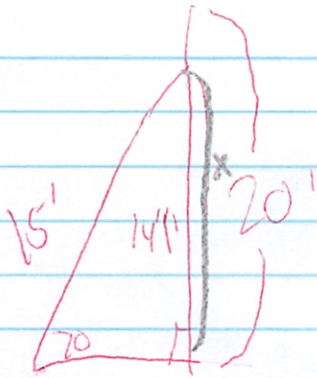


Pole Cat

p501

5/6 Assigned
5/9 Actual



$$\sin 70 = \frac{\text{opp}}{\text{hyp}} = \frac{x}{15}$$

$$\sin 70 = \frac{x}{15}$$

$$15(\sin 70) = x$$

$$15(0.9396) = x$$

$$14.1 = x$$

Diana 5' 6" + 1' reach
15' ladder.

14' 1" \in ladder height on pole (top of ladder)

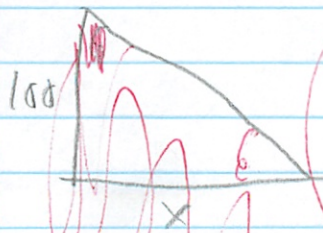
6' 6" \in her + reach

20' 7" \in She can make it

Smoker + Dude (#23)

5/2

1.b

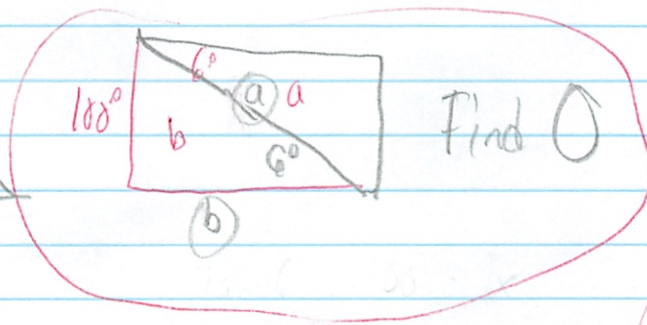


$$\tan 6 = \frac{x}{100}$$

$$100(\tan 6) = x$$

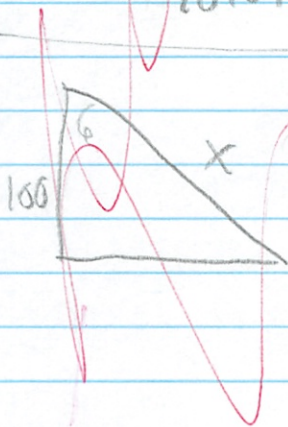
$$105.1(100) = x$$

$$x = 10.51 \text{ - He is } 10.51$$



So
Re-d
No x

1a



$$\cos(6) = \frac{100}{x}$$

$$(\cos 6)/x = 100$$

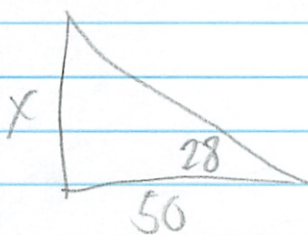
$$\frac{.9945x}{.9945} = \frac{100}{.9945}$$

$$x = 100.5508 \text{ ft from fire}$$

? correct

Pg.

2



$$\tan 28 = \frac{x}{50}$$

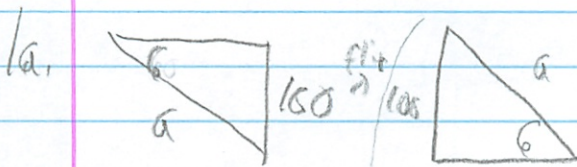
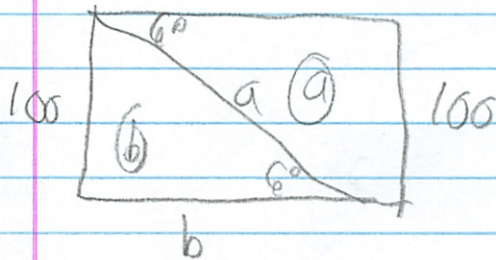
$$\tan 28(50) = x$$

$$.5317(50) = x$$

$$26.58 = x$$

$$26.58 \text{ ft tall}$$

(#123) Again

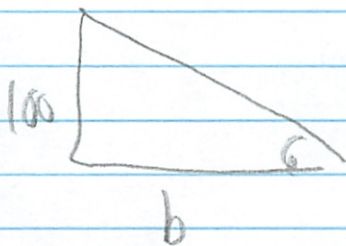


$$\sin 6 = \frac{100}{a}$$

$$(\sin 6)a = 100$$

$$\frac{(.1095)a}{.1095} = \frac{100}{.1095}$$

$$a = 956.67 \text{ ft}$$



$$\tan 6 = \frac{100}{b}$$

$$(\tan 6)b = 100$$

$$(.1051)b = 100$$

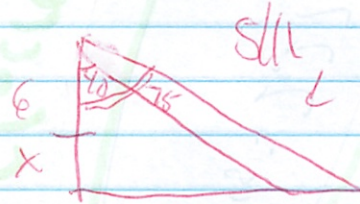
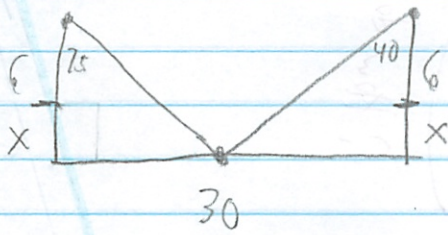
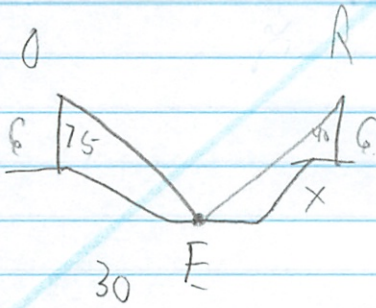
$$\frac{.1051b}{.1051} = \frac{100}{.1051}$$

$$b = 951.43 \text{ ft}$$

Dog in a ditch

p502

5/10



$$\frac{\text{Real}}{\text{Scale}} \quad \frac{22}{30} \quad \frac{44}{6}$$

$$30x = 132$$

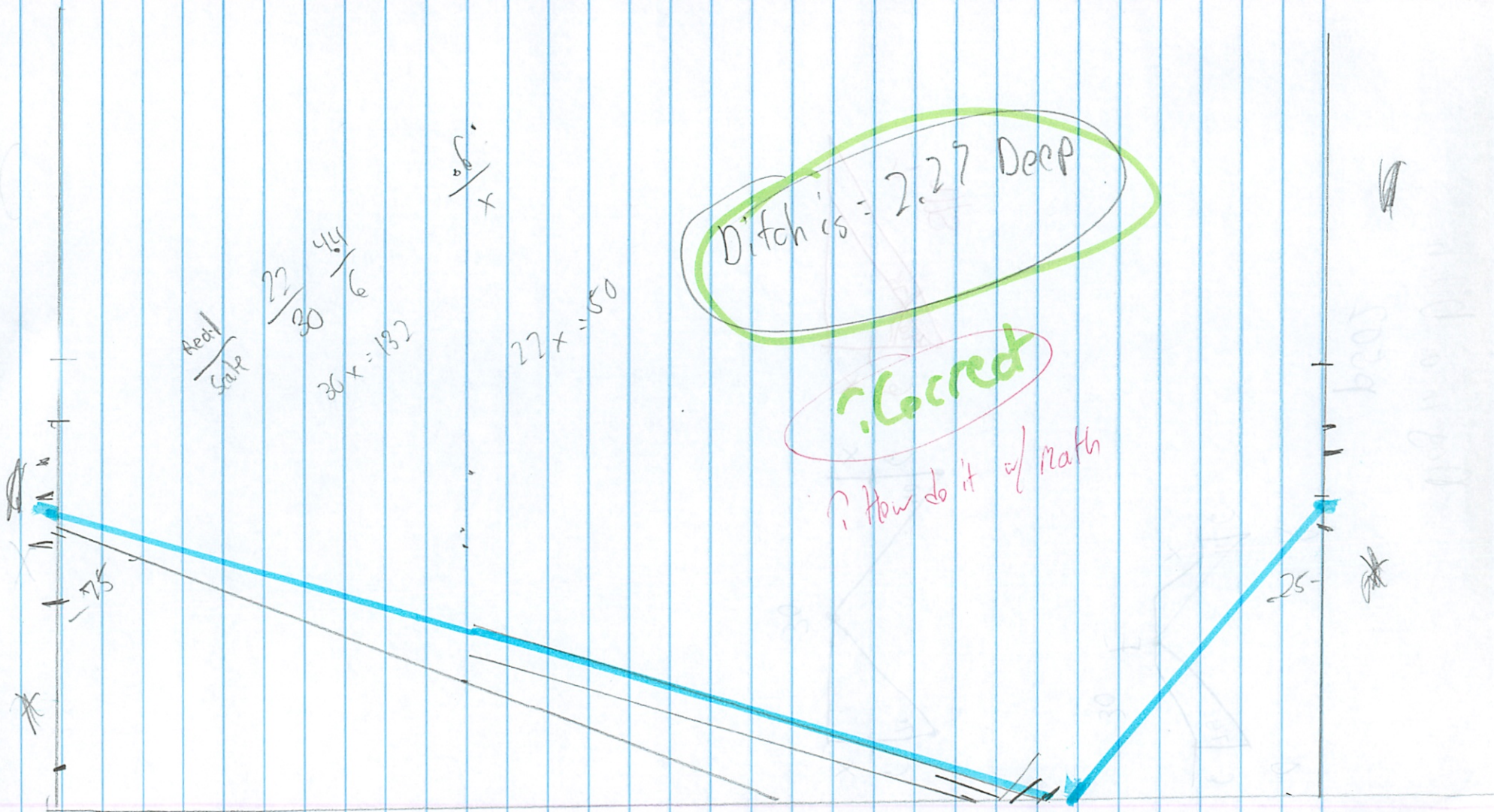
$$\frac{8}{x}$$

$$22x = 50$$

Ditch is = 2.27 Deep

Correct

How do it w/ math



Name Michael Plasmeier

Date 5/9

Show All Work

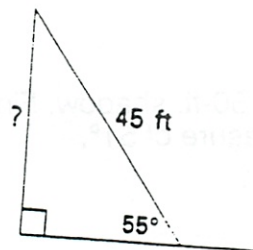
- 1) A 45-ft ladder makes an angle of 55° with the ground. How high up the wall does the ladder reach?

$$\sin 55 = \frac{x}{45}$$

$$45(\sin 55) = x$$

$$45(.8191) = x$$

$$36.86 \text{ ft up}$$



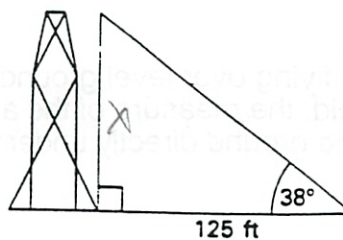
- 2) At a point 125 ft from the base of a tower, the angle of elevation of the top of the tower has a measure of 38° . How high is the tower?

$$\tan 38 = \frac{x}{125}$$

$$125(\tan 38) = x$$

$$125(.7812) = x$$

$$97.65 \text{ ft tall}$$



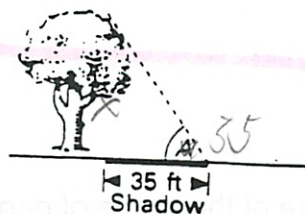
- 3) A tree casts a shadow that is 35 ft. long. The angle of elevation, angle A is 55° . How high is the tree?

$$\tan 55 = \frac{x}{35}$$

$$35(\tan 55) = x$$

$$35(1.428) = x$$

$$49.98 \text{ ft tall}$$



- 4) A 20-ft. ladder is leaning against a wall. The foot of the ladder forms an angle of elevation of measure 65° with the ground. How far is the top of the ladder from the ground?

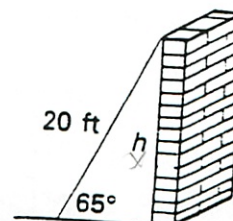
$$\sin 65 = \frac{x}{20}$$

$$20(\sin 65) = x$$

$$20(.9063) = x$$

$$18.13 \text{ ft up}$$

Sound
Correctly



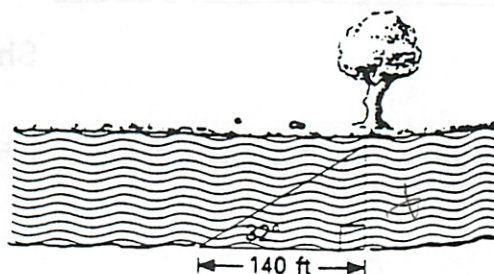
- 5) To estimate the width of a lake, Bob stood directly opposite a large tree. He then walked 140 ft. along the bank and approximated the measure of the angle between his line of sight to the tree and the lake's edge as 32° . Find the approximate width of the lake.

$$\tan 32 = \frac{x}{140}$$

$$140(\tan 32) = x$$

$$140(0.6248) = x$$

87.48 ft wide



- 6) A tree casts a 60-ft. shadow. Find the height of the tree if the angle of elevation of the sun has a measure of 51° .



angle of elevation
see 7

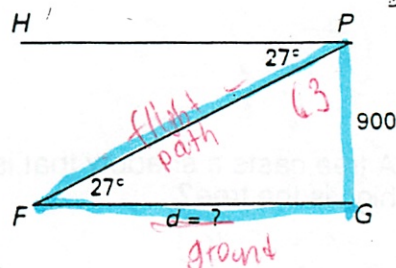
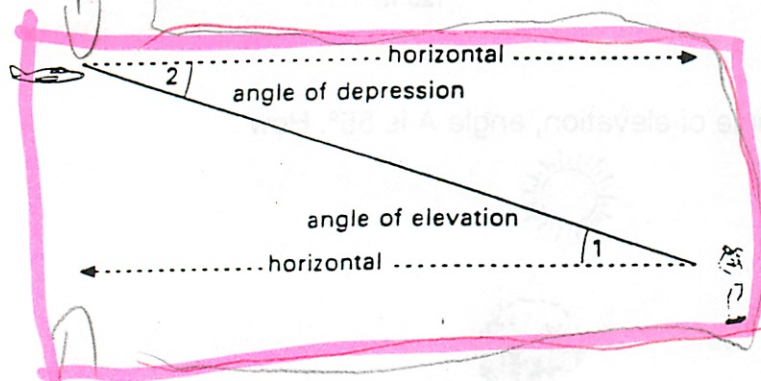
$$\tan 51 = \frac{x}{60}$$

$$60(\tan 51) = x$$

$$60(1.234) = x$$

74.09 ft tall

- 7) A plane is flying over level ground at an altitude of 900 m. When the pilot sights a landing field, the measure of the angle of depression is 27° . Find the distance from the point on the ground directly under the pilot to the landing field.



$$\tan 27 = \frac{900}{d}$$

$$(\tan 27)d = 900$$

$$(0.5095)d = 900$$

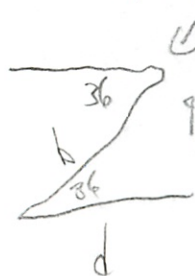
$$\frac{900}{0.5095} = d$$

981.3 m

- 8) The measure of the angle of depression 36° . The altitude of the plane is 9,000 ft.

a) Find the ground distance d from the plane to the runway.

b) Find the flight distance from the plane to the runway.



$$\tan 36 = \frac{9000}{d}$$

$$9,000 (\tan 36) = 9000$$

$$(0.7265)d = 9000$$

$$\frac{9000}{0.7265} = d$$

$d = 12387$ ft

$$\sin 36 = \frac{9000}{b}$$

$$(\sin 36)b = 9000$$

$$(0.5877)b = 9000$$

$$\frac{9000}{0.5877} = b$$

$b = 15311$

Units

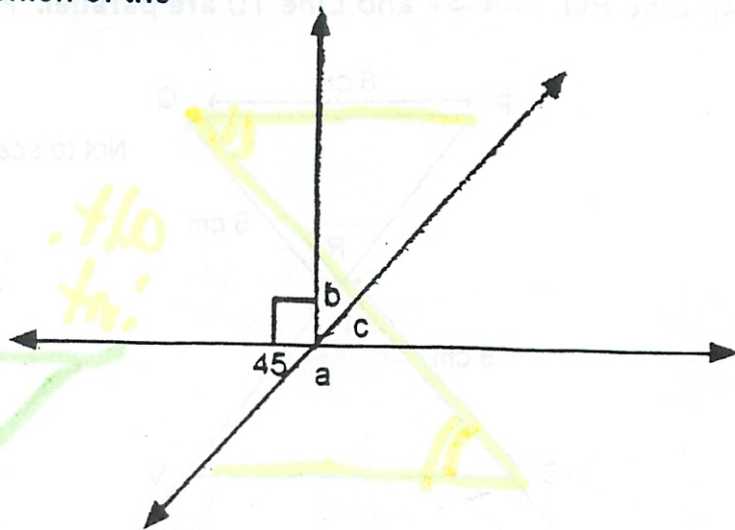
Michael Plasmeier

1) For the figure at the right, which of the following must be true?

1) $a = 3c$

2) $a = 90$

3) $b = c$



A) 1 only

B) 1 & 2 only

C) 2 only

D) 1, 2 & 3

E) 1 & 3 only

Circled wrong one →

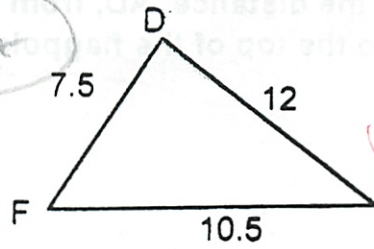
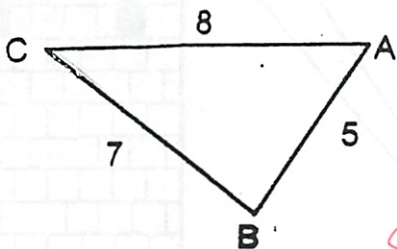
(stupid mistake)

2) What must be true about the sides of any triangle?

It must be smaller than the 2 other sides combined (Triangle Inequality)

All Add up to 180°

3) Are the following triangles similar. Explain your answer.



No order

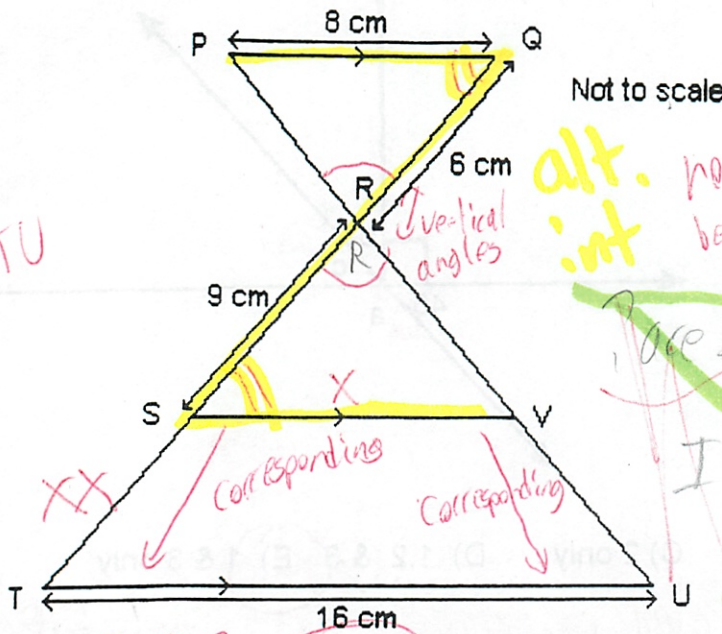
$\frac{8}{10.5} \quad \frac{5}{7.5} \quad \frac{7}{12}$
 $\frac{5}{7.5} \quad \frac{7}{10.5} \quad \frac{8}{12}$
then cross X

$8(7.5) = 10.5(5) \quad 7(7.5) = 5(10.5)$
 $60 \neq 52.5 \quad 52.5 \neq 52.5 \quad 10.5(7) = 12(8)$
 $73.5 \neq 96$

Go from largest to smallest

No, not similar because I don't see the 6 sides in proportion, and nothing tells me what order to put it in

4) Line PQ, Line SV and Line TU are parallel. Find SV and ST.



Not to scale

alt. int.

new 2 angles are = because 2 angles are =

$PRQ \sim LRS$

$$\frac{PR}{VR} = \frac{RQ}{RS} = \frac{QP}{SP}$$

$$\frac{6}{9} = \frac{8}{x}$$

$$6x = 72$$

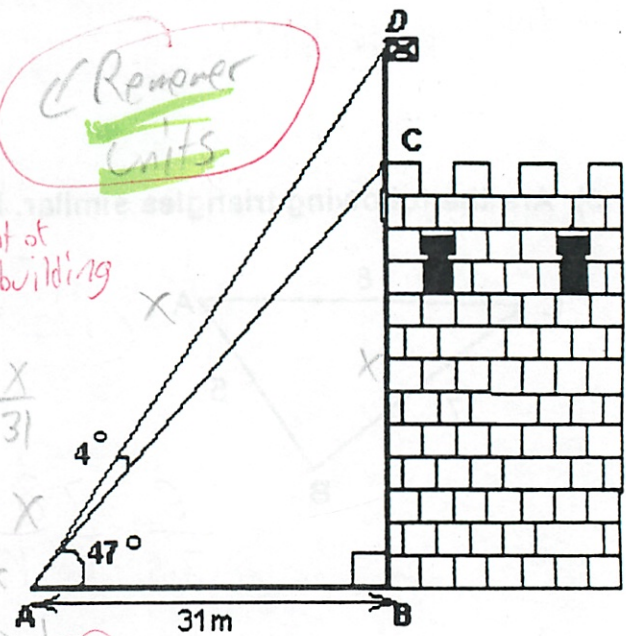
$$x = 12$$

5) Calculate the height BD, of the flag above the ground

6) Calculate the height, CD, of the flagpole.

7) Calculate the distance, AD, from point A to the top of the flagpole.

Remover units



$$\tan(4+47) = \frac{x}{31}$$

$$\tan 47 = \frac{x}{31}$$

$$\tan 51 = \frac{x}{31}$$

$$31(\tan 47) = x$$

$$31(\tan 51) = x$$

$$31(1.0723) = x$$

$$31(1.234) = x$$

$$33.24 = x$$

$$38.281 = x$$

$$\cos(4+47) = \frac{31}{x}$$

$$\cos(51) = \frac{31}{x}$$

$$x(\cos 51) = 31$$

$$\frac{.6293x}{.6293} = \frac{31}{.6293}$$

$$x = 30.37$$

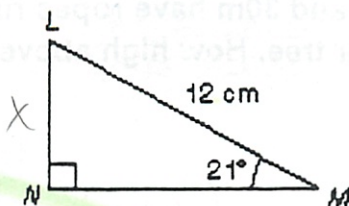
8) Find LN.

$$\sin 21 = \frac{x}{12}$$

$$12(\sin 21) = x$$

$$12(.3583) = x$$

$$4.3 = x$$



$$LN = 4.3 \text{ cm}$$

9) A surveyor stands at a Point P. She measures the angle of elevation of the mountain top Q as 20.8 degrees and its horizontal distance as 14.25 km. Find the height of the mountain.

$$\tan 20.8 = \frac{x}{14.25}$$

$$14.25(\tan 20.8) = x$$

$$14.25(.3798) = x$$

$$5.413 \text{ km}$$



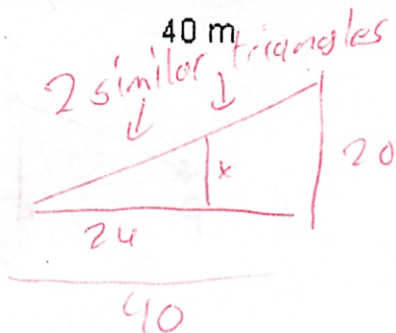
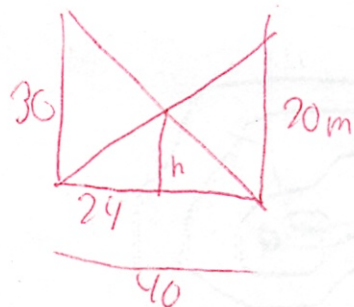
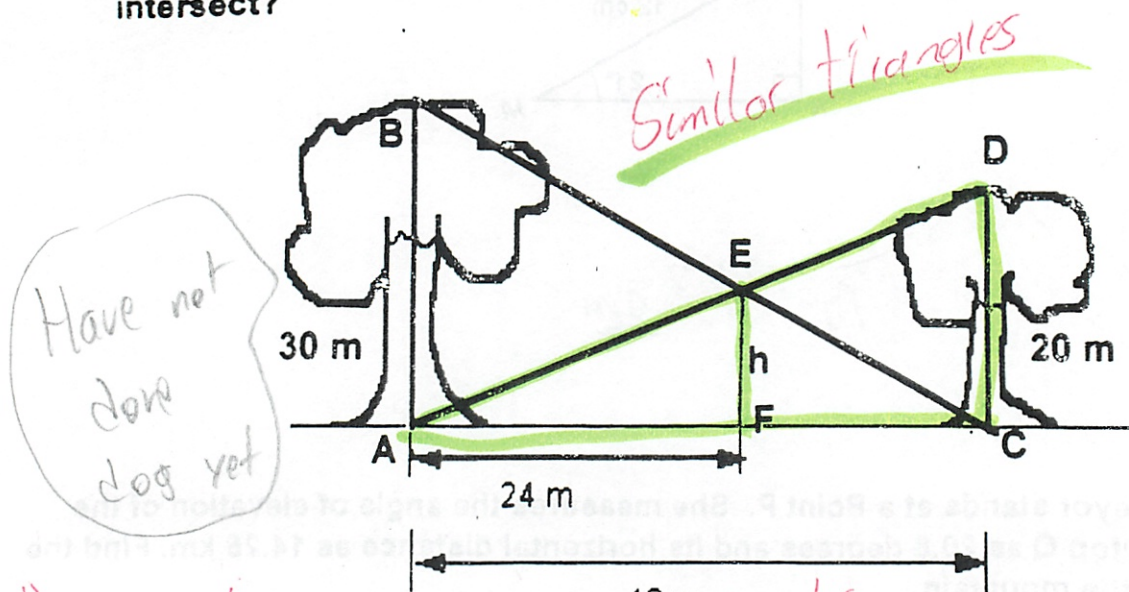
Not good picture

because topo lines

represent birds-eye

view

- 10) Two trees of height 20m and 30m have ropes running from the top of each tree to the bottom of the other tree. How high above the ground do the ropes intersect?

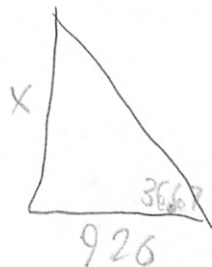
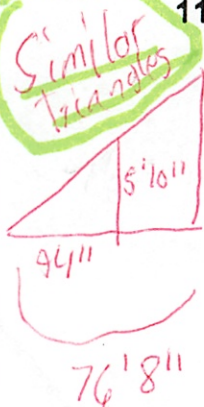


$$\frac{20}{40} = \frac{x}{24}$$

$$\frac{40x}{40} = \frac{480}{40}$$

$$12 = x$$

- 11) I need to cut down a tree that's shading my garden and drop it between the garden and another tree; if it's taller than 59 feet it will smash my lilac bush. I measured the tree's shadow and my shadow standing next to it - the tree's shadow was 76'8", and mine was 94 inches. I'm 5'10"; will the tree land on the lilac?



$$\tan \angle A = \frac{76}{94}$$

$$\tan \angle A = .7446$$

$$\angle A = 36.67^\circ$$

$$\tan(36.67) = \frac{x}{926}$$

$$926(\tan 36.67) = x$$

$$926(.7446) = x$$

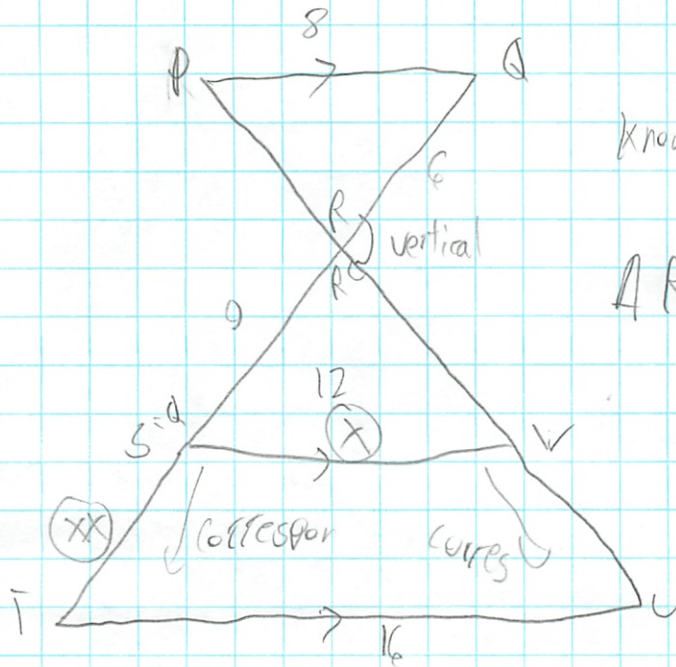
It is shorter and will not hit. But that doesn't mean you can cut it down

$$x = 684.99 \text{ inches}$$

$$\text{or } 57'1"$$

Study

5/12



know it's similar

$$\triangle RPQ \sim \triangle RSV$$

$$\frac{RP}{RV} = \frac{PQ}{VS} = \frac{QR}{SR}$$

$$\frac{8}{x} = \frac{6}{4}$$

$$\frac{6x}{6} = \frac{22}{6}$$

$$x = 12$$

$$\triangle RTU \sim \triangle RSV$$

$$\frac{RT}{RS} = \frac{TU}{SV} = \frac{UR}{VR}$$

$$\frac{x}{9} = \frac{16}{12} = \frac{?}{?}$$

why not

$$\frac{144}{12} = \frac{12x}{12}$$

$$12 - x = 9 + xx$$

$$3 = xx$$

$$\frac{9+xx}{9} = \frac{16}{12}$$

Shadows Assessment

55 Points

Name Michael Plasmeier
Date 5/12

8848

50
55

Circle the correct answer to the following questions.

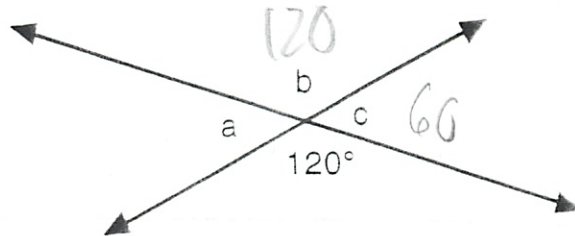
- 1) For the intersecting lines at the right, which of the following must be true? (3 points)

1) $b = 2c$

2) $a = \frac{b}{2}$

3) $a + 120 = b + c$

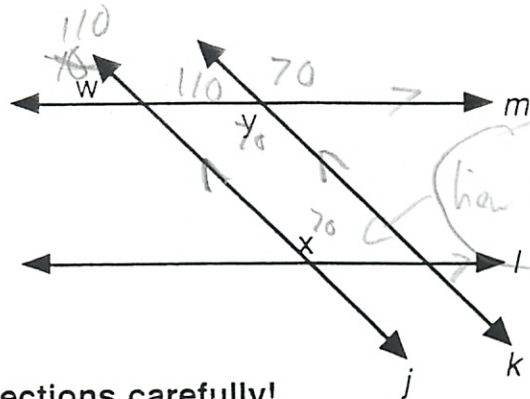
- A) 1 only B) 1 and 2 only C) 2 only D) 2 and 3 only E) 1, 2 and 3



90.9%

- 2) In the figure to the right j is parallel to k and l is parallel to m . If $x + y = 140$, what is the value w ? (3 points)

- A) 20 B) 40 C) 70 D) 110 E) 140



how is obtuse angle = to 70°

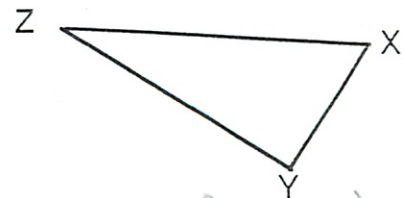
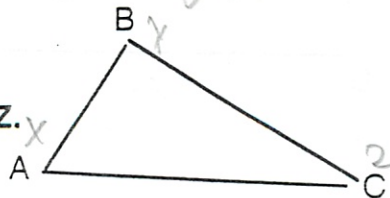
Complete each of the following. Read directions carefully!

Is it possible to construct a triangle with sides of the given lengths? Answer yes or no, if no explain why not. (3 points)

- 3) 1 cm, 5 cm, 6 cm No, the 2 smallest sides are not larger than the largest side.

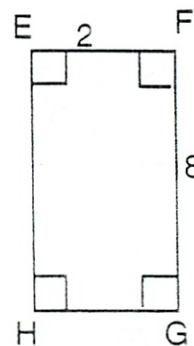
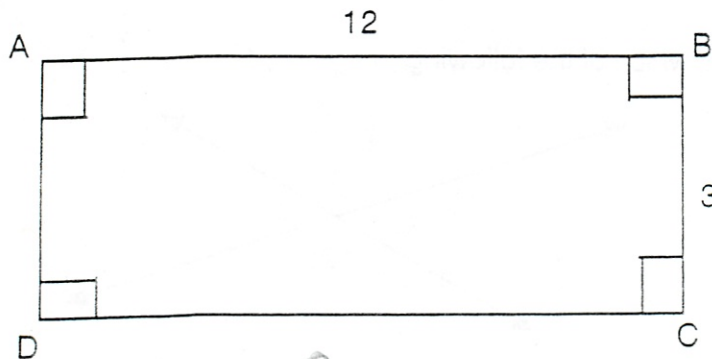
$\triangle ABC$ is similar to $\triangle XYZ$.

(3 points each)



- 4) Identify two pairs of corresponding angles. A and X B and Y
AB and XY CA and ZX

- 6) Determine if the two polygons below are similar. If they are similar explain why you know they must be similar. If they are not similar explain why you know they can not be similar. (5 points)



All angles = \checkmark *good*

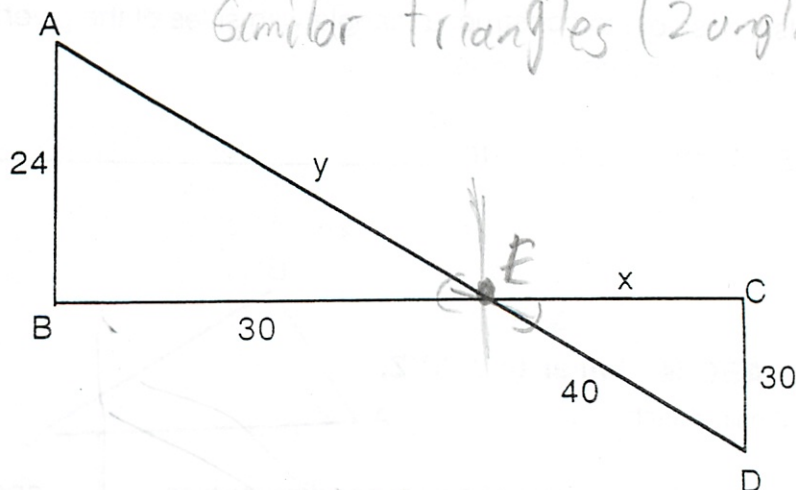
Sides in proportion \times $\frac{12}{2} = \frac{3}{8} \rightarrow 8(12) \neq 3(2)$

96 \neq 6 \times -3

No, the sides are not in proportion, so it's not similar

- 7) Find the values of x and y in the diagram below. Show all work for credit! (6 points)

$\overline{AB} \parallel \overline{CD}$



\times

$$\frac{24}{30} = \frac{y}{40}$$

$$\frac{30}{30} \times = \frac{960}{36}$$

$$y = 32$$

$$\frac{AB}{CD} = \frac{AE}{ED}$$

$$\frac{24}{30} = \frac{30}{x}$$

$$\frac{900}{24} = \frac{24x}{24}$$

$$x = 37.5$$

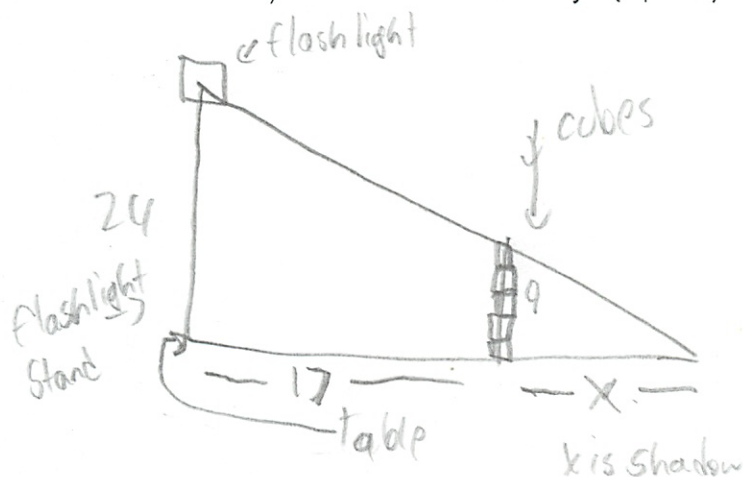
$$\frac{AB}{ED} = \frac{BE}{CE}$$

(3)

8) There is a tower of cubes 9 inches tall, placed on a table. You are shining a flashlight at the tower, and the flashlight is mounted on a stand so that it is 24 inches above the table top. The distance from the bottom of the tower to the spot on the table directly below the flashlight is 17 inches. How long is the shadow cast by the tower?

a) Draw and label a diagram {3 points}

b) Show all work clearly! {5 points}



similar triangles

$$\frac{24}{9} = \frac{17+x}{x}$$

$$24x = 9(17+x)$$

$$24x = 135 + 9x$$

$$-9x \quad -9x$$

$$15x = 135$$

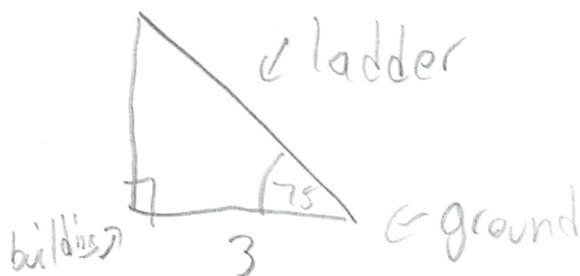
$$\frac{15x}{15} = \frac{135}{15}$$

$$x = 9$$

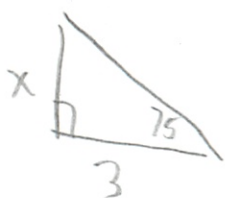
The shadow is 9 in long

9) A ladder is leaning up against a building. The bottom of the ladder is 3 feet away from the bottom of the building, and makes an angle of 75 degrees with the ground.

a) Draw and label a diagram. {3 points}



b) How high up on the building does the ladder reach? Show all work! {5 points}



$$\tan 75 = \frac{\text{opp}}{\text{adj}} = \frac{x}{3}$$

$$\tan 75 = \frac{x}{3}$$

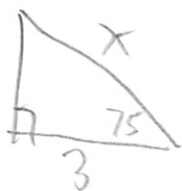
$$3(\tan 75) = x$$

$$3(3.7320) = x$$

$$11.196 = x$$

Ladder reaches 11.196 ft up building

c) How long is the ladder? Show all work? {5 points}



$$\cos 75 = \frac{\text{adj}}{\text{hyp}} = \frac{3}{x}$$

$$\cos 75 = \frac{3}{x}$$

$$(\cos 75)x = 3$$

$$.2588x = 3$$

$$\frac{.2588x}{.2588} = \frac{3}{.2588}$$

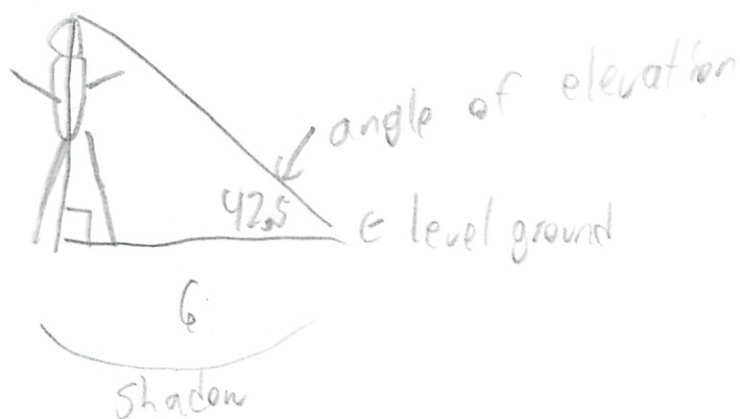
$$x = 11.5911$$

Ladder is 11.59 ft long

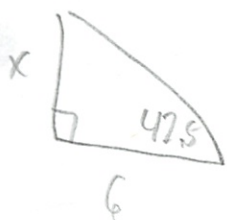
0

10) Carrie is standing on level ground and has a shadow which is 6 feet long. The angle of elevation of the sun is 42.5 degrees.

a) Draw and label a diagram. {3 points}



b) How tall is Carrie? Show all work! {5 points}



$$\tan 42.5 = \frac{\text{opp}}{\text{adj}} = \frac{x}{6}$$

$$\tan 42.5 = \frac{x}{6}$$

$$6(\tan 42.5) = x$$

$$6(.9163) = x$$

$$5.49 = x$$

Carrie is 5.49 feet tall

Pit + Pendulum

Mean \rightarrow Average

$$\frac{\sum_{i=1}^n x_i}{n} = \bar{x}$$

\bar{x} \leftarrow symbol of mean

5/13

Median \rightarrow the "middle" number

Mode \rightarrow most frequently occurring #

range \rightarrow difference from high to low

Standard deviation

All measures
of central
tendency

2, 2, 3, 3, 4, 4, 4, 4, 5, 6, 7

$n = 11$ (11 numbers above) \nearrow count 5 from

to find median $11/2 = 5\frac{1}{2}$

median = 4

mode = 4 $\bar{x} = 4$

Another way

to write: $2(2) + 2(3) + 4(4) + 1(5) + 1(6) + 1(7)$

$$4 + 6 + 16 + 5 + 6 + 7 = 44 / 11 = 4$$

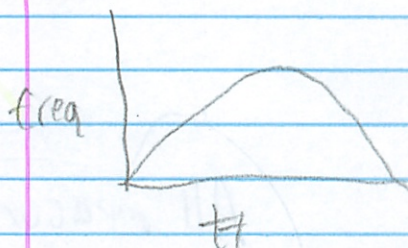
w/ even number of data

\uparrow
of pieces

3 | 4 | 5 | 6

$$(4 + 5) / 2 = 4.5 = \text{median}$$

Tossed a die



normal or bell curve

Chab. 10.10.10

10.10.10

10.10.10

10.10.10

10.10.10

10.10.10

10.10.10

10.10.10

10.10.10

10.10.10

10.10.10

Coin Flip (#8)

8/15

Heads.

7	6	8	7
4	7	3	6
5	5	6	5
7	7	6	5
7	5	8	100
7	4	6	
7	6	5	
7	5	5	
7	6	4	
4	3	7	
7	4	7	
7	7	7	
7	3	5	
7	5	5	
7	7	7	
7	8	5	
2	3	3	
5	6	7	
2	4	7	
3	3	4	
3	3	5	
2	3	7	
3	3	7	
6	5	7	
6	6	3	
6	6	4	
6	5	6	
6	4	3	
6	3	4	
6	3	4	
6	3	6	
6	3	3	

Median 5

Mode 5

Mean 5.24

Range 7

Count 0-8

Count 1-0

" 2-3

" 3-16

" 4-11

" 5-25

" 6-19

" 7-20

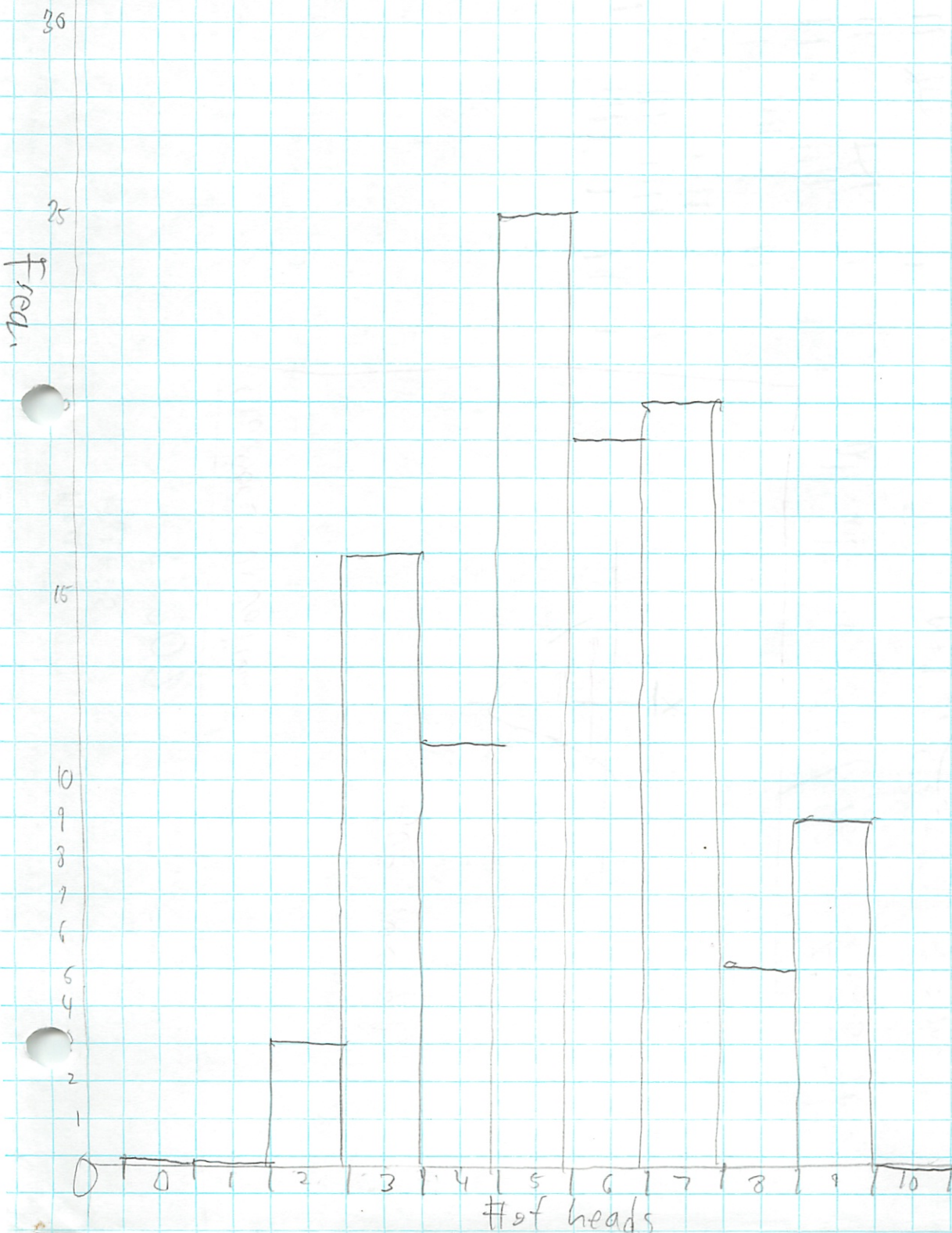
" 8-5

" 9-1

" 10-0

Coin Flip #8

5/16



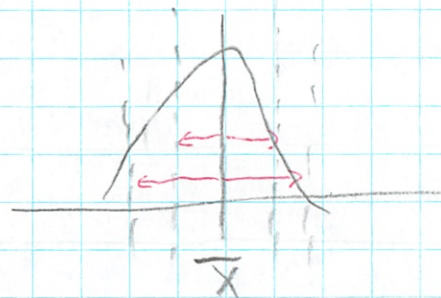
Over →

mean = 3
mode = 5

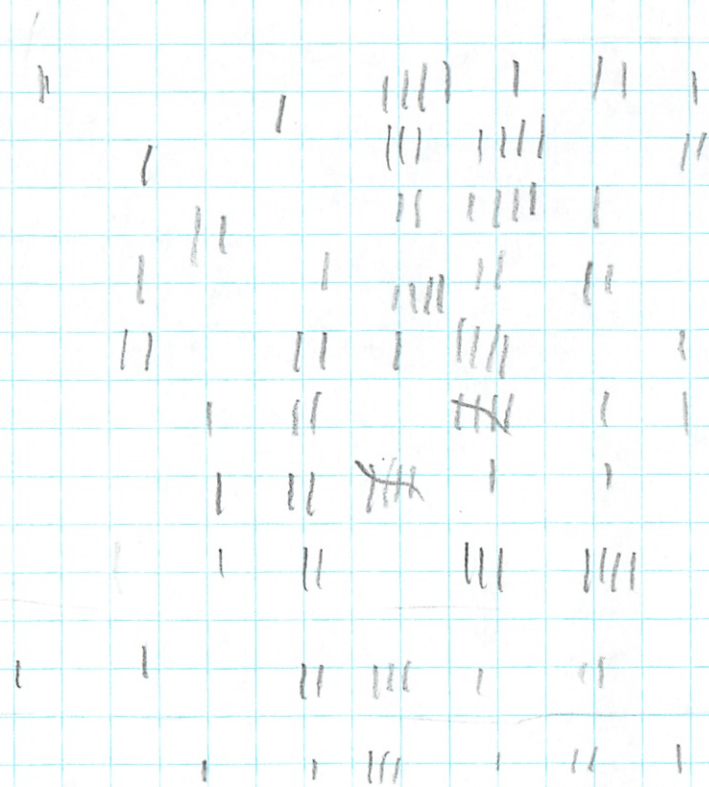
SS 302

Standard Deviation

see next pg



freq



all add to $518/98 = 5.28 = \text{mean}$

Median $\frac{515}{2} = 5$ 5 = median

mode 6

Range = 7

0	1	2	3	4	5	6	7	8	9	10
0	2	5	6	12	25	27	15	5	0	0

Use #3
data

Standard Deviation

P334

8/6

S.3 = mean

$$x_i - \bar{x} =$$

$$(x_i - \bar{x})^2 \text{ Freq}$$

$$1 - 5.3 = -4.3$$

$$18.49 \times 2$$

$$36.98$$

$$2 - 5.3 = -3.3$$

$$10.89 \times 5$$

$$54.45$$

$$3 - 5.3 = -2.3$$

$$5.29 \times 6$$

$$31.74$$

$$4 - 5.3 = -1.3$$

$$1.69 \times 12$$

$$20.28$$

$$5 - 5.3 = -.3$$

$$.09 \times 25$$

$$2.25$$

$$6 - 5.3 = .7$$

$$.49 \times 27$$

$$13.23$$

$$7 - 5.3 = 1.7$$

$$2.89 \times 15$$

$$42$$

$$8 - 5.3 = 2.7$$

$$7.29 \times 6$$

$$43.74$$

to make
all positive

x Freq

$$\frac{244.67}{98} = 2.4966$$

$$1.58 = 0$$

Create a set of data that matches each set of restrictions.

1. Martin played in 5 basketball games. The mean number of points that he scored was 12. The median number of points he scored was 14.

8, 8, 14, 14, 19 6 = must add to (5×12)

2. Denise played in 5 basketball games also. Her mean number of points scored is 18. Her range of points scored was 9.

12, 19, 19, 19, 21

3. Six students kept track of how much time they spent watching TV in a week. Their mean time was 8 hours. Their mode time was 9 hours.

8 6 6 9 9 18 order 6, 6, 8, 9, 9, 18

4. Ramon bought 5 books. Their mean cost was \$15.20. Their median cost was \$18. The most expensive book cost \$24.

5 6.50 18 19.5 24

$$15.20 \times 5 = 76 \quad 76 - 24 - 18 = 34$$

$$34/3$$

5. In a certain I.Q. test, an I.Q. of 100 is considered "average." Six students take this I.Q. test and have a mean score of 100,

- a. What is the greatest number of the six students who could have a score that is above "average?" Give a set of scores that demonstrates this.

0, 0, 0, 0, 0, 600 (5)

- b. What is the smallest number of the six students who could have a score that is above "average?" Give a set of scores that demonstrates this.

50 50 51 300 50 99 (1)

6. Garrison Keillor claims that in Lake Wobegon, Minnesota, "All the children are above average." Is this possible? Explain.

Yes, the average is figured from past tests and is nation-wide/international, figured

Dr PHD

X
The **mean** for a set of values is obtained by adding the numbers and dividing the result by the number of values that were added.

The **median** for a set of numbers is found by arranging the numbers in increasing or decreasing order, then choosing the middle number. For an even number of values, the median is obtained by taking the two middle numbers and averaging them.

The **mode** for a set of values is the number that occurs most often. If all of the numbers are different, there is no mode. If two different numbers occur most often then there are two modes.

The **range** for a set of data is the difference between the highest and lowest values.

1. For the following set of numbers, find the mean, median and mode (if any),

5, 8, 8, 11, 13

Mean: 9

Median: 8

Mode: 8 Range: 8

2. For the following set of numbers, find the mean, median and mode (if any),

15, 8, 12, 11, 4, 18, 14, 9

Mean: 11.375

Median: 11.5

Mode: —

Range: 14 ~~19~~

3. Marvin bought 5 items at a mean (average) cost of 40¢.

Find two different sets of prices that would give this result.

40 40 40 40 40

35 35 40 45 45

do $.40 \times 5$ and -1 at a time

↑ opps

4. Six students each worked on a term paper for their history class. They each spent a different whole number of hours on their papers. The average (mean) time spent by the students was 20 hours. The student who spent the least time spent 9 hours. The student who spent the most time spent 25 hours. Find three possibilities for the amounts of time the other 4 students spent on their papers.

9 20 20 21 25

9 21 21 23 21 25

9 18 18 25 25 25

25

Seven students were complaining about how much time they had to spend on schoolwork over their spring vacation. Their mean time was 15 hours. Make up a data set for each of the requirements given below. For each requirement, demonstrate that your data set meets the requirement by finding the mean, median, and mode.

1. The mean is larger than the median.

8, 9, 10, 11, 12, 15, 40
 Mean: 15 Median: 11 Mode: —

2. The median is larger than the mean.

5, 5, 10, 20, 20, 20, 25
 Mean: 15 Median: 20 Mode: 5

3. The mean is larger than the mode.

4, 4, 4, 13, 20, 30, 30
 Mean: 15 Median: 13 Mode: 4

4. The mode is larger than the mean.

4, 6, 7, 20, 20, 23, 25
 Mean: 15 Median: 20 Mode: 20

5. The mode is larger than the median.

3, 6, 7, 20, 23, 23, 23
 Mean: 15 Median: 20 Mode: 23

6. The median is larger than the mode.

4, 4, 4, 13, 25, 25, 30
 Mean: 15 Median: 13 Mode: 4

7. The mean, median, and mode are equal.

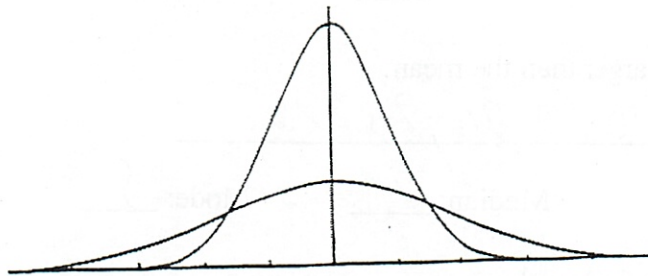
15, 15, 15, 15, 15, 15, 15
 Mean: 15 Median: 15 Mode: 15

105 Total

What Is Standard Deviation?

The **standard deviation** of a set of data measures how "spread out" the data set is. In other words, it tells you whether all the data items bunch around close to the mean or if they are "all over the place."

The superimposed graphs below show two normal distributions with the same mean, but the taller graph is less "spread out." Therefore, the data represented by the taller graph has a smaller standard deviation.



Calculation of Standard Deviation

Here is a list of the steps for calculating standard deviation.

1. Find the mean.
2. Find the difference between each data item and the mean.
3. Square each of the differences.
4. Find the average (mean) of these squared differences.
5. Take the square root of this average.

Organizing the computation of standard deviation into a table like the one on the next page can be very helpful. This table is based on a data set of five items: 5, 8, 10, 14, and 18. The mean for this data set is 11. The mean of a set of data is often represented by the symbol \bar{x} , which is read as "x bar."

The computation of the mean is shown below the table to the left. On the right below the table, step 4 of the computation of the standard deviation is broken down into two substeps: (a) adding the squares of the differences and (b) dividing by the number of data items. The symbol usually used for standard deviation is the lower case form of the Greek letter sigma, written σ .

Use!

See
 $x - \bar{x}$

x	$x - \bar{x}$	$(x - \bar{x})^2$
5	-6	36
8	-3	9
10	-1	1
14	3	9
18	7	49

sum of the data items = 55

number of data items = 5

\bar{x} (mean of the data items) = 11

sum of the squared differences = 104

mean of the squared differences = 20.8

σ (standard deviation) = $\sqrt{20.8} \approx 4.6$

Suppose you represent the mean as \bar{x} , use n for the number of data items, and represent the data items as x_1, x_2 , and so on. Then the standard deviation can be defined by the equation

$$\sigma = \sqrt{\frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}}$$

Standard Deviation and the Normal Distribution

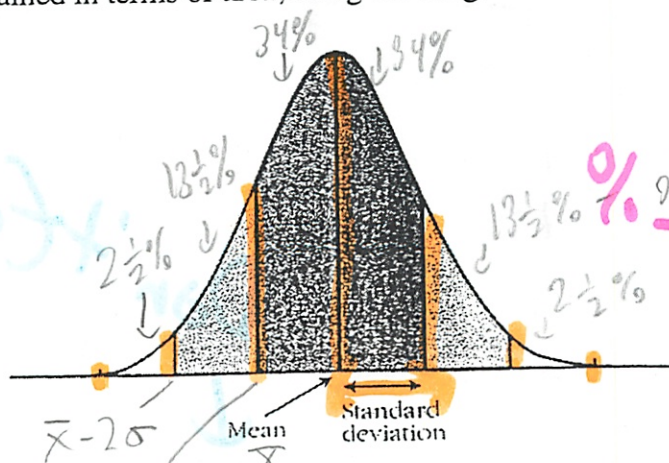
The normal distribution was identified and studied initially by a French mathematician, Abraham de Moivre (1667-1754). De Moivre used the concept of normal distribution to make calculations for wealthy gamblers. That was how he supported himself while he worked as a mathematician.

One of the reasons why standard deviation is so important for normal distributions is that there are some principles about standard deviation that hold true for any normal distribution. Specifically, whenever a set of data is normally distributed, these statements hold true.

Approximately 68% of all results are within one Standard deviation of the mean.

Approximately 95% of all results are within two standard deviations of the mean.

These facts can be explained in terms of area, using the diagram "The Normal Distribution."



The Normal Distribution

In this diagram, the darkly shaded area stretches from one standard deviation below the mean to one standard deviation above the mean; it is approximately 68% of the total area under the curve.

The light and dark shaded areas together stretch from two standard deviations below the mean to two standard deviations above the mean, and constitute approximately 95% of the total area under the curve.

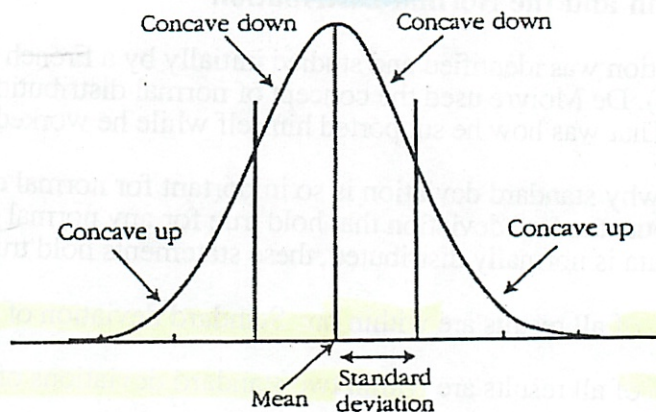
So standard deviation provides a good rule of thumb for deciding whether something is "rare."

Geometric Interpretation of Standard Deviation

Geometrically, the standard deviation for a normal distribution turns out to be the horizontal distance from the mean to the place on the curve where the curve changes from being concave down to concave up.

In the diagram "Visualizing the Standard Deviation," the center section of the curve, near the mean, is concave down, and the two "tails" (that is, the portions farther from the mean) are concave up.

The two places where the curve changes its concavity, marked by the vertical lines, are exactly one standard deviation from the mean, measured horizontally.



Practice

x	$x - \bar{x}$	$(x - \bar{x})^2$
5	-3	9
7	-1	1
8	0	0
9	1	1
11	3	9
$\bar{x} = 8$		$20/5 = 4$

Don't forget
the square root

↓
 $\sqrt{4} = 2$

Stand. Deviation Review

5/26

10

11

11

12

12

12

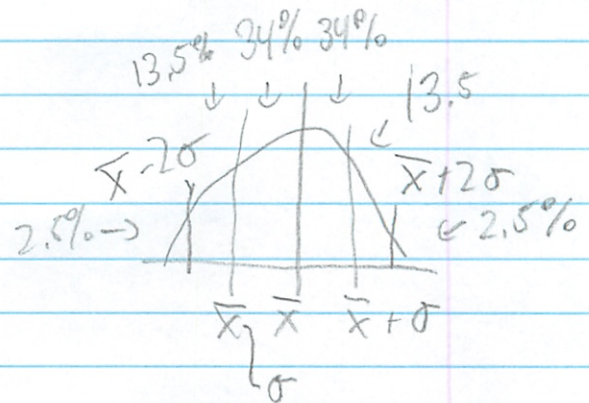
12

13

13

13

$\bar{x} = 11.9$
median - 12
mode - 12
range - 3
stand. div.

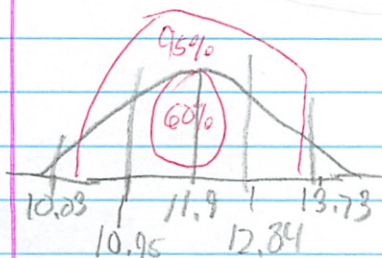


Stand
D.v

x_i	Freq(x_i)	$x_i - \bar{x}$	$(x_i - \bar{x})^2$	Freq(x_i)($x_i - \bar{x})^2$
10	1	-1.9	3.61	3.61
11	2	-.9	.81	1.62
12	4	.1	.01	.04
13	3	1.1	1.21	3.63
$n = 10$				8.90

Find \bar{x} $10(1) + 11(2) + 12(4) + 13(3)$
 $10 + 22 + 48 + 39$
 $\frac{119}{n = 10}$
 $= 11.9$

$\sigma = \sqrt{\frac{\sum f(x_i)(x_i - \bar{x})^2}{n}}$ $\sigma = 1.9433$



Data Practice

5/20

Measures
Central tend
 \bar{x}
Med:
Mode:
Range:
 σ
Graph w/
 $\sigma + \bar{x}$

x_i	$\text{freq}(x_i)$	$x_i - \bar{x}$	$(x_i - \bar{x})^2$	$\text{freq}(x_i)(x_i - \bar{x})^2$
0	0	-5.06	25.60	0
1	7	-4.06	16.48	115.36
2	36	-3.06	9.36	336.96
3	101	-2.06	4.24	428.24
4	125	-1.06	1.12	140
5	209	-0.06	.00	0
6	162	.94	.88	142.56
7	100	1.94	3.76	376
8	30	2.94	8.64	259.2
9	11	3.94	15.52	170.72
10	4	4.94	24.40	97.6

$$1(7) + 2(36) + 3(101) + 4(125) + 5(209) + 6(162) + 7(100) + 8(30) + 9(11) + 10(4)$$

$$\frac{2069.37}{n} = \frac{2069.37}{785} = 2.63$$

$$\sigma = 1.6225$$

So different

$$n = 785$$

$$7 + 72 + 303 + 500 + 1045 + 972 + 700 + 240 + 99 + 40$$

$$3978/n$$

$$3978/785 \approx 5.07 = \bar{x}$$

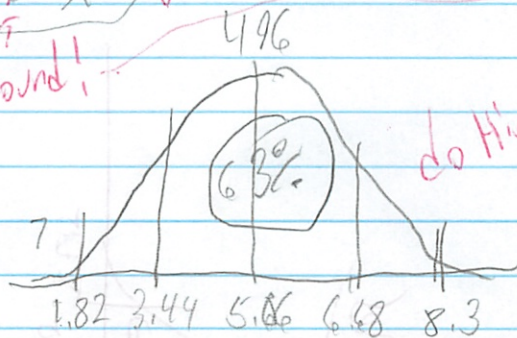
$$5.0675$$

round!

$$\text{Med} = 5$$

$$\text{Mode} = 5$$

$$\text{Range} = 9$$



do Histogram

Variance

σ = population standard deviation
large amount of data

S = sample standard deviation
small amount of data

$$763$$

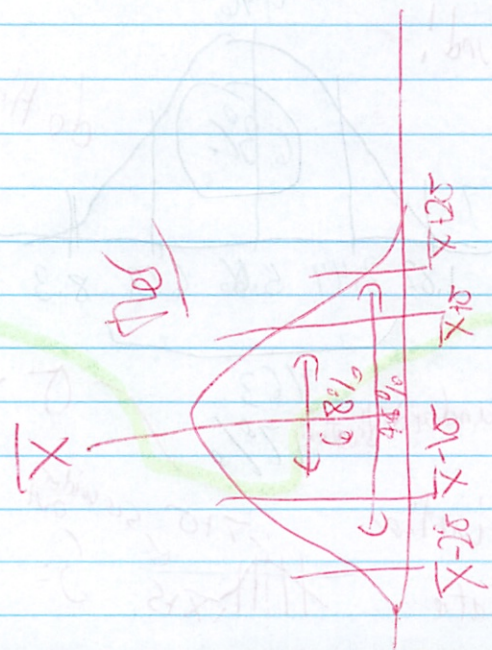
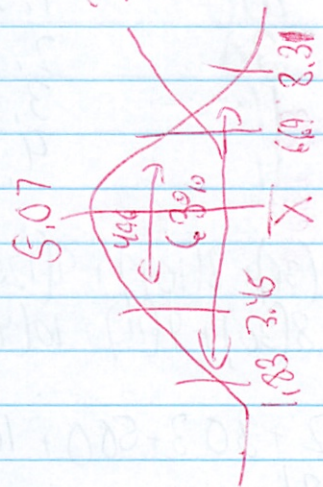
$$7\%$$

$$\sigma = \sqrt{\frac{\sum f(x_i)(x_i - \bar{x})^2}{n}}$$

$$S = \sqrt{\frac{\sum f(x_i)(x_i - \bar{x})^2}{n-1}}$$

$$\frac{763}{795} = 97\%$$

$$2 \leq x \leq 8$$



variance

Super Set

$$n = 124,249$$

x_i #	Freq
0	151
1	1171
2	5589
3	14518
4	25766
5	30475
6	25441
7	14322
8	5472
9	1199
10	145

off interest

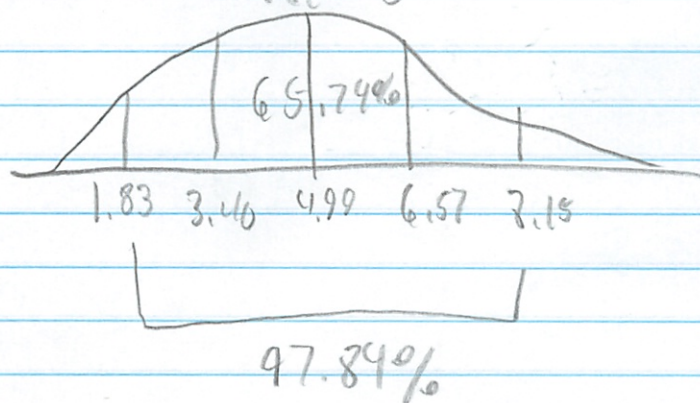
$$\bar{x} = 4.99$$

$$s = 1.5831$$

$$\text{Range} = 10$$

$$\text{median} = 5$$

$$\text{mode} = 5$$



In Class

over here

x_i	$f(x_i)$	$x_i f(x_i)$	$x_i - \bar{x}$	$(x_i - \bar{x})^2$	$f(x_i) / (x_i - \bar{x})^2$
14	7	98	-5.69	32.38	453.27
15	6	90	-4.69	22	131.98
16	11	176	-3.69	13.62	149.78
17	19	323	-2.69	7.24	137.44
18	44	792	-1.69	2.86	125.67
19	37	703	-.69	.48	17.62
20	38	766	.31	.10	2.59
21	25	525	1.31	1.72	112.90
22	27	594	2.31	5.34	144.57
23	14	322	3.31	10.96	63.34
24	15	360	4.31	18.58	278.64
25	4	100	5.31	28.26	112.78
26	2	52	6.31	39.82	79.63
27	1	27	7.31	53.44	53.44
		4922			1883.25

$\frac{250}{250} = n$

$\frac{4922}{250} = \bar{x}$
19.69

colour through me diff

watch

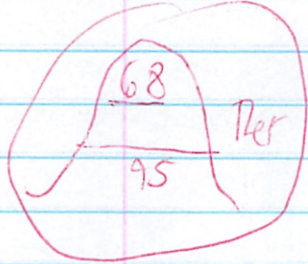
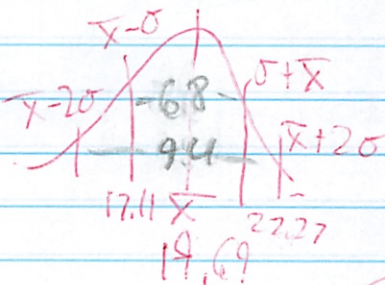
$\sigma = \sqrt{\frac{1883.25}{250}} = 2.74$
~~2.58~~

Should do w/ this!

Mode = ~~26~~ 18 Read!

Median = 20

Range = 13



~~Suppose to do this~~

MORE Data to

(1) Graph

(2) Find the mean, etc

x_i

$f(x_i)$

4.0

1

x_i

5.4

10

4.4

2

5.5

5

4.6

11

5.7

1

4.3

1

5.6

2

4.5

5

6.0

1

4.7

32

4.9

112

All MEASURES
OF Central Tendency

4.8

80

using
1-var
Gstat

$\bar{X} = 17.68$

5.0

131

$n = 34$

$\sigma = 31.26$

5.1

67

$S = 31.73$

$130 = \text{Range}$

5.2

29

Median = 5.05

Mode = 1

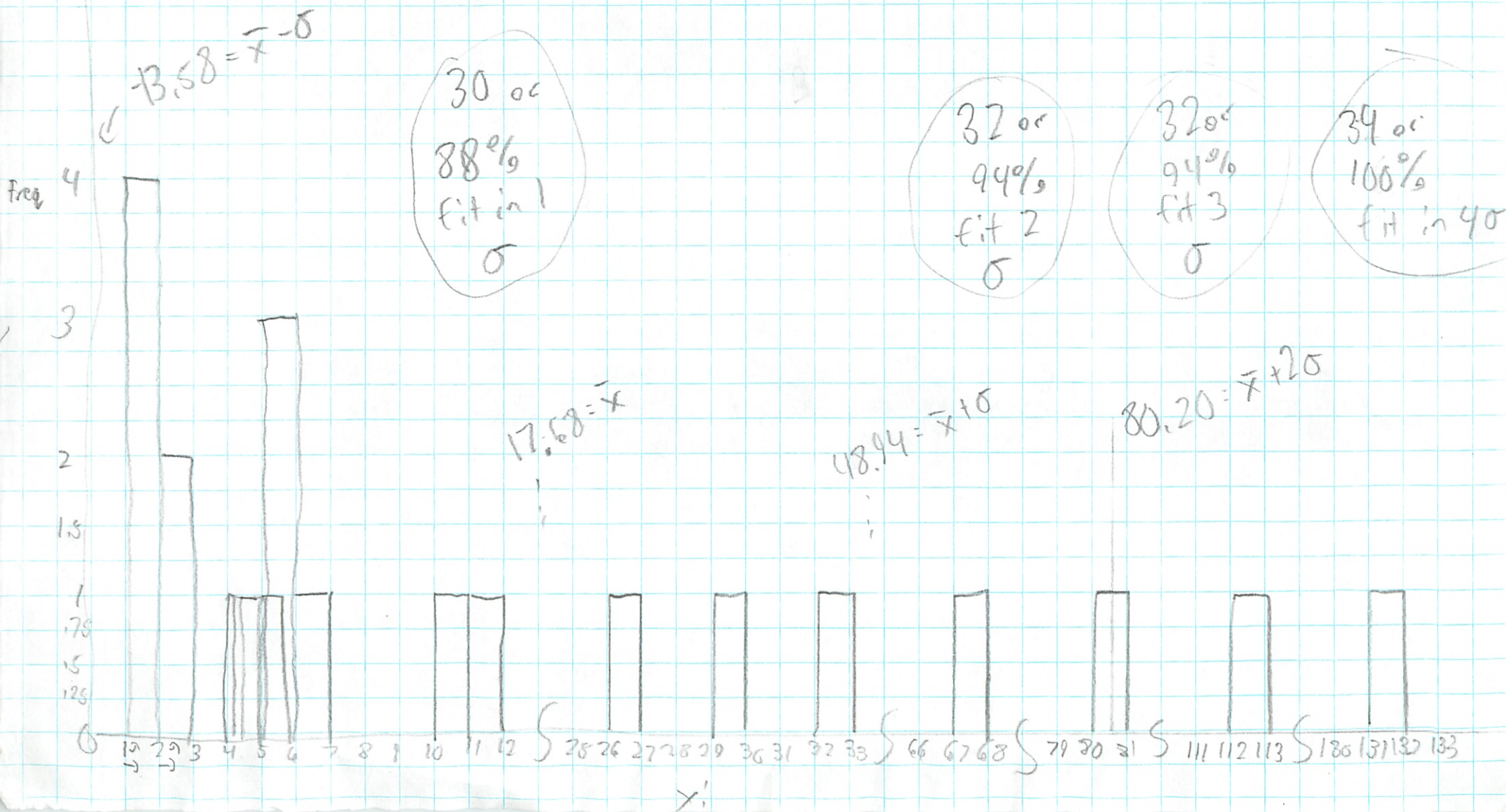
5.3

26

Data
By hand

		$x_i - \bar{x}$	$(x_i - \bar{x})^2$
1		-16.68	278.22
1		-16.68	278.22
1		-16.68	278.22
1		-16.68	278.22
2	Median = 5	-15.68	245.86
2	Range = 131 - 1 = 130	-15.68	245.86
4		-13.68	187.14
4.3	Median = 5 = 601/34 = 17.68	-13.38	179.02
4.4	n = 34	-13.28	176.36
4.5		-13.18	173.71
4.6		-13.08	171.09
4.7	$\Sigma (x_i - \bar{x})^2 = 33226.56$	-12.98	168.48
4.8	34 =	-12.88	165.89
4.9	977.25	-12.78	163.33
5	$\sqrt{\quad}$	-12.68	160.78
5	$\sigma = 31.26$	-12.68	160.78
5.1		-12.68	160.78
5.1	$\Sigma (x_i - \bar{x})^2 = 33226.56$	-12.58	158.26
5.2	33 =	-12.48	155.75
5.3	4.2 1606.87	-12.38	153.26
5.4	$\sqrt{\quad}$	-12.28	150.80
5.5	$\sigma = 31.73$	-12.18	148.31
5.6		-12.08	145.43
5.7		-11.98	143.52
6		-11.68	136.42
10		-7.68	58.93
11		-6.68	44.58
26		8.32	69.28
29		11.32	128.22
32		14.32	205.16
67		49.32	2432.81
80		62.32	3884.22
117	-131	94.32	8896.43
		-128.42	16510.88

Data



Warmup

5/26

1. $y = f(x) = x + 3$ - Find $f(3)$ (6)

$3 + 3 = 6$

$(0, 3)$
 $m=1$

$f(3) = 3 + 3 = 6$

f means function

$f(x)$ also means $y =$

2. $y = f(x) = 2x - 1$ Find $f(-1)$ - where x is put -1

$f = x - 1$

$x = -1$

$2(-1) - 1$

$-2 - 1$

$= -3$

$m=2$
 $(0, -1)$

$y = mx + b$

3. $g(x) = x^2 + 2x$ Find $g(6)$

$6^2 + 2(6)$

$36 + 12 = 48$

can have different letter

proper

$g(x) = x^2 + 2x$

$g(6) = 6^2 + 2x$

$= 36 + 12$

$= 48$

Function eval at 6 equals 48

Data

x_i	$\text{Freq}(x_i)$	$(x_i) \cdot \text{freq}(x_i)$	$x_i - \bar{x}$	$(x_i - \bar{x})^2$	$(x_i - \bar{x})^2 / \text{freq}(x_i)$
40	1	40	-9.65	93.12	93.12
41	0	0	0	0	0
42	0	0	0	0	0
43	1	43	-6.65	44.22	44.22
44	2	88	-5.65	31.92	63.85
45	5	225	-4.65	21.62	108.11
46	11	506	-3.65	13.32	146.55
47	37	1504	-2.65	7.02	224.77
48	80	3840	-1.65	2.72	217.80
49	112	5488	-0.65	0.42	47.32
50	131	6550	0.35	0.12	16.05
51	67	3417	1.35	1.82	122.11
52	29	1508	2.35	5.52	166.15
53	26	1374	3.35	11.22	291.79
54	10	540	4.35	18.92	189.23
55	5	275	5.35	28.62	143.11
56	1	56	6.35	40.32	40.32
57	1	57	7.35	54.02	54.02
58	0	0	0	0	0
59	0	0	0	0	0
60	1	60	10.35	107.12	107.12

$$\begin{aligned} \frac{515}{n} &= 257.5 \\ \frac{515}{n} &= 257.5 \\ \frac{515}{n} &= 257.5 \end{aligned}$$

$$\begin{aligned} \frac{2069.59}{515} &= 4.02 \\ \sqrt{4.02} &= 2.00 \\ \sigma &= 2.00 \end{aligned}$$

$$\text{Median} = 515/2 = 257.5$$

$$\text{Mode} = 50$$

$$\text{Range} = 60 - 40 = 20$$

Find central
tendency
Graph

$\bar{x} = 49.65$ Data 5/26

136
134
132
130
128
118
116
114
112
110
82
80
78
76
74
72
70
68
66
64
34
32
30
28
26
24
22
20
18
16
14
12
10
8
4
2

1st σ
 $48 < x < 51$
 $\frac{390}{515} = 76\%$

2nd σ
 $46 < x < 53$
 $\frac{488}{515} = 95\%$

$\bar{x} - \sigma = 47.65$

$\bar{x} + \sigma = 51.65$

$\bar{x} + 2\sigma = 53.65$

$\bar{x} - 2\sigma = 45.65$

$\bar{x} - 3\sigma = 43.65$

$\bar{x} + 3\sigma = 55.65$

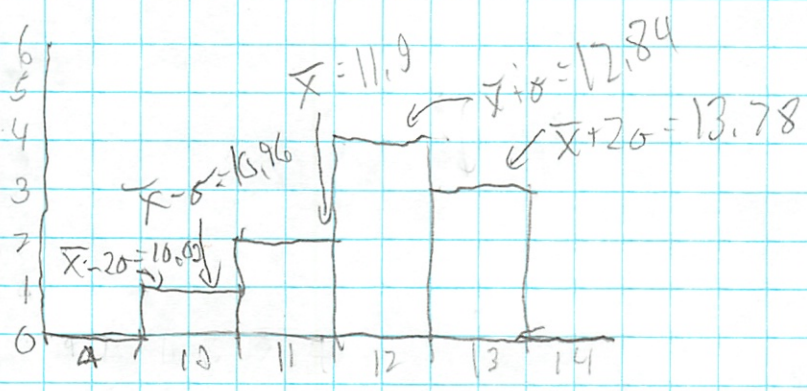
38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68

X_i	$\text{freq}(X_i)$	$x_i (\text{freq } x_i)$	$x_i - \bar{x}$	$(x_i - \bar{x})^2$	$\text{freq } x_i (x_i - \bar{x})^2$
10	1	10	-1.9	3.61	3.61
11	2	22	-0.9	.81	1.62
12	4	48	.1	.01	.04
13	3	39	1.1	1.21	3.63
		<u>110</u>			<u>8.9</u>
		10(n)			<u>10</u>
					5.89

$\bar{x} = 11.9$
 $n = 10$

Median - 12
 Mode - 12
 Range $13 - 10 = 3$

$1.94 = 5$



Then:
 $68 - 10$
 $95 - 20$

$11, 12$
 $2 + 4 = 6$
 $\frac{6}{10} = 60\%$
 in 10

$11, 12, 13$
 $6 + 3 = 9$
 $\frac{9}{10} = 90\%$
 in 20

~~57, 58, 60~~
~~72, 70, 67~~
~~62, 64, 65~~
~~63, 64, 65~~
~~63, 66, 64~~
~~66, 66~~

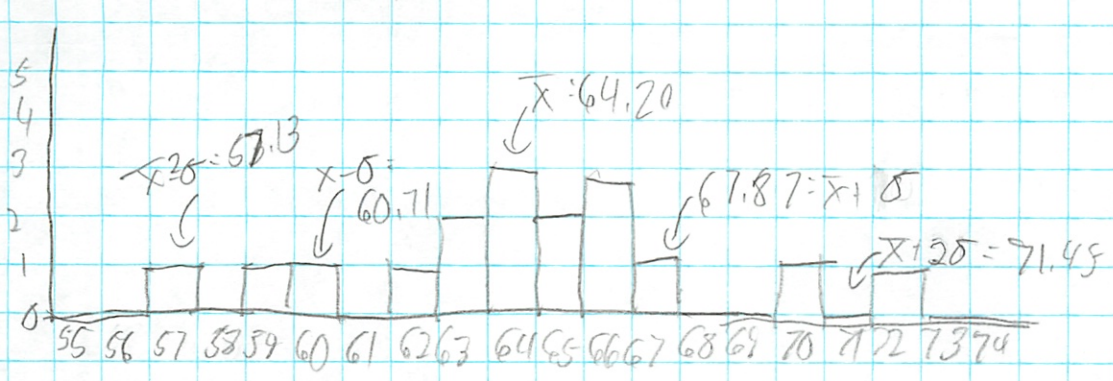
x_i	$f(x_i)$	$x_i f(x_i)$	$x_i - \bar{x}$	$(x_i - \bar{x})^2$	$f(x_i)(x_i - \bar{x})$
57	1	57	-7.29	53.2	53.2
58	0	0	-	-	0
59	1	59	-5.29	28.03	28.03
60	1	60	-4.29	18.44	18.44
61	0	0	-	-	0
62	1	62	-2.29	5.26	5.26
63	2	126	-1.29	1.67	3.35
64	3	192	-.29	.09	-.26
65	2	130	.71	.5	1
66	3	198	1.71	2.91	8.73
67	1	67	2.21	7.32	7.32
68	0	0	-	-	0
69	0	0	-	-	0
70	1	70	5.71	32.56	32.56
71	0	0	-	-	0
72	1	72	7.71	59.38	59.38

Median = 64
 Mode = 64 and 66
 Range 72 - 57 = 15

$\frac{17}{n}$
 $\frac{1043}{17} = 64.29$

$\frac{217.53}{17} = 12.80$
 $\sigma = 3.58$

3.58×0



1s: 61, 62, 63, 64, 65, 66, 67

$0 + 1 + 2 + 3 + 2 + 3 + 1$

$13 \rightarrow \frac{13}{17} = 76\%$ vers ther 86%

2s: 58, 59, 60, 68, 69, 70, 71

$0, 1, 1, 1, 3, 1, 0, 1, 0$

$16 \rightarrow \frac{16}{17} = 94\%$ vs. ther 95%

Name Michael Plasnoier 8848

Pit assessment

Date 6/1

(20 points)

20

Show all work in an organized way. (Columns and correct symbols could help!) Label all areas clearly. Be sure to show all necessary calculations.

Given the following data {10, 12, 13, 12, 13, 11, 12, 11, 13, 12} find:

(1 pt) 1) the mode 12 (1 pt) 2) the range 3

(1 pt) 3) the median 12 (1 pt) 4) the mean 11.9

(10 points) 5) the standard deviation 1.943

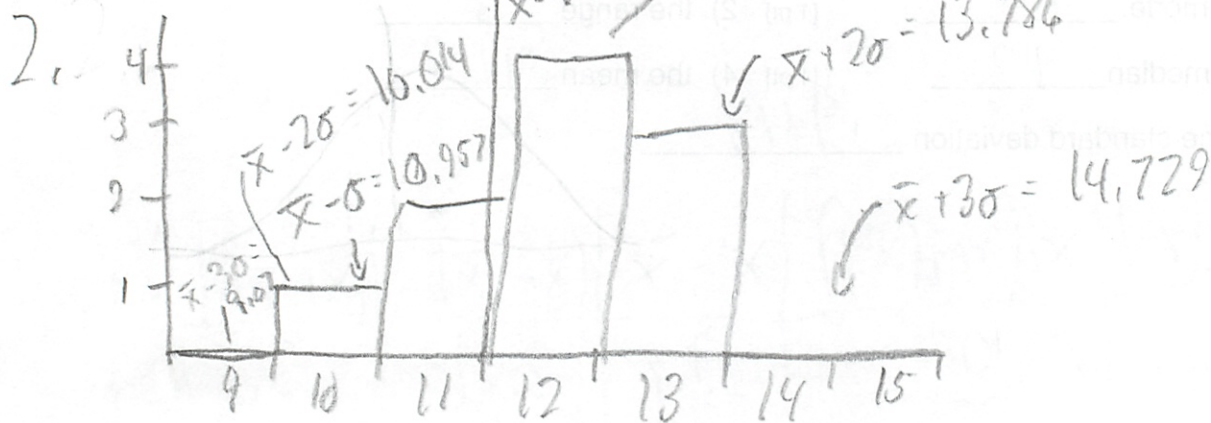
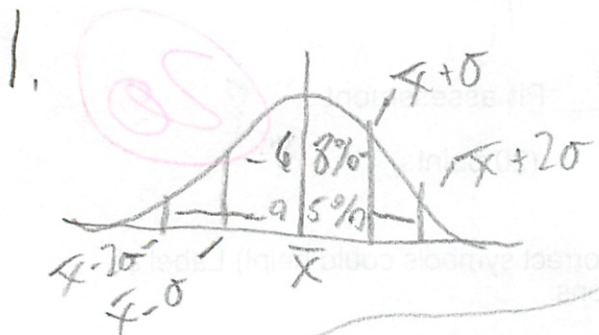
X_i	$\text{freq}(X_i)$	$X_i(\text{freq}(X_i))$	$X_i - \bar{X}$	$(X_i - \bar{X})^2$	$(X_i - \bar{X})^2 \text{freq}(X_i)$
10	1	10	-1.9	3.61	3.61
11	2	22	-.9	.81	1.62
12	4	48	.1	.01	.04
13	3	39	1.1	1.21	3.63
	<u>10 = n</u>	<u>119</u> 10 = <u>11.9 = \bar{X}</u>			<u>8.9</u> 10 = .890 <u>1.943 = \sigma</u>

Median = $10/2 = 5$ - Count 5 in \rightarrow (12)

Mode = 12

Range $13 - 10 = 3$

OVER



$1\sigma = 11, 12$
 $2 + 4 = 6$ or $\frac{6}{10} = 60\%$

$2\sigma = \dots 13$
 $6 + 3 = 9$ or $\frac{9}{10} = 90\%$

3.

2^{nd} $+$ 7 1 2 $Stat$ $Enter$ 1 0 $Enter$ 1 1 $Enter$ 1
 2 $Enter$ 1 3 $Enter$ \rightarrow 1 $Enter$ 2 $Enter$ 4 $Enter$
 3 $Enter$ $Stat$ \rightarrow $Enter$ 2^{nd} 1 1 2^{nd} 2 $Enter$