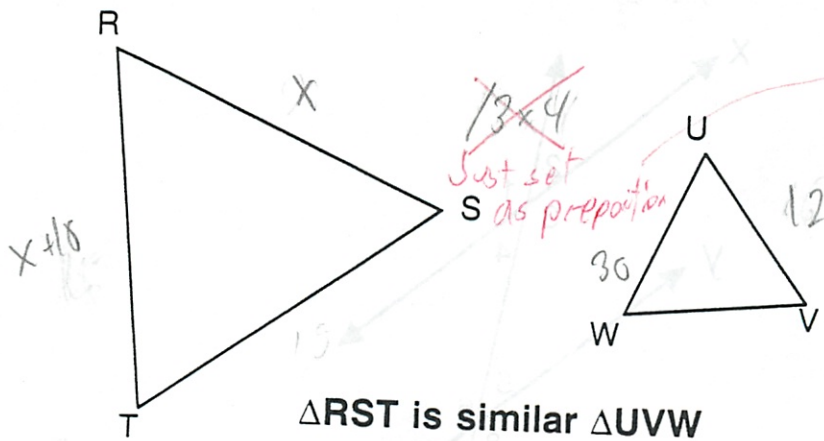
2 or more adjacent angles making a line and whose exterior rays are supplementary

classwork



Given: $\triangle CAB$
Prove: $m\angle CAR = \angle ACB + \angle ABC$

Statement	Reason
$\triangle CAB$	Given
$\angle CAR$ and $\angle CAB$ are supplementary	2 adj \angle 's w/ exterior rays form a line are supp.
$m\angle CAR + m\angle CAB = 180^\circ$	Definition* of supplementary
$m\angle ACB + m\angle BAC + m\angle CBA = 180^\circ$	The sum of the measures of a triangle is 180°
$m\angle CAR + m\angle CAB = 180^\circ$	Transitive Property
$m\angle ACB + m\angle BAC + m\angle CBA = 180^\circ$	Subtraction property
$m\angle CAR = m\angle ACB + m\angle ABC$	



$$\frac{9}{16} \cdot \frac{x}{15} = \frac{16x}{16 \cdot 15} = \frac{135}{16}$$

$$x = 8\frac{7}{16}$$

$$\frac{x+10}{30} = \frac{x}{12}$$

$$12x + 120 = 30x$$

$$-12x$$

$$120 = 18x$$

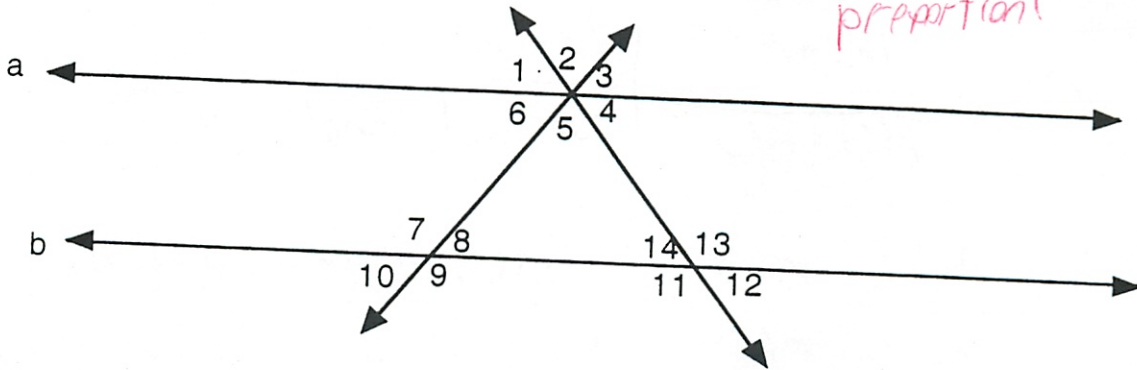
$$\frac{120}{18} = \frac{18x}{18}$$

$$6\frac{2}{3} = x$$

- $\angle R = 80^\circ$, $\angle S = 30^\circ$. Find the measure of angle W. 70
- $RS = 9$; $RT = 15$ and $UV = 16$. Find UW . $8\frac{2}{3}$
- $RS = x$; $UW = 30$; $RT = x + 10$; $UV = 12$. Find RT .

$x = 6\frac{2}{3}$ so, $16\frac{2}{3}$

Just use proportion!

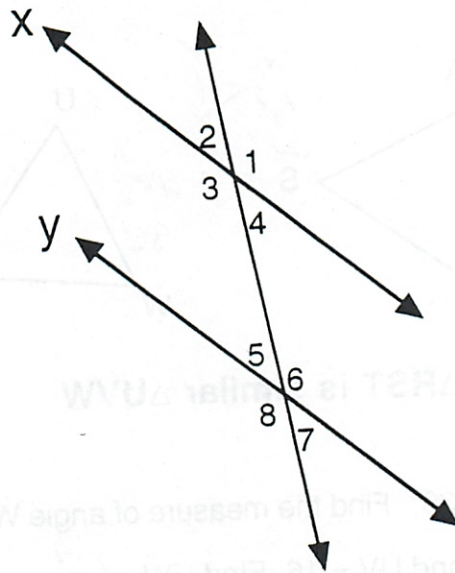


Given: $a \parallel b$

Classify the given pair of angles. Write NONE if no classification exists.

- | | |
|---|--|
| 4) angle 1 and angle 4
<i>vertical</i> | 7) angle 3 and angle 8
<i>Corresponding</i> |
| 5) angle 6 and angle 8
<i>alt. interior</i> | 8) angle 6 and angle 11
<i>w/a</i> |
| 6) angle 4 and angle 12
<i>Corresponding</i> | 9) angle 14 and angle 13
<i>supplementary</i> |

Given: $x \parallel y$



Angle 1 and angle 7 are classified as same side exterior angles.
 Prove (explain in words) that angle 1 and angle 7 are supplementary.

Forgot

S.L.A

$x \parallel y$ Given

Statement	Reason
$m\angle 1 = m\angle 3$	vertical angles are \cong
$m\angle 3 = m\angle 8$	corresponding angles are \cong
$m\angle 6 = m\angle 8$	vertical angles are equal
$m\angle 7 + m\angle 6 = 180^\circ$	share a common line (supplementary)
$m\angle 7 + m\angle 1 = 180^\circ$	Sub or Tran Property ???

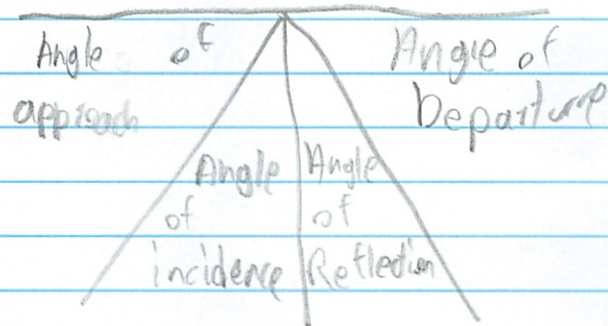
Ask

Said were 2 Trans at top, then sub at bottom

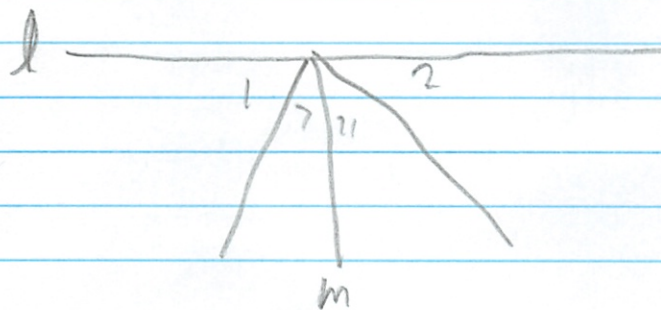
Light, Notes

Reflection

4/25



Principle of Light Reflection: When light is reflected off a surface, the angle of approach is = to the angle of departure



$$\angle 1 \cong \angle 2$$

$$l \perp m$$

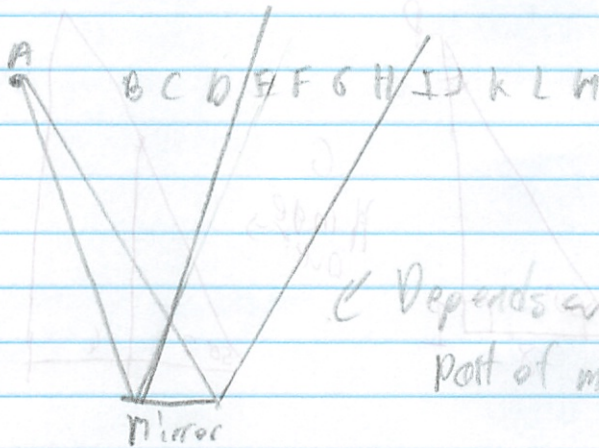
↑ perpendicular (forms a 90° angle)

$$\angle 7 \cong \angle 1$$

$\angle 1$ and $\angle 7$ are complementary

Now you see it (117)

I think A can see E, F, H

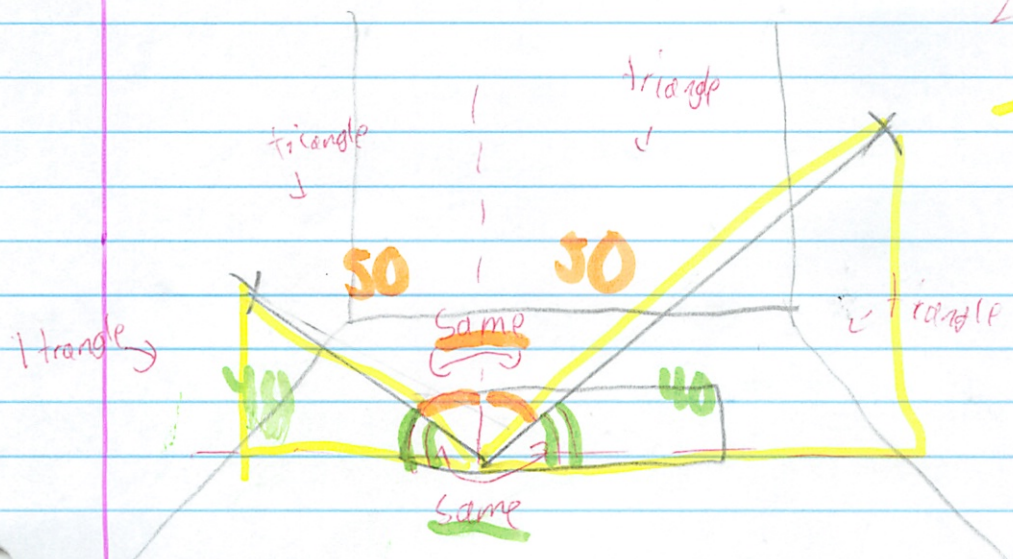


Depends what part of mirror

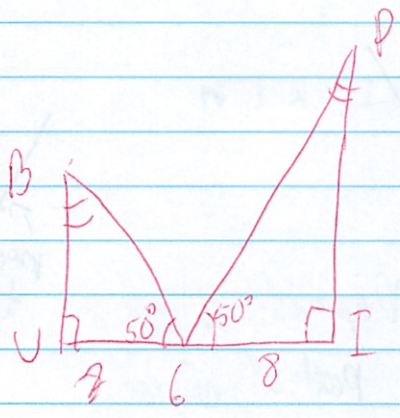
Use same thing, but other way
measure that

See principle of light reflection

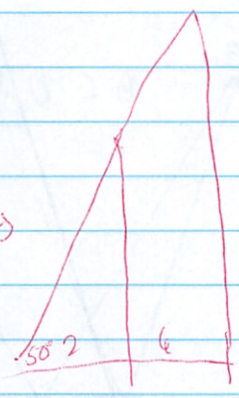
2 triangles on side =
2 in middle are =
- similar



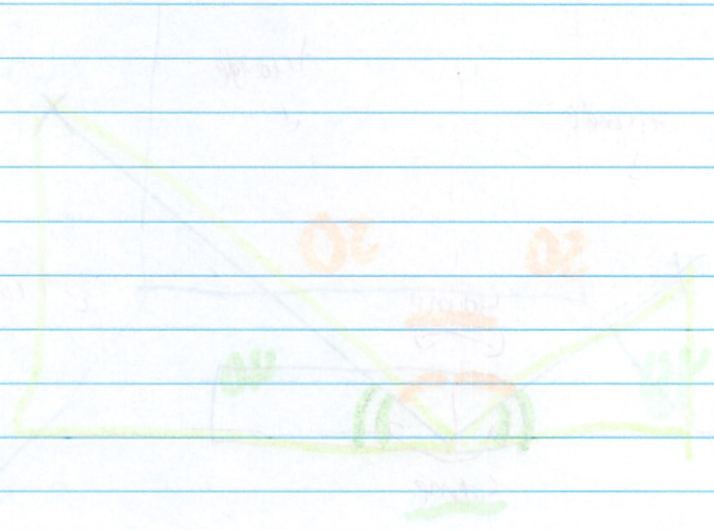
Over



G
Hinges
over \rightarrow



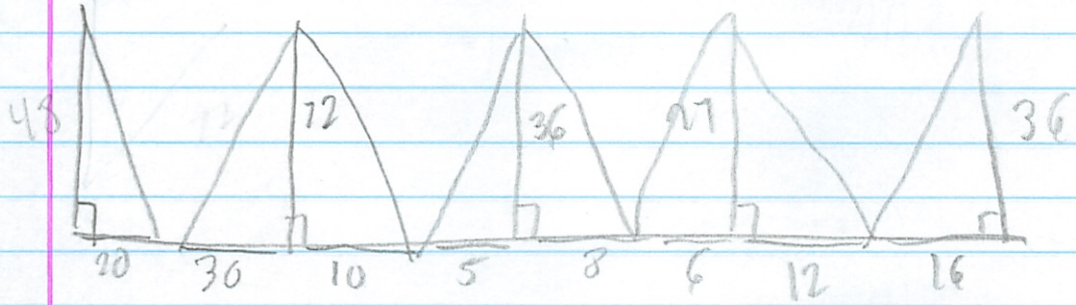
200/100



Mirror Madness (#18)

4/26

similar
(a)



5'6 Given = 48

Momma = 72 in off ground

Uncle = 36

Baby = 27

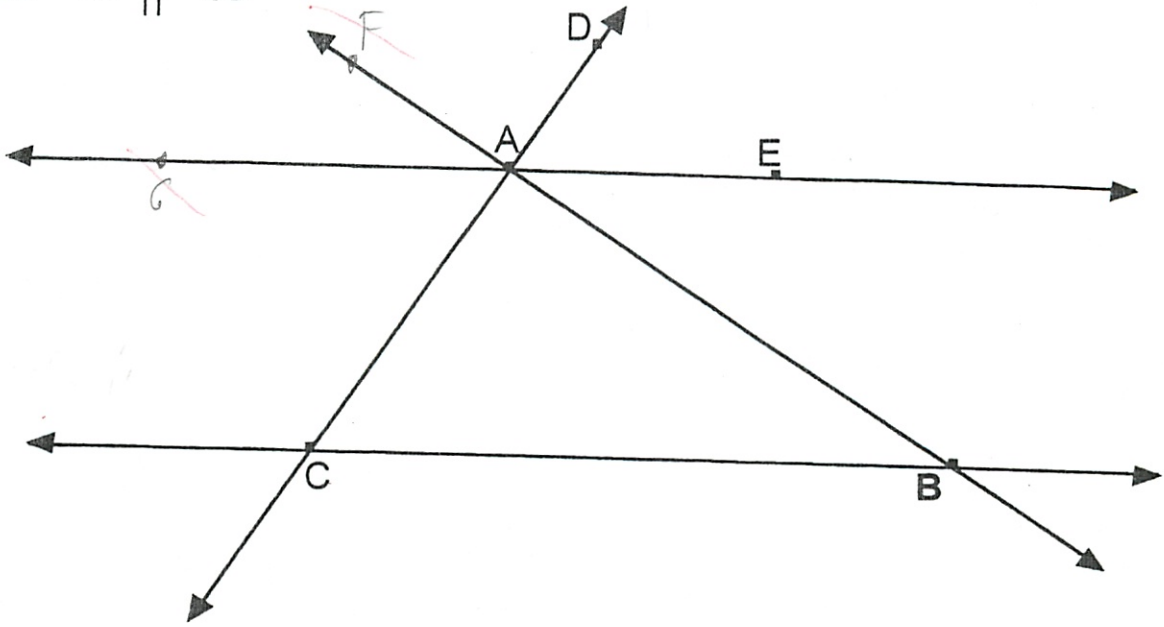
Grandad = 36

I solved it by using principles of similar triangles

$\frac{48}{20} = \frac{72}{30}$
 $\frac{36}{10} = \frac{72}{20}$
 $\frac{27}{8} = \frac{72}{30}$
 $\frac{36}{6} = \frac{72}{20}$

8/36

GIVEN: $\overleftrightarrow{AE} \parallel \overleftrightarrow{CB}$



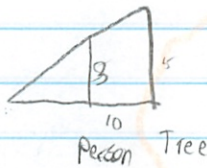
Prove (explain in words) that the sum of the measures of $\angle ACB$ and $\angle ABC$ equals the measure of $\angle DAB$.

Statement	Reason	Statement	Reason	Statement	Reason
$\overleftrightarrow{AE} \parallel \overleftrightarrow{CB}$	Given	$\overleftrightarrow{AE} \parallel \overleftrightarrow{CB}$	Given		
$\angle CAR + \angle CAB$ are suppl	2 adj w/ exterior rays are suppl.	$m\angle ACB = m\angle DAE$	Corresponding Angles =		
$m\angle BAD = 180^\circ$	Def of Suppl	$m\angle CBA = m\angle EAB$	Alternate Interior angles are =		
$m\angle ACB + m\angle CBA = 180^\circ$	Sum of measures of triangle is 180	$\angle DAE + \angle EAB = 90^\circ$	(Explain) 2 angles add to 90° supplements		<p><u>Don't know</u> w/ perpendicular lines, can't prove 90°</p> <p><u>Don't need it</u></p>
$m\angle BAD = m\angle CAB + m\angle ACB + m\angle CBA$	Trans property	$\angle ACB + \angle CBA = 90^\circ$	Substitution		
$m\angle DAB = m\angle ACB + m\angle ABC$	Sup property	$\angle DAB = 90^\circ$?? ? Prove ?		
		$\angle ACB + \angle CBA = \angle DAB$	trans		
		$\angle DAE + \angle EAB = \angle DAB$	Adj angle addition		

Measure a tree (#19)

how measure a tree

Like the shadows, If you know the distance from tree and angle from your head to the top of the tree + distance from head to tree

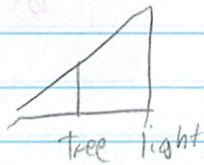


Or the entire shadow way,

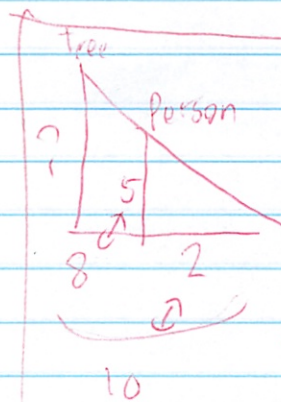
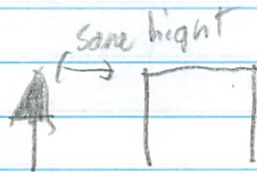
You could also throw a measure up to the top of the tree

You could use a sight

You could measure the shadow of the tree



Or you could measure a building the same height as the tree



$$\frac{5}{2} = \frac{x}{10}$$

$$50 = 2x$$

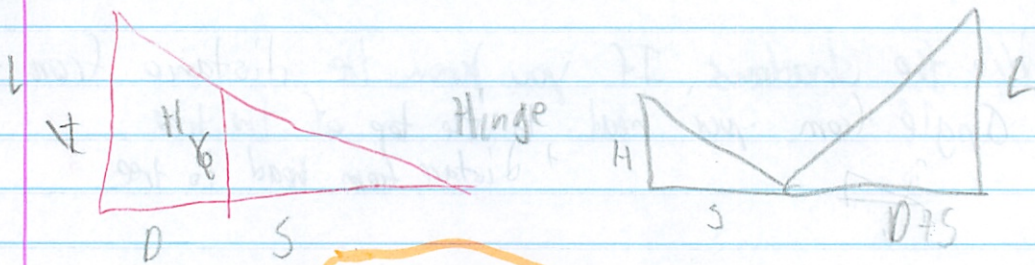
$$25 = x$$

$$x = 25$$

$$\frac{10}{2} = \frac{x}{5}$$

(cont)

Class 4/27



$$\frac{L}{H} = \frac{D+S}{S}$$

$$D+S(H) = L(S)$$

$$D(H) + S(H) = L(S)$$

try #

$$8(5) + 2(5) = 25(2)$$

$$40 + 10 = 50$$

$$4(2.5) + 5 = 25$$

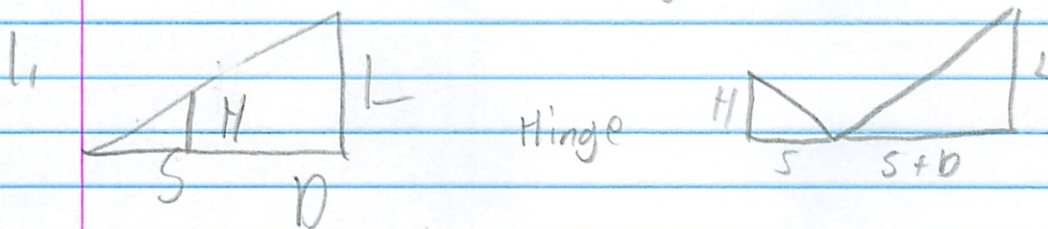
$$\frac{1}{2}(D(H)) + H = L$$

See shadow of double

Shadow of Dault

p458

4/27



2 similar triangles

$$\frac{L}{H} = \frac{D+S}{S}$$

$$3. \quad \frac{11}{5} = \frac{12+S}{5} \quad (5) \quad \frac{15}{5} = \frac{60+D}{5}$$

$$60 + 5D = 11 \cdot 5$$

$$-5D \quad -55$$

$$\frac{60}{5} = \frac{65}{5}$$

$$(10 = 5)$$

Formula

$$\frac{L}{H} = \frac{D+S}{S}$$

$$H(D+S) = L(S)$$

$$300 + 5D = 15 \cdot 5$$

$$-5D \quad -75$$

$$\frac{300}{5} = \frac{10 \cdot 5}{5}$$

$$(30 = 5)$$

$$4. \quad \frac{15}{5} = \frac{12+S}{5}$$

(*)

$$HD + HS = LS \quad \text{LS on 2 sides}$$

$$-HS \quad -HS$$

$$HD = LS - HS$$

$$HD = S(L-H)$$

$$\div (L-H) \quad \div (L-H)$$

*factoring
common of
distribution*

$$60 + 5D = 15 \cdot 5$$

$$-5D \quad -75$$

$$\frac{60}{5} = \frac{10 \cdot 5}{5}$$

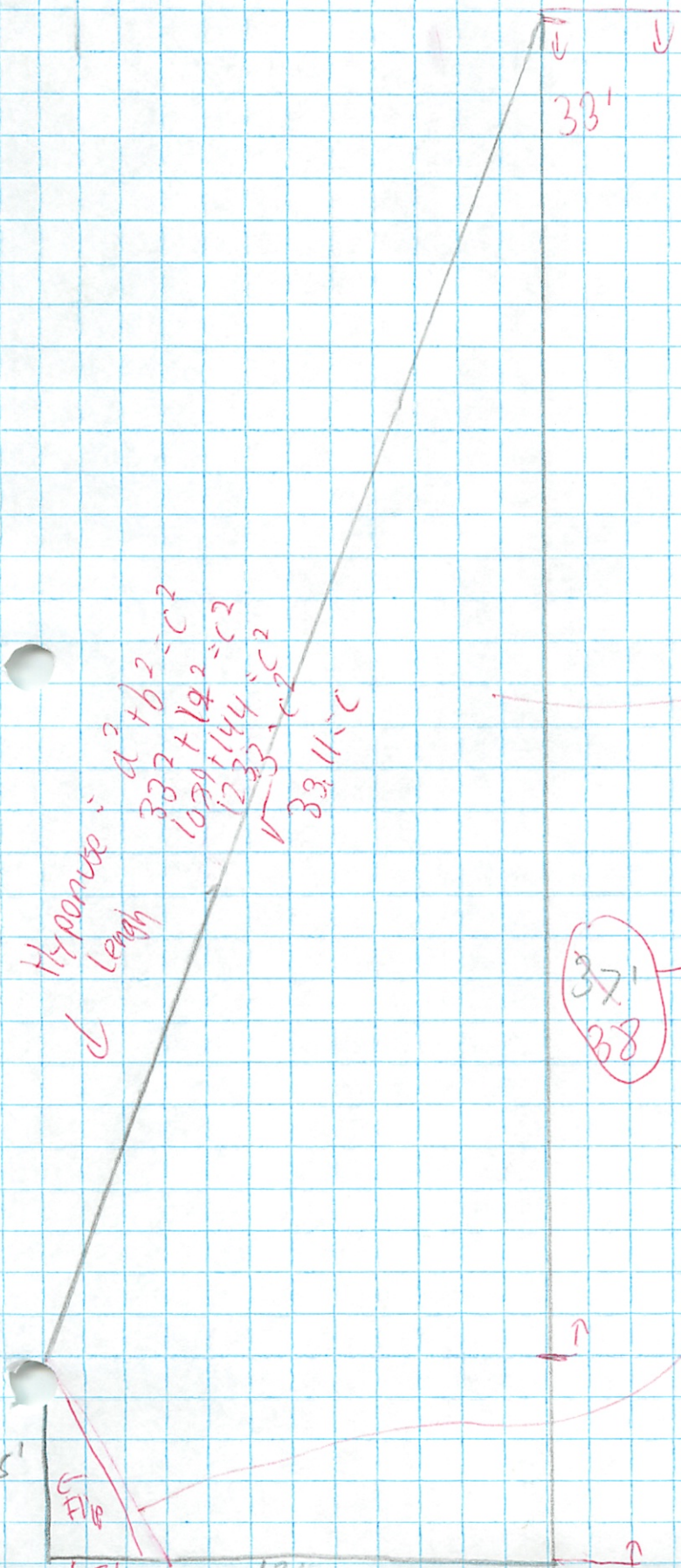
$$(5 = 6)$$

$$\frac{HD}{L-H} = S$$

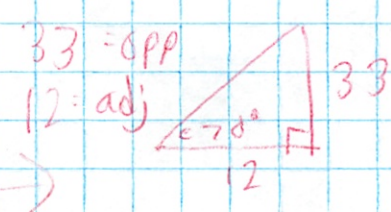
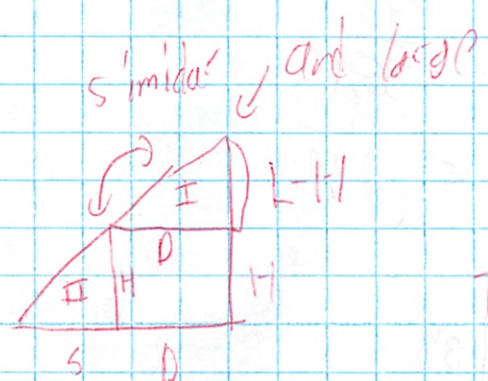
6. Multiply H by D, add quantity of that to quantity of 75 by H. This equals to LKS

1 Block = 1 Foot

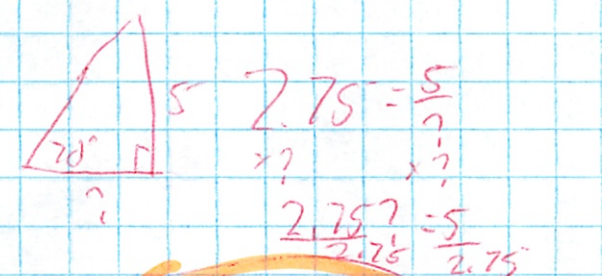
Tan



Hypotenuse: $a^2 + b^2 = c^2$
 $33^2 + 12^2 = c^2$
 $1089 + 144 = c^2$
 $1233 = c^2$
 $\sqrt{1233} = c$
 $33.11 = c$



$\tan(\theta)$
 \downarrow
 $\frac{\text{opp}}{\text{adj}} = \frac{33}{12} = 2.75$
 \downarrow



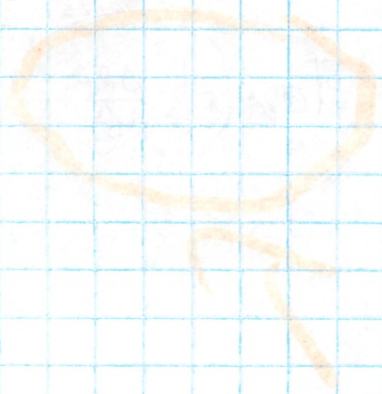
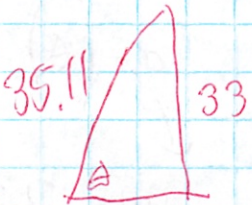
37.1
 38

$\tan(\theta) = \frac{\text{opp}}{\text{adj}}$
 $? = 1.81$

check whole triangle
 $\frac{38}{13.81} = 2.75 = \tan(70)$

Sin

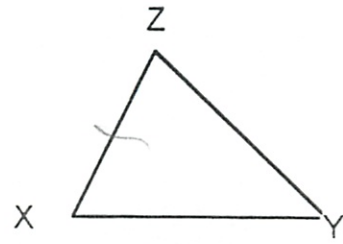
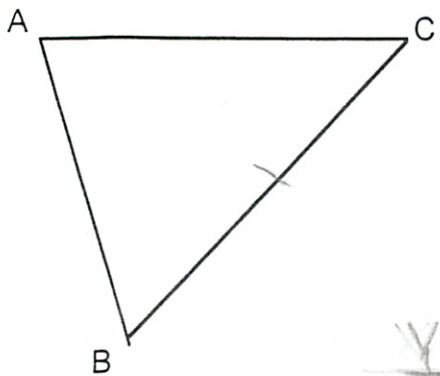
$$\begin{aligned}\sin \theta &= \frac{\text{opp}}{\text{hyp}} \\ &= \frac{33}{35.11} \\ &= 0.939\end{aligned}$$



Name Michael Plasmie 8848
 Date 4/29

Shadows Quiz 2
 50 points

50
 50
 5



$$\frac{YZ}{AB} = \frac{ZX}{BC} = \frac{XY}{CA}$$

Triangle ABC is similar to Triangle YZX

Very important

Use order

1) $\angle A = 70^\circ$ and $\angle B = 50^\circ$, find $\angle X$.
 {3 points}

$$180 - 50 - 70 = 60^\circ$$

2) $AB = 6$, $AC = 9$, and $YZ = 10$. Find XY .
 {3 points}

$$\frac{10}{6} = \frac{x}{9} \quad \frac{90 = 6x}{6} \quad x = 15$$

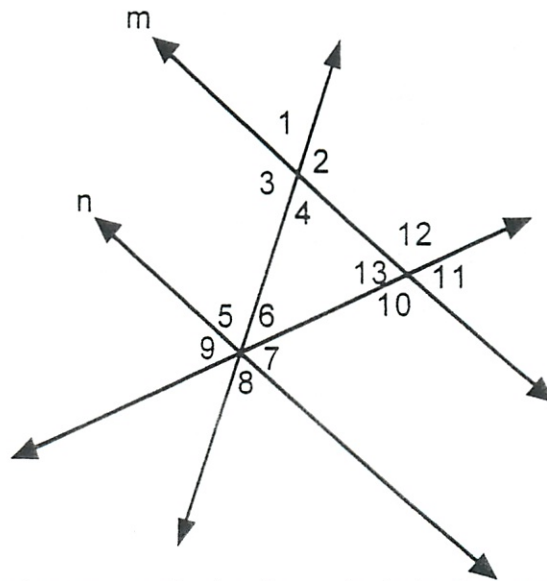
3) $AB = x$, $XY = 20$, $AC = x + 15$, $YZ = 5$. Find AC .
 {3 points}

$$\frac{5}{x} = \frac{20}{x+15} \quad 20x = 5x + 175 \quad 15x = 175 \quad x = 11\frac{2}{3} \quad \rightarrow 20 = AC$$

4) $CB = 6$, $AC = 8$, and $YX = 15$. Find ZX .
 {3 points}

$$\frac{x}{6} = \frac{15}{8} \quad 8x = 90 \quad 2x = 11\frac{1}{4}$$

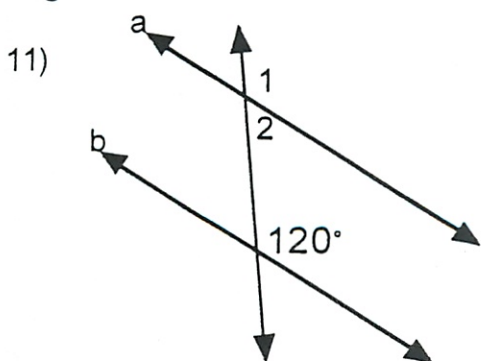
Given: $m \parallel n$



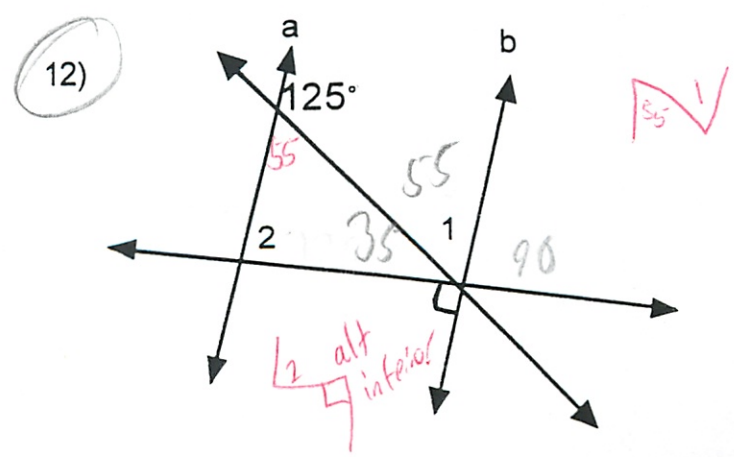
Classify each pair of angles as **vertical**, **alternate interior**, or **corresponding**.
(3 points each)

- 5) $\angle 1$ and $\angle 4$ vertical
- 6) $\angle 11$ and $\angle 7$ corresponding
- 7) $\angle 3$ and $\angle 2$ vertical
- 8) $\angle 1$ and $\angle 5$ corresponding
- 9) $\angle 4$ and $\angle 5$ alt. interior
- 10) $\angle 13$ and $\angle 7$ alt. interior

In each of the following, line a is parallel to line b. Find the measure of angle 1 and angle 2. (6 points each)

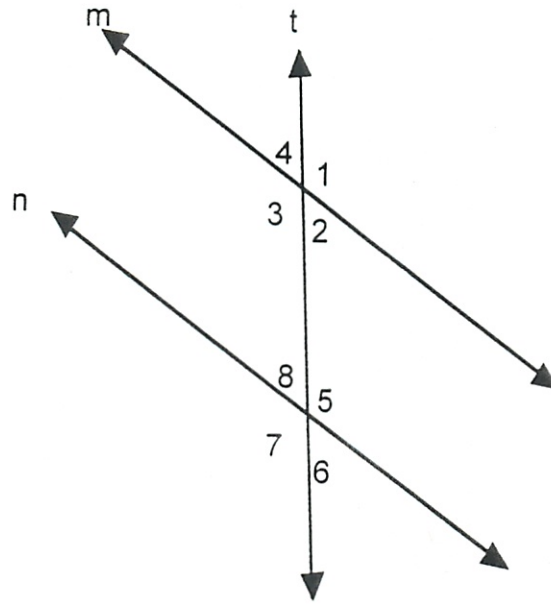


Angle 1 = 120° Angle 2 = 60°



Angle 1 = 55 Angle 2 = 90

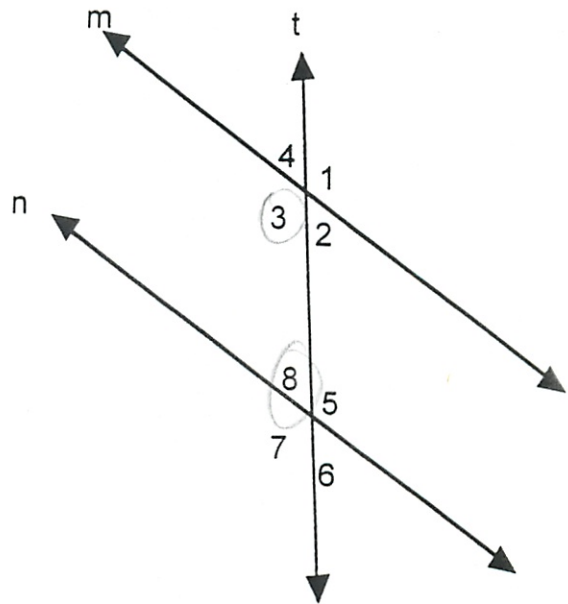
Given: $m \parallel n$



- 13) Angle 1 and angle 7 are classified as alternate exterior angles.
 Prove (explain in words) that angle 1 has the same measure as angle 7.
 {4 points}

Statement	Reason
$m \parallel n$	Given
$m\angle 1 = m\angle 3$	Vertical angles are =
$m\angle 3 = m\angle 7$	Corresponding angles are =
$m\angle 1 = m\angle 7$	Transitive property

Given: $m \parallel n$



If $A=B$ and $B=C$ then $A=C$	If $A=B$ and $B+C=U$ then $A+C=U$
<u>Transitive Property</u>	<u>Substitution</u>

14) Angle 3 and angle 8 are classified as same side interior angles. Prove (explain in words) that angle 3 and angle 8 are supplementary. {4 points}

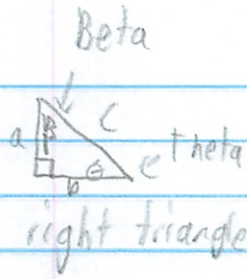
Don't Need

Statement	Reason
$m \parallel n$	Given
$m \angle 3 + m \angle 4 = 180^\circ$	Share a ray that makes a line
$m \angle 3$ and $m \angle 8$ are suppl	if 2 adj. angles have ext. sides forming a line they are suppl.
$m \angle 7 + m \angle 8 = 180^\circ$	Share a ray that makes a line
$m \angle 3 = m \angle 7$	Corresponding Angles are
$m \angle 4 = m \angle 8$	Corresponding Angles are =
$m \angle 3 + m \angle 8 = 180^\circ$	Substitution

Pythagorean Theorem + Tan + Sin + Cos

Pythagorean
Theorem

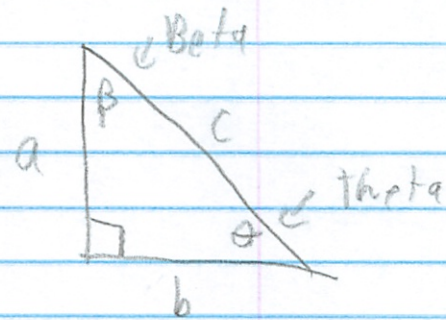
$c^2 = a^2 + b^2$ is used only in right triangles
can also use to see if 3 #'s make a right triangle



* $\tan(\angle) = \frac{\text{OPP}}{\text{adj}}$
any angle

$\tan(\theta) = \frac{\text{OPP}}{\text{adj}} = \frac{a}{b}$

$\tan(\beta) = \frac{\text{OPP}}{\text{adj}} = \frac{b}{a}$



* $\sin(\angle) = \frac{\text{OPP}}{\text{hyp}}$

$\sin(\theta) = \frac{\text{OPP}}{\text{hyp}} = \frac{a}{c}$

$\sin(\beta) = \frac{\text{OPP}}{\text{hyp}} = \frac{b}{c}$

* $\cos(\angle) = \frac{\text{adj}}{\text{hyp}}$

$\cos(\theta) = \frac{\text{adj}}{\text{hyp}} = \frac{b}{c}$

$\cos(\beta) = \frac{\text{adj}}{\text{hyp}} = \frac{a}{c}$

Memory trick:

Sohcahtoa
 (P Y O D V A P)
 (N P S S P H P)

Right triangle Rat's (#22)

To check $\frac{10}{12} = .83$ then go $\sin^{-1}(.83)$

53.90°

should be 55°

$$\frac{\text{Opp } A}{\text{Hyp}} = \frac{10}{12} = \frac{5}{6} = .83$$

$$\cos(55) = .57$$

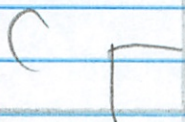
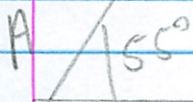
$$\frac{\text{Adj } A}{\text{Hyp}} = \frac{6.5}{12} = .54$$

$$\sin(55) = .81$$

$$\frac{\text{Opp } A}{\text{Adj } A} = \frac{10}{6.5} = 1.53$$

$$\tan(55) = 1.42$$

Yes, I think everyone got the same result for ratios because it is Cos, Sin, Tan



5, 12, 13

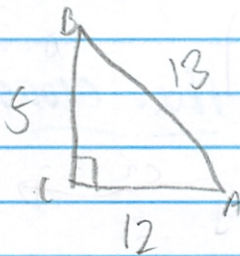
Trig Review

1. 2 smaller sides combined, bigger w/ third

2. Pythagorean $5^2 + 12^2 = 13^2$
 $25 + 144 = 169$

h
e
i
g
h
t
t
r
i
a
n

3. Sohcahtoa



Find α : $\text{Sig} \frac{\text{opp}}{\text{hyp}} = \frac{5}{13}$

$\sin \angle A = \frac{5}{13}$

~~Deq mode~~

Do $\boxed{5} \div \boxed{13} = .3846$

Do $\boxed{2nd} \boxed{\sin} .3846 = 22.61^\circ$

$\angle A = \text{that}$

$\sin \frac{\text{opp}}{\text{hyp}}$

$\cos \frac{\text{adj}}{\text{hyp}}$

$\tan \frac{\text{opp}}{\text{adj}}$

Find $\cos \angle A = \frac{\text{adj}}{\text{hyp}} = \frac{12}{13}$

$\cos \angle A = .9230$

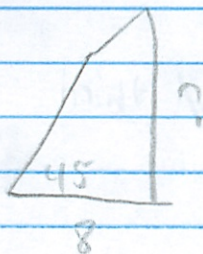
$\text{Reverse } \cos = 22.61 = m\angle A$

Find β : $\tan \angle B = \frac{\text{opp}}{\text{adj}}$

$\frac{12}{5} = 2.4$ Inverse $\rightarrow 67.38 = m\angle B$

Find $m\angle B$ if know A on Right triangles

$m\angle B = 90 - m\angle A$



~~21~~

~~$\frac{Adj}{Hyp} = \cos \angle$~~

Use $\tan 59$

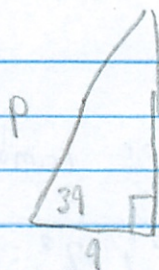
$$\tan(45) = \frac{\text{Opp}}{\text{Adj}}$$

$$\tan(45) = \frac{\text{Opp}}{8}$$

Do this

$$1 = \frac{x}{8}$$

$$1 = \frac{x}{8} \quad ? = 8$$



$$\cos = \frac{\text{Adj}}{\text{hyp}}$$

$$\cos(39) = \frac{9}{p}$$

$$(p) \cdot (0.777) = \frac{9}{p} (p)$$

Now cross

4 digits

$$0.7771 \rightarrow \frac{17771}{10000} = \frac{9}{p}$$

$$.7771 p = 9$$

$$\frac{.7771 p}{.7771} = \frac{9}{.7771}$$

$$p = 11.58$$

$(.7771)p = 9$
Then see

p468
tree + pendulum

5/5

1.



Do other way

$$x \tan(70) = \frac{12}{x} (x)$$

$$\frac{x \tan(70)}{\tan 70} = \frac{12}{\tan 70}$$

$$x = \frac{12}{1.3639}$$

$$x = 32.69$$

know adj - need opp, so use tan
* notice 2 mentioned

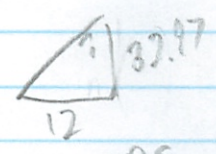
$$(70) \tan(70) = \frac{x}{12} (70)$$

$$12 (\tan 70) = x$$

$$12 (2.74) = x$$

$$32.96 = x$$

Weed 4



$$\tan ? = \frac{12}{32.97}$$

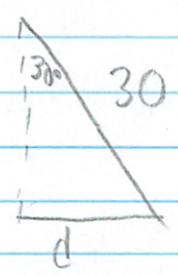
$$\tan ? = 1.3639$$

$$\tan^{-1}(1.3639) = 19.99$$

Inverse tan

$$32.96 + 5 = 37.96 = \text{height of tree}$$

2.



$$\sin(30) \frac{\text{opp}}{\text{hyp}}$$

$$(30) \sin(30) = \frac{d}{30} (30)$$

$$30 (\sin 30) = d$$

$$30 (0.5) = d$$

$$15 = d$$

know hyp, need opp

Sin, Cos, and Tan Buttons Revealed

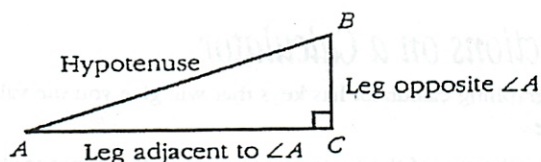
Did you ever wonder what those keys on your calculator that say "sin," "cos," and "tan" are all about? Well, here's where you find out.

You've seen that, whenever two right triangles have another angle in common, the triangles must be similar, and so the corresponding ratios of lengths of sides within those triangles are equal.

These ratios depend only on that common acute angle, and each ratio of lengths within the right triangle has a name. The study and use of these ratios is part of a branch of mathematics called **trigonometry**.

Suppose you are given an acute angle (in other words, an angle between 0° and 90°).

You can create a right triangle in which one of the acute angles is equal to that given angle. Suppose you label that triangle as shown in the diagram below, so that $\angle A$ is equal to the acute angle you started with.



The trigonometric ratios are then defined as explained on the following pages. The principles of similarity guarantee that these ratios will be the same for *every* right triangle that has an acute angle the same size as $\angle A$.

Sine of an Angle

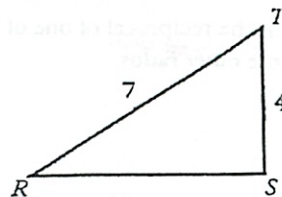
The **sine** of $\angle A$ is the ratio of the length of the leg opposite $\angle A$ to the length of the hypotenuse. The sine of $\angle A$ is abbreviated as $\sin A$. For example, in $\triangle RST$ below, the leg opposite $\angle R$ has length 4, and the hypotenuse has length 7, so $\sin R = \frac{4}{7}$.

In summary

$$\sin A = \frac{\text{length of leg opposite } \angle A}{\text{length of hypotenuse}}$$

or simply,

$$\sin A = \frac{\text{opposite}}{\text{hypotenuse}}$$



Cosine of an Angle

The **cosine** of $\angle A$ is the ratio of the length of the leg adjacent to $\angle A$ to the length of the hypotenuse. The cosine of $\angle A$ is abbreviated as $\cos A$. For example, in $\triangle UVW$ below, the leg adjacent to $\angle U$ has length 3, and the hypotenuse has length 5, so $\cos U = \frac{3}{5}$.

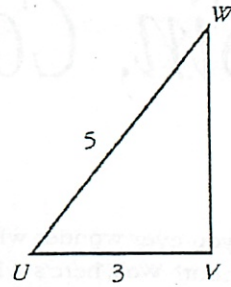
4/7 that and do inverse sine

In summary

$$\cos A = \frac{\text{length of leg adjacent to } \angle A}{\text{length of hypotenuse}}$$

or simply,

$$\cos A = \frac{\text{adjacent}}{\text{hypotenuse}}$$



Tangent of an Angle

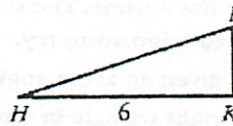
The tangent of $\angle A$ is the ratio of the length of the leg opposite $\angle A$ to the length of the leg adjacent to $\angle A$. The tangent of $\angle A$ is abbreviated as $\tan A$. For example, in $\triangle HKL$ on

In summary

$$\tan A = \frac{\text{length of leg opposite } \angle A}{\text{length of leg adjacent to } \angle A}$$

or simply,

$$\tan A = \frac{\text{opposite}}{\text{adjacent}}$$



$\tan A = \frac{2}{6} = \frac{1}{3}$

Then do
 $\tan^{-1}(.33)$
and get
the m of $\angle A$
 18°

Does that return measure for $\angle A$? or what?

Trigonometric Functions on a Calculator

Any scientific calculator or graphing calculator has keys that will give you the values of these functions for any angle.

In some calculators, you enter the size of the angle and then push the appropriate trigonometric key, while for other calculators, you do the opposite.

~~C~~ **Caution:** You have been measuring angles using *degrees* as the unit of measurement, but there are other units for measuring angles. Most calculators that work with trigonometric functions have a *mode* key that you can set to "deg."

doing $\tan(18)$ gives
you ratio
like .33

The Other Ratios

There are three other ratios of side lengths within a right triangle, in addition to the sine, the cosine, and the tangent. These other ratios are used less often and usually do not have their own calculator keys.

Each is the reciprocal of one of the three ratios already defined. Here are the definitions of those other ratios.

$$\text{cotangent } A = \frac{1}{\text{tangent } A}$$

$$\text{secant } A = \frac{1}{\text{cosine } A}$$

$$\text{cosecant } A = \frac{1}{\text{sine } A}$$

They are abbreviated, respectively, as $\cot A$, $\sec A$, and $\csc A$.

or inverse of
~~Sin~~
not inverse

Michael Plasmel

SHADOWS After Day 10

SIMILAR POLYGONS

In each of the pairs of figures below, assume the figures are similar and that they are facing the same way; that is, assume that the left side of one corresponds to the left side of the other, etc. In each case, do the following:

- Set up equations to find the lengths of the sides labeled by variables, and
- Find answers to the equations.

1.

$\frac{6}{12} = \frac{x}{15} = \frac{y}{19}$
 $12x = 90$
 $x = 7.5$
 $12y = 114$
 $y = 9.5$

2.

$\frac{8}{10} = \frac{11}{b} = \frac{6}{c}$
 $8a = 110$
 $8b = 60$
 $8c = 150$
 $a = 13.75$
 $b = 7.5$
 $c = 18.75$

3.

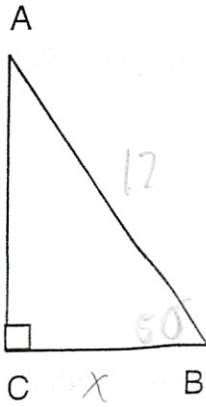
$\frac{p}{10} = \frac{18}{12} = \frac{15}{r} = \frac{20}{t}$
 $18t = 240$
 $t = 13\frac{1}{3}$
 $18p = 120$
 $15 = p$
 $t = 10$

4.

$\frac{x+3}{20} = \frac{x}{18}$
 $20x = 18(x+3)$
 $20x = 18x + 54$
 $-18x \quad -18x$
 $2x = 54$
 $x = 27$
 $x+3 = 30$

TRIANGLE TRIGONOMETRY

Find all lengths to nearest tenth.



$\sin(50) = \frac{x}{12}$
 $12(\sin 50) = x$
 $12(0.776) = x$
 $9.19 = x$

$\cos(50) = \frac{x}{12}$
 $12(\cos 50) = x$
 $12(0.642) = x$
 $7.71 = x$

Even Problems on loose leaf

1. $AB = 12, \angle B = 50^\circ, AC = 9.19, BC = 7.71$

2. $BC = 8, \angle A = 43^\circ, AC = 8.57, AB = 11.73$



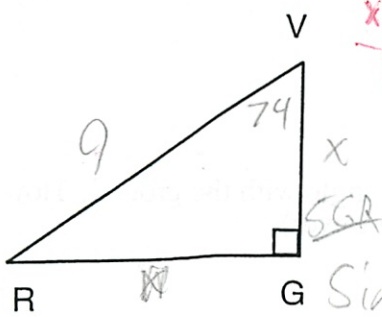
$\tan(67) = \frac{5}{x}$
 $x(\tan 67) = 5$
 $x(1.65) = 5$
 $x = 3.03$

$\sin(67) = \frac{5}{x}$
 $x(\sin 67) = 5$
 $x(0.9205) = 5$
 $x = 5.43$

Don't know shortcut yet

3. $HT = 5, \angle M = 67^\circ, MT = 5.43, HM = 3.03$

4. $MT = 13, \angle T = 21^\circ, HT = 12.13, HM = 4.65$

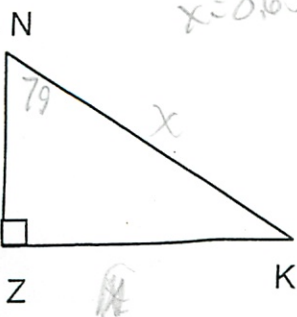


$\sin 74 = \frac{x}{9}$
 $9(\sin 74) = x$
 $9(0.9612) = x$
 $x = 8.65$

$\cos 74 = \frac{x}{9}$
 $9(\cos 74) = x$
 $9(0.2756) = x$
 $x = 2.48$

5. $VR = 9, \angle V = 74^\circ, GR = 8.65, GV = 2.48$

6. $GR = 26, \angle R = 13^\circ, RV = 26.68, GV = 112.61$



$\tan(79) = \frac{x}{17}$
 $17(\tan 79) = x$
 $17(3.487) = x$
 $x = 59.28$

$\cos(79) = \frac{17}{x}$
 $(\cos 79)x = 17$
 $0.2756x = 17$
 $x = 61.67$

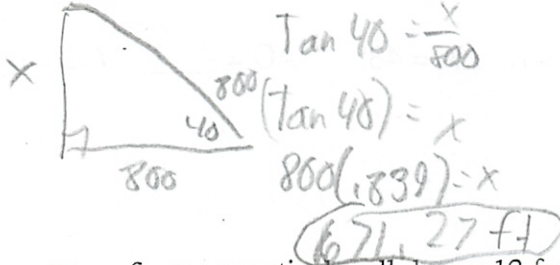
7. $NZ = 17, \angle N = 79^\circ, KZ = 59.28, KN = 61.67$

8. $KZ = 4, \angle K = 60^\circ, NZ = 6.92, KN = 2$

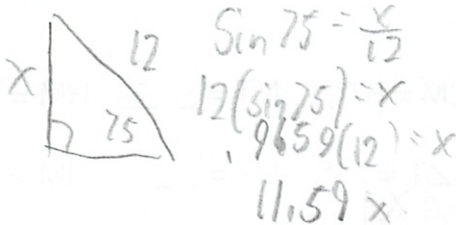
Can not be negative

For each problem, make a right triangular drawing labeled correctly with the given information and a variable for what you are trying to find. FORM A TRIG EQUATION, using sin, cos, or tan; THEN, write an equation that would find your variable. Using a calculator, find the solution to the question.

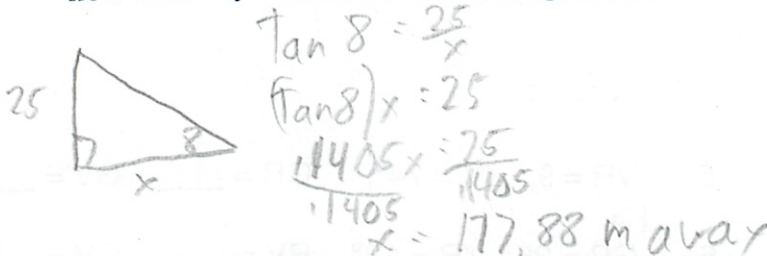
1. When the angle of elevation of the sun is 40 degrees, a building casts a shadow of 800 feet. How tall is the building?



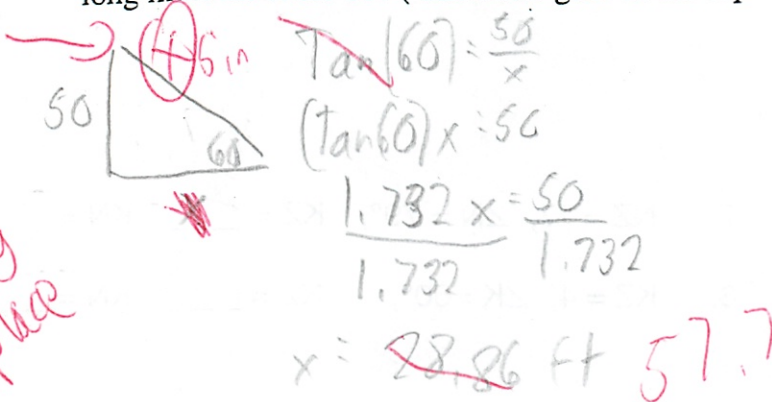
2. How far up a vertical wall does a 12 foot ladder reach if the angle it makes with the ground is 75 degrees?



3. The operator of a lighthouse spots a sailboat on a line that makes an 8 degree angle with the horizontal. If the top of the lighthouse is 25 meters above sea level, the sailboat is how far away from the base of the lighthouse?



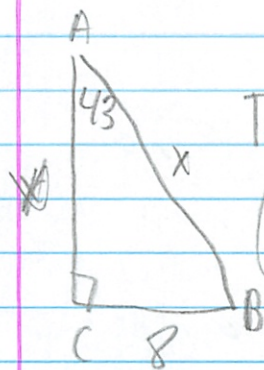
4. A support cable for a 50 ft. tower is to make a 60 degree angle with the ground. How long must the cable be? (The cable goes to the top of the tower).



Even Problems

Shadows 16

2.



$$\tan(43) = \frac{8}{x}$$

$$(\tan 43)x = 8$$

$$\frac{.9325x = 8}{.9325 \quad .9325}$$

$$x = 8.57$$

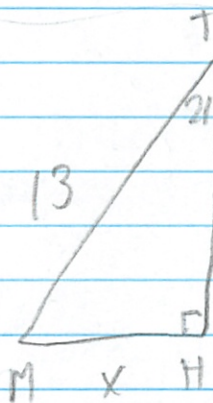
$$\sin(43) = \frac{8}{x}$$

$$(\sin 43)x = 8$$

$$\frac{.6819x = 8}{.6819 \quad .6819}$$

$$x = 11.73$$

4.



$$\cos(21) = \frac{x}{13}$$

$$13(\cos 21) = x$$

$$.9335(13) = x$$

$$12.13 = x$$

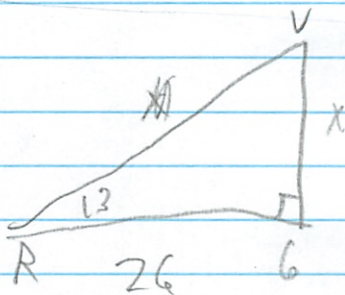
$$\sin(21) = \frac{x}{13}$$

$$13(\sin 21) = x$$

$$13(.3583) = x$$

$$4.65$$

6.



$$\cos(13) = \frac{26}{x}$$

$$x(\cos 13) = 26$$

$$\frac{.9743x = 26}{.9743 \quad .9743}$$

$$x = 26.68$$

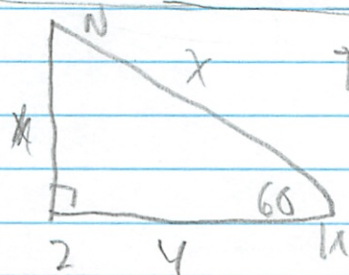
$$\tan(13) = \frac{26}{x}$$

$$(\tan 13)x = 26$$

$$\frac{.2308x = 26}{.2308 \quad .2308}$$

$$x = 112.61$$

8.



$$\tan 60 = \frac{x}{4}$$

$$4(\tan 60) = x$$

$$1.732(4) = x$$

$$6.928 = x$$

$$\cos 60 = \frac{4}{x}$$

$$(\cos 60)x = 4$$

$$\frac{.5x = 4}{.5 \quad .5}$$

$$x = 2$$

Opposite/Adj (H24)

5/8

1. They must both add to 90°

2. $\frac{BC}{AB}$ for $\angle B$ $\frac{Adj}{hyp}$ or $\cos \angle B$

For $\angle A$ $\frac{opp}{hyp}$ or $\sin \angle A$

are =

$\angle A$ and $\angle B$ are Complementary (add to 90°)

3. $90^\circ -$ The \sin of an acute angle in a right triangle is the \cos of the other acute angle

$90^\circ -$ the \cos of an acute angle in a right triangle is the \sin of the other acute \angle .

$$\sin \angle B = \cos \angle A$$

$$m\angle A + m\angle B = 90^\circ$$

$$\sin \angle A = \cos (90 - \angle A)$$

$$m\angle B = 90^\circ - m\angle A$$

Example $\sin 30^\circ = \cos (90 - 60)$

$$\sin 30 = \cos 60$$

$$.5 = .5$$

(V)

Name Mike Plummer
 Date Apr 5/6/05 Act 5/9

Shadows Quiz 3
 55 points

$\frac{49}{55}$ $\frac{16}{16}$

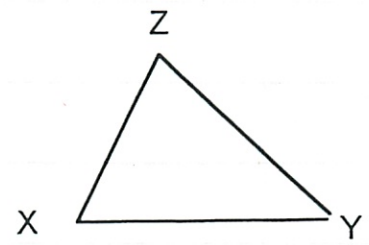
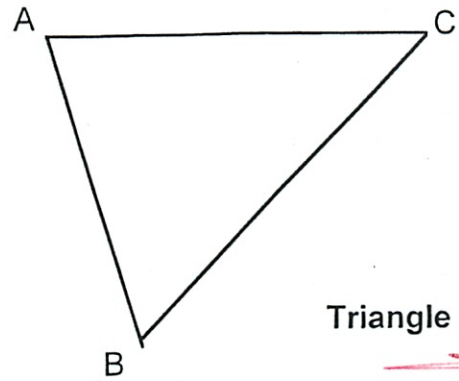
Solve each proportion for x. Show all work for full credit! {3 points each}

1) $\frac{5}{8} = \frac{x}{12}$
 $5 \times 12 = 8x$
 $60 = 8x$
 $\frac{60}{8} = \frac{8x}{8}$
 $7.5 = x$

2) $\frac{4}{x} = \frac{x}{4}$
 $x^2 = 4 \times 4$
 $x^2 = 16$
 $x = \pm 4$

3) $\frac{x}{x+2} = \frac{2}{3}$
 $3x = 2(x+2)$
 $3x = 2x + 4$
 $-2x \quad -2x$
 $x = 4$

↑
 $\frac{89}{100}$



$\frac{AB}{YZ} = \frac{BC}{ZX} = \frac{CA}{XY}$

Triangle ABC is similar to Triangle YZX

4) $\angle A = 70^\circ$ and $\angle B = 50^\circ$, find $\angle X$.
 {3 points}

$180 - 70 = 110$
 $- 50$
 $\hline 60$
 $m\angle X = 60$

5) $AB = 6$, $AC = 9$, and $YZ = 10$. Find XY .
 {3 points}

$\frac{6}{16} = \frac{9}{x}$ $\frac{6x}{6} = \frac{90}{6}$
 $xy = 15$

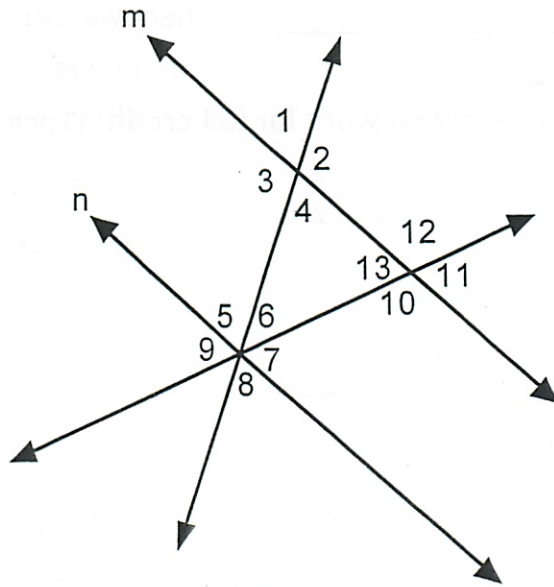
6) $AB = x$, $XY = x$, $AC = 20$, $YZ = 5$. Find AB .
 {3 points}

$\frac{x}{5} = \frac{20}{x}$
 $x^2 = 100$
 $x = 10$
 $AB = 10$

7) $CB = 6$, $AC = 8$, and $YX = 15$. Find ZX .
 {3 points}

$\frac{6}{x} = \frac{8}{15}$ $8x = 6(15)$
 $\frac{8x}{8} = \frac{90}{8}$
 $2x = 11\frac{1}{2}$
 $x = 11.25$

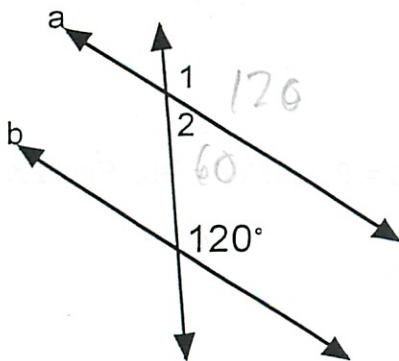
Given: $m \parallel n$



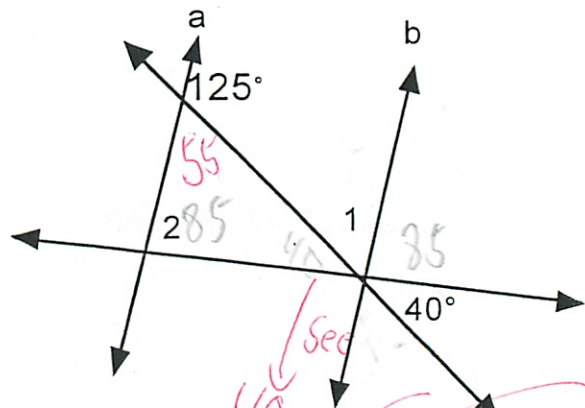
Classify each pair of angles as vertical, alternate interior, or corresponding.
{3 points each}

- 8) $\angle 1$ and $\angle 4$ vertical
- 9) $\angle 11$ and $\angle 7$ Corresponding
- 10) $\angle 3$ and $\angle 2$ vertical
- 11) $\angle 1$ and $\angle 5$ Corresponding
- 12) $\angle 5$ and $\angle 4$ alt. interior
- 13) $\angle 13$ and $\angle 7$ alt. interior

In each of the following, line a is parallel to line b. Find the measure of angle 1 and angle 2.
{3 points each}

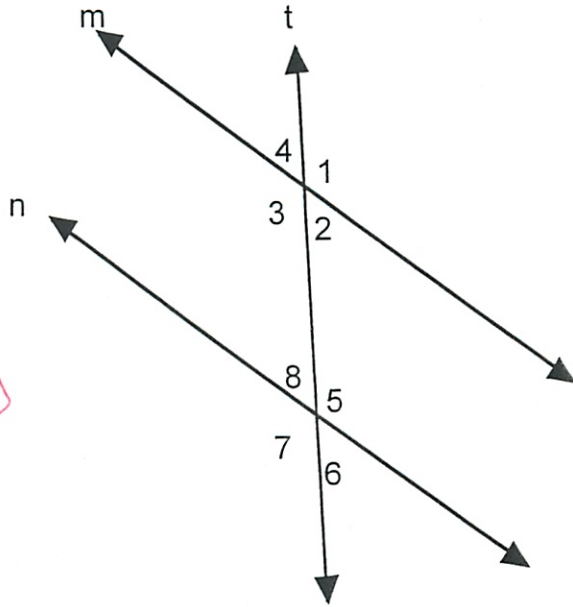


- 14) Angle 1 = 120° 15) Angle 2 = 60°



- 16) Angle 1 = 55° 17) Angle 2 = 85°

Given: $m \parallel n$



Satz
 Given $m \parallel n$
 P: $\angle 3 + \angle 8$ are suppl

18) Angle 3 and angle 8 are classified as same side interior angles.
 Prove (explain in words) that angle 3 and angle 8 are supplementary. {4 points}

Statement	Reason
$m \parallel n$	Given
$\angle 3$ and $\angle 4$ are suppl	Adj. angles share a line <i>2 adj angles w/ exterior rays forming a line are suppl</i>
$\angle 7$ and $\angle 8$ are suppl	adj. angles share a line
$m\angle 4$ and $m\angle 8$ are \cong	Corresponding angles
$\angle 3$ and $\angle 8$ are suppl	transitive property <i>-2</i> Substitution (2)

Don't need!

Grading for Pow 17

Michael Plosmeier

Diagrams!

Points

1. Process

- unrelated to the problem----- 2
- incomplete - no work, tables, or diagrams shown----- 5
- complete - minor gaps in process explanation----- 7
- complete - explanation with examples, charts, tables, and work shown----- 10

4/25

2. Solution

- wrong answers- no explanation and not defended----- 2
- correct answers- no explanation or proof of answer being correct----- 4
- wrong answers - with explanation----- 6
- partially correct answers - some values correct / some incorrect----- 8
- correct - complete explanation and well supported----- 10

OK

TOTAL POINTS (20)

